



UNIVERSITY OF  
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INSTITUTE OF  
PARTICLE  
PHYSICS



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# NEUTRINO OSCILLATION EXPERIMENTS

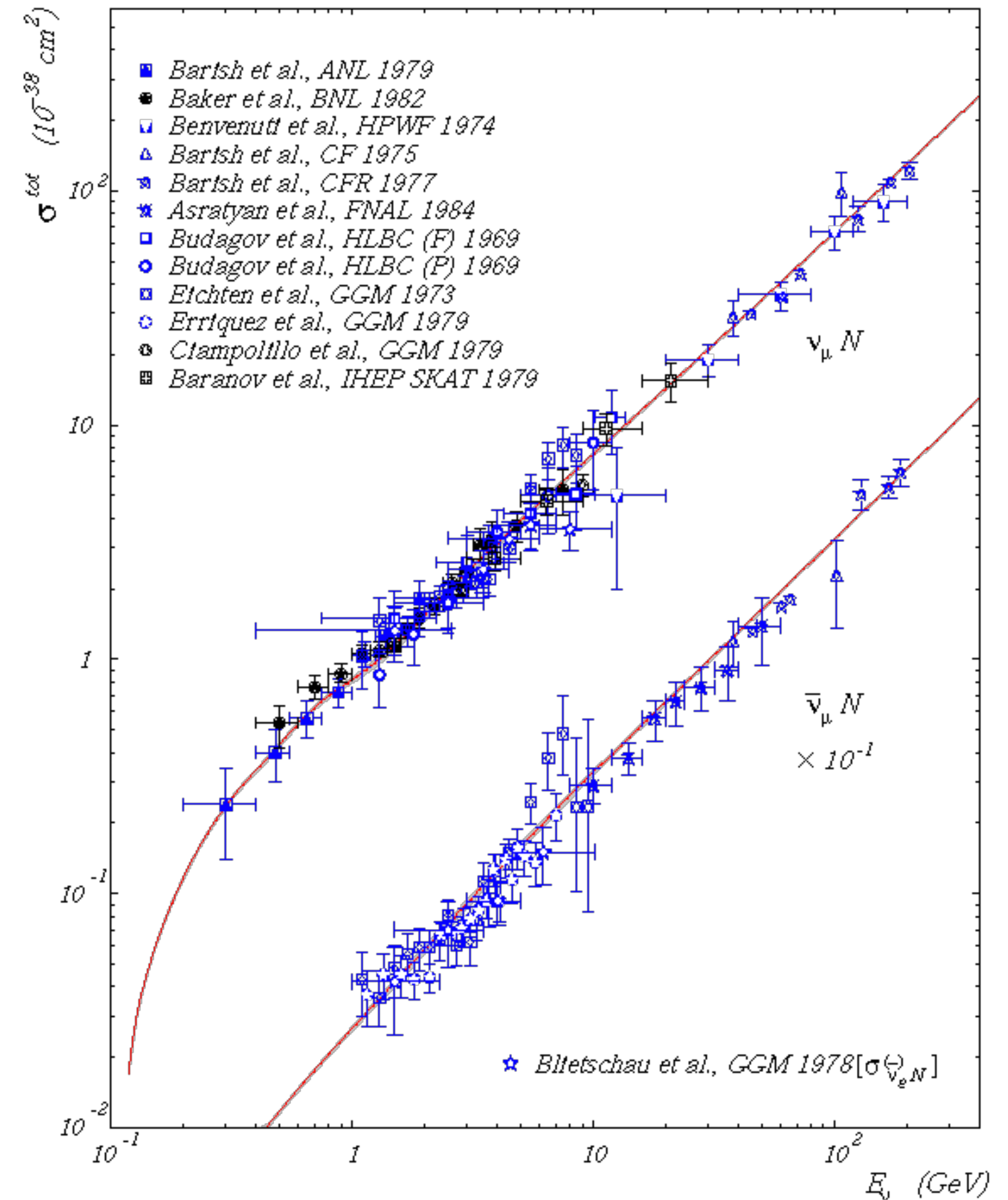
TRISEP 2016

# OVERVIEW

- Today:
  - Challenges of studying neutrinos experimentally
  - Neutrino sources
  - Basic categorization of neutrino detectors
  - Quick review of neutrino oscillations
  - “Classical era” of neutrino oscillations
    - reactor and solar neutrino oscillations
    - atmospheric neutrino oscillations
- Tomorrow:
  - Verifying atmospheric neutrino oscillations
    - accelerator-based experiments
  - Three-flavour mixing
    - $\nu_e$  appearance, CP violation,  $\theta_{23}$  octant, mass hierarchy . . .
  - Other relevant measurements and anomalies.

# NEUTRINO INTERACTION CROSS SECTION

- Fundamental challenge of neutrino experiments
- How to put  $\sigma = 10^{-38} \text{ cm}^2$  in perspective?
  - this is the typical cross section for 1 GeV neutrino
- Recall how to obtain "interaction length"
- $1/L = \sigma \times n$ 
  - $\sigma =$  cross section ( $\text{cm}^2$ )
  - $n =$  number density of target particles
  - for normal matter with  $\rho \sim O(1 \text{ gm/cm}^3)$   $n \sim N_A/\text{cm}^3 = 10^{24}/\text{cm}^3$
  - $L \sim 10^{11} \text{ cm} = 10^{14} \text{ km} \sim 10 \text{ light years}$
- If we consider lead ( $\rho = 11.35 \text{ g/cm}^3$ )
  - The interaction length of a 1 GeV neutrino is  $\sim 1$  light year in lead.
  - in comparison,  $L_{\text{rad}}$  for a photon is 0.56 cm
- Illustrates the weakness of the weak interaction at low energy
  - alternatively the massiveness of the W and Z



# NEUTRINO ECONOMICS

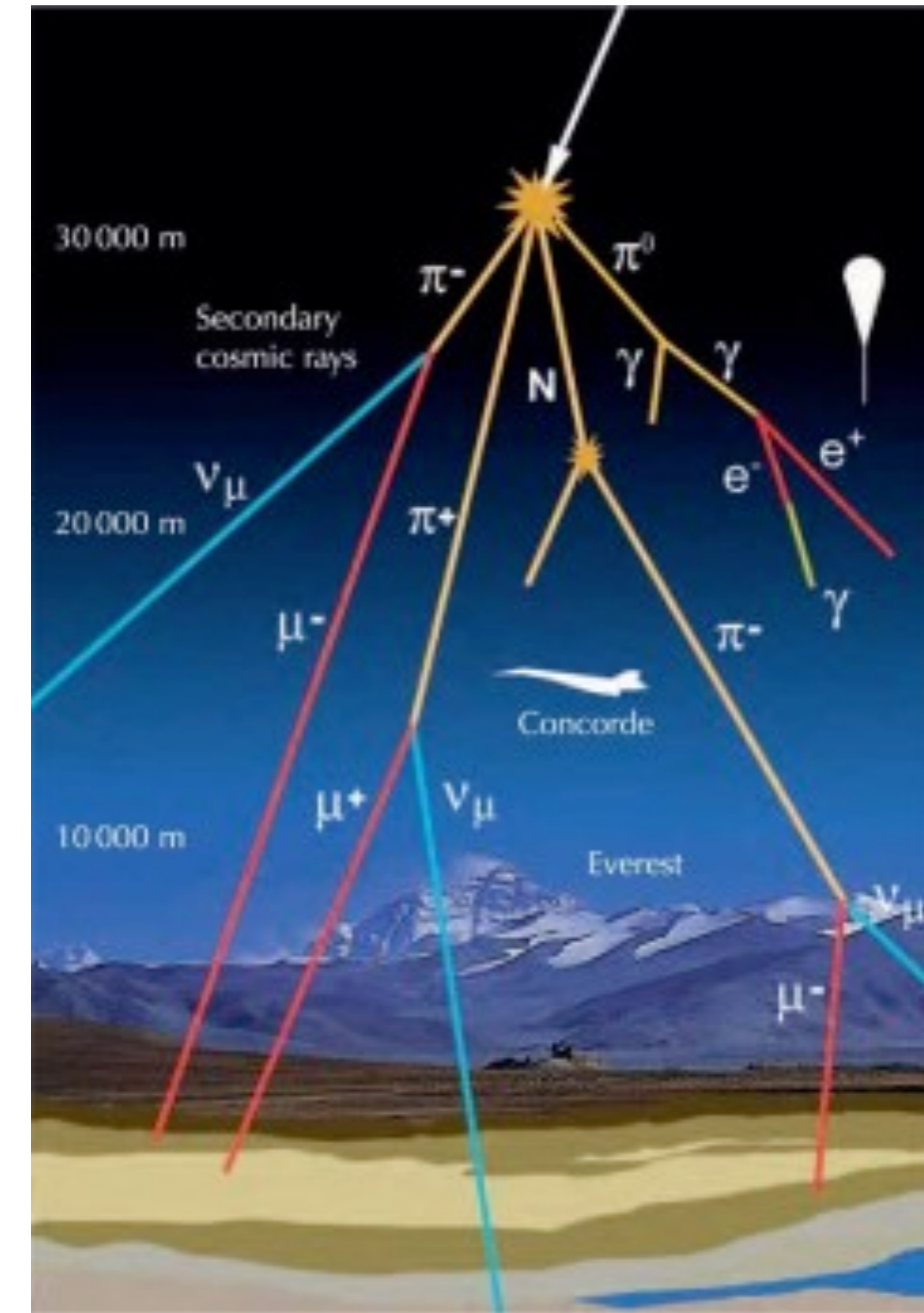
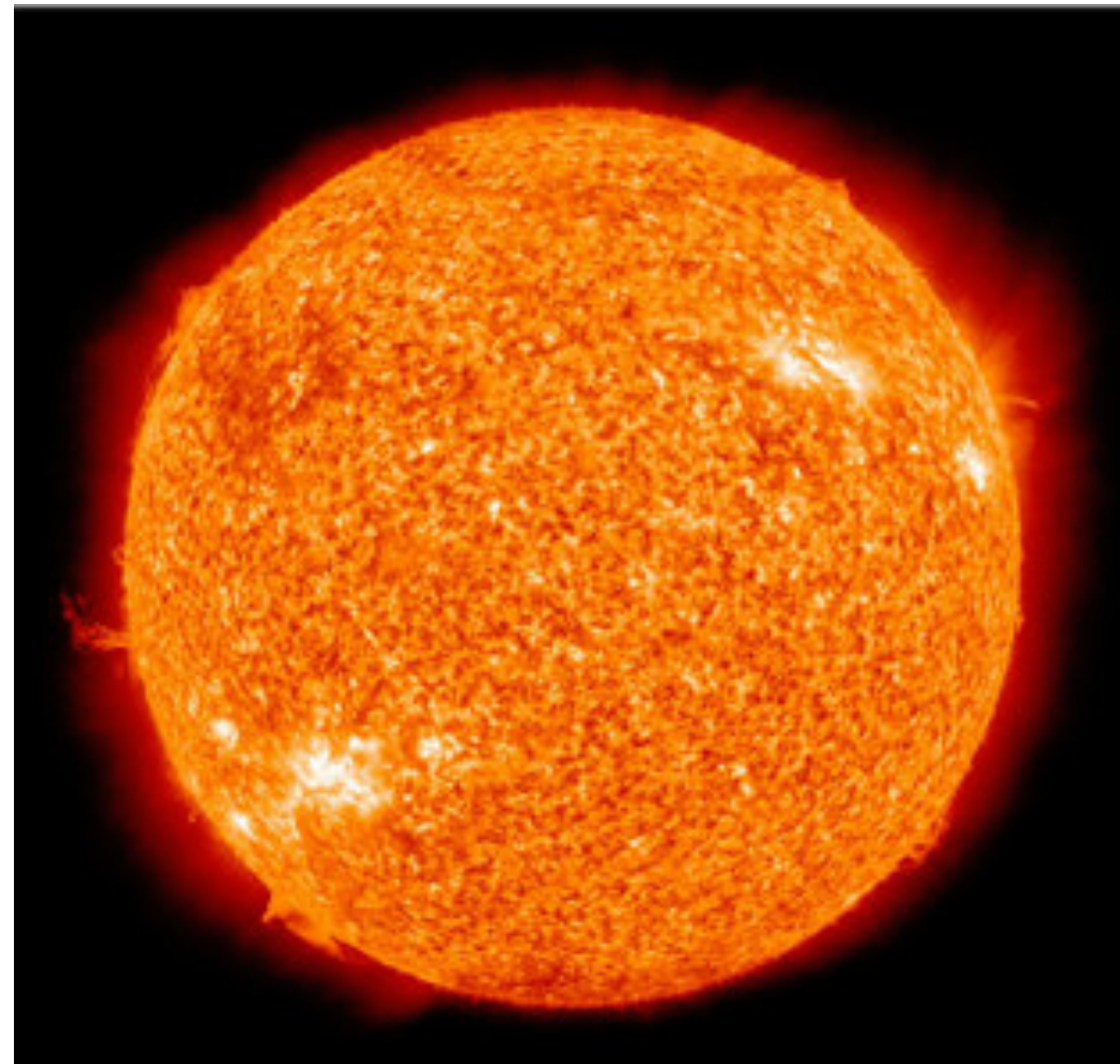
$$R = \varphi \times \sigma \times V \times n$$

- R: rate of neutrino interactions (/sec)
  - $\varphi$ : flux of neutrinos (neutrinos/cm<sup>2</sup>/sec)
  - $\sigma$ : neutrino cross section on target(cm<sup>2</sup>)
  - V: size of detector (cm<sup>3</sup>)
  - n: number density of target particles in detector
- Neutrino experiments need:
  - intense neutrino sources (maximize  $\varphi$ )
  - large detectors (maximize  $V \times n$ )

H. Bethe and R. Peirels:

- **"there is no practically possible way of observing the neutrino"**

# NEUTRINO SOURCES



- Nuclear decays:
  - solar
    - 3% of sun's energy radiated as neutrinos
    - $10^{11}$   $\nu/cm^2/sec$  on surface of earth
  - reactor:
    - ~5% of reactor power emitted as antineutrinos
    - $10^{20}$   $\bar{\nu}/sec$  emitted by typical GW reactor
  - Typical energy  $\sim O(MeV)$ 
    - only  $\nu_e$  charged-current and neutral current interactions visible

- Meson/muon decays
  - e.g. pion decay ( $\pi \rightarrow \nu_{\mu} + \mu$ )
  - atmospheric neutrinos
    - $\pi/K/\mu$  produced in atmosphere by cosmic ray protons
  - accelerator-based neutrinos
    - $\pi/K/\mu$  produced by high energy protons produced by accelerators
  - Typical energy  $\sim O(GeV)$ 
    - can observe charged current interactions of  $\nu_e, \nu_{\mu}, \nu_{\tau}$ , sometimes  $\nu_{\tau}$

# FIRST IDEA:

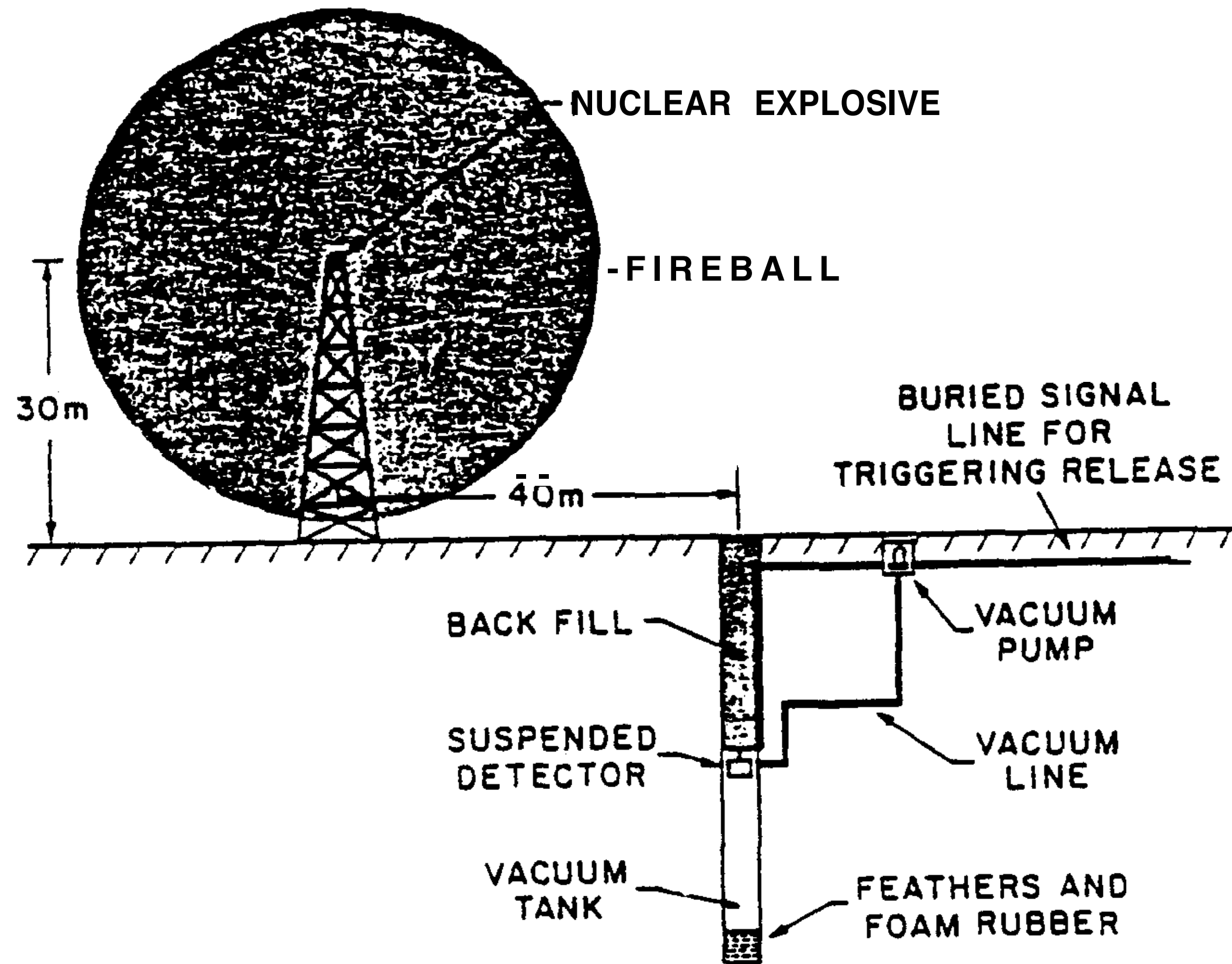
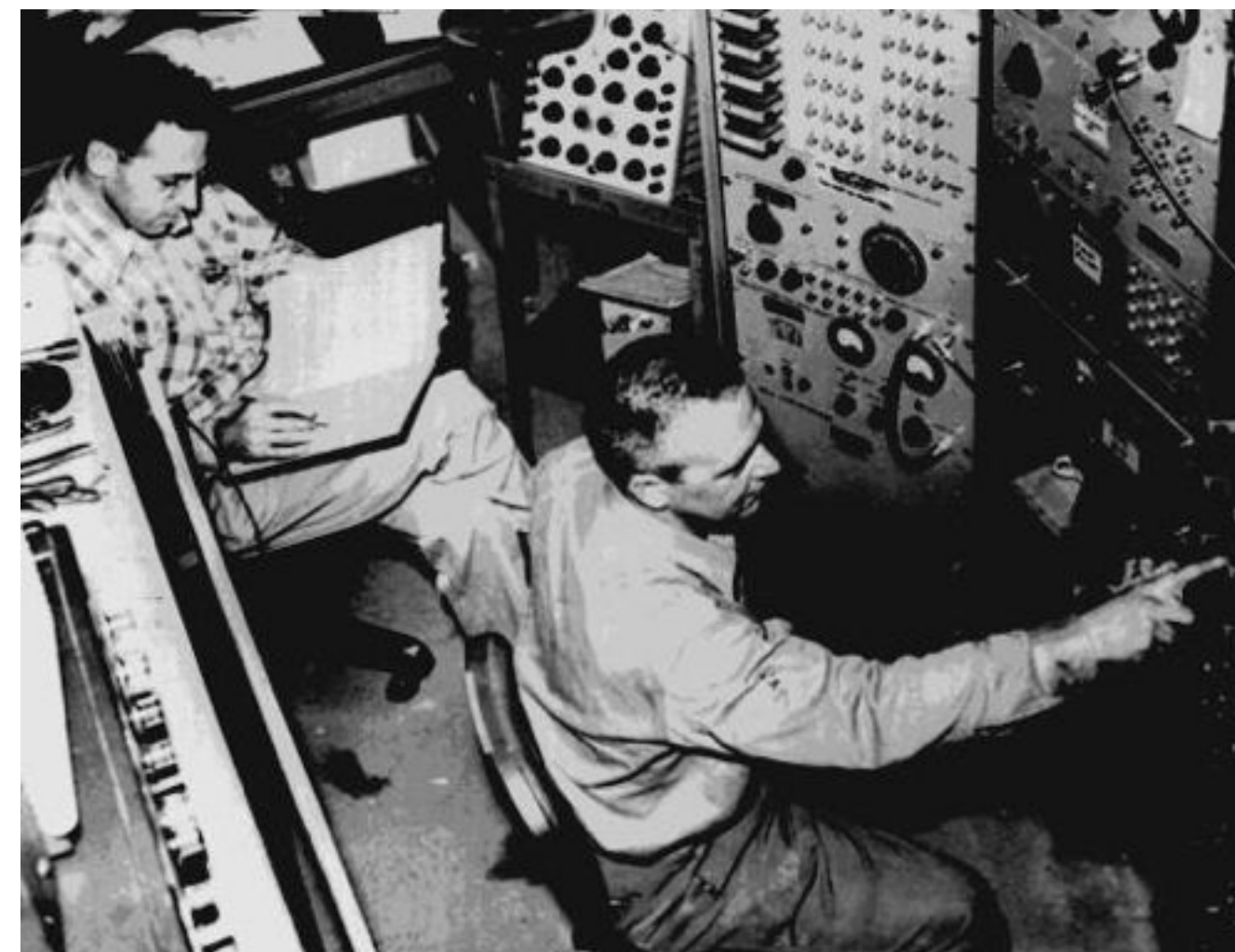


Figure 1. Sketch of the originally proposed experimental setup to detect the neutrino using a nuclear bomb. This experiment was approved by the authorities at Los Alamos but was superseded by the approach which used a fission reactor.

So why did we want to detect the free neutrino? Because everybody said, you couldn't do it. Not very sensible, but we were attracted by the challenge. After all, we had a bomb which constituted an excellent intense neutrino source. So, maybe we had an edge on others. Well, once again being brash,

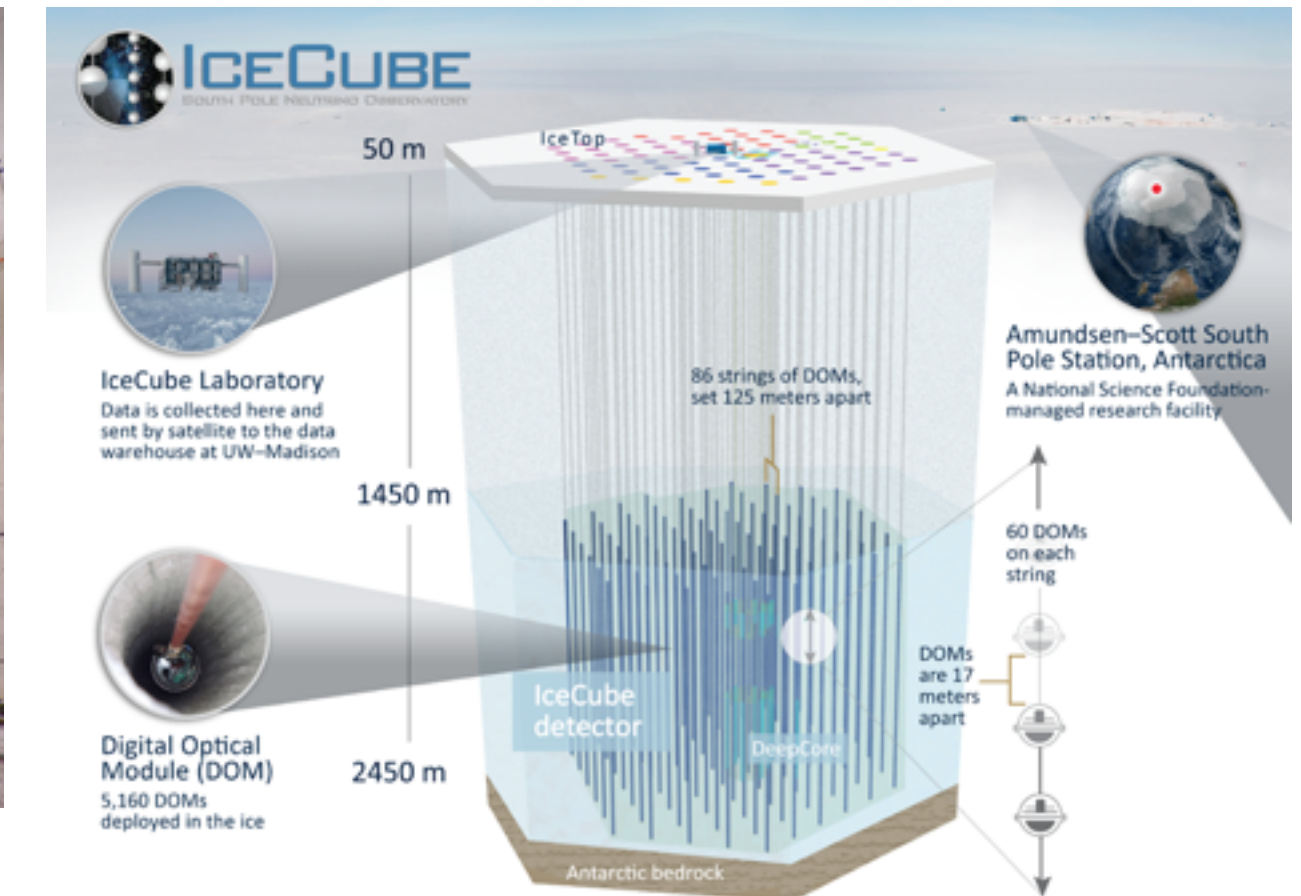
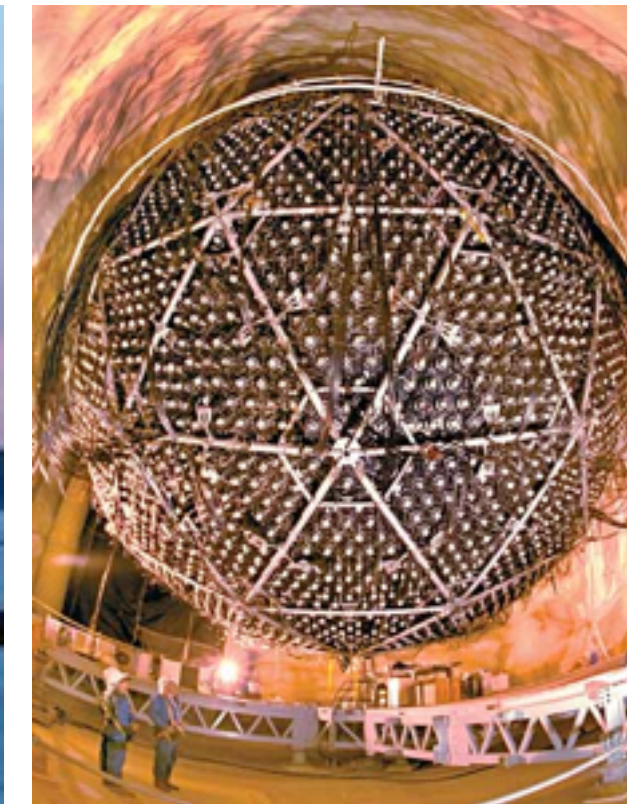
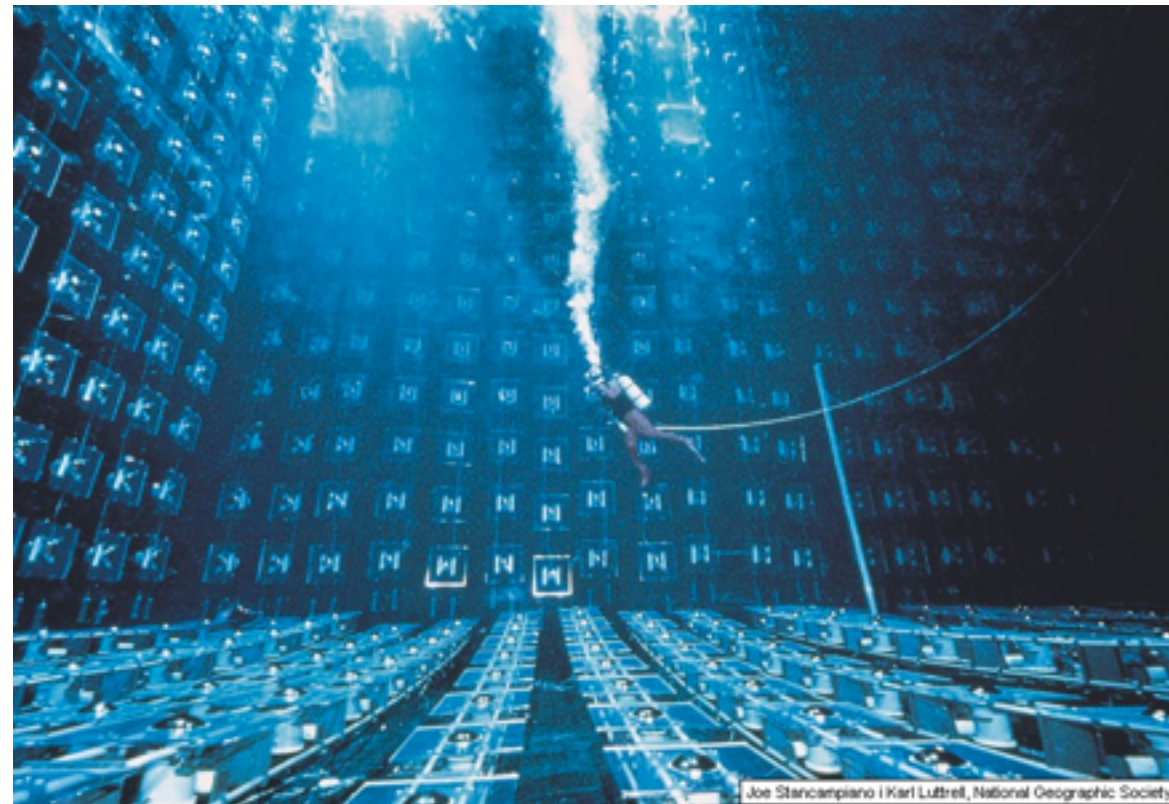
It happened during the summer of 1951 that Enrico Fermi was at Los Alamos, and so I went down the hall, knocked timidly on the door and said, "I'd like to talk to you a few minutes about the possibility of neutrino detection." He was very pleasant, and said, "Well, tell me what's on your mind?" I said, "First off as to the source, I think that the bomb is best." After a moment's thought he said, "Yes, the bomb is the best source." So far, so good! Then I said, "But one needs a detector which is so big. I don't know how to make such a detector." He thought about it some and said he didn't either. Coming from the Master that was very crushing. I put it on the back

The idea that such a sensitive detector could be operated in the close proximity (within a hundred meters) of the most violent explosion produced by man was somewhat bizarre, but we had worked with bombs and felt we could design an appropriate system. In our bomb proposal a detector would be sus



F. Reines (1995 Nobel Lecture)

# NEUTRINO DETECTORS

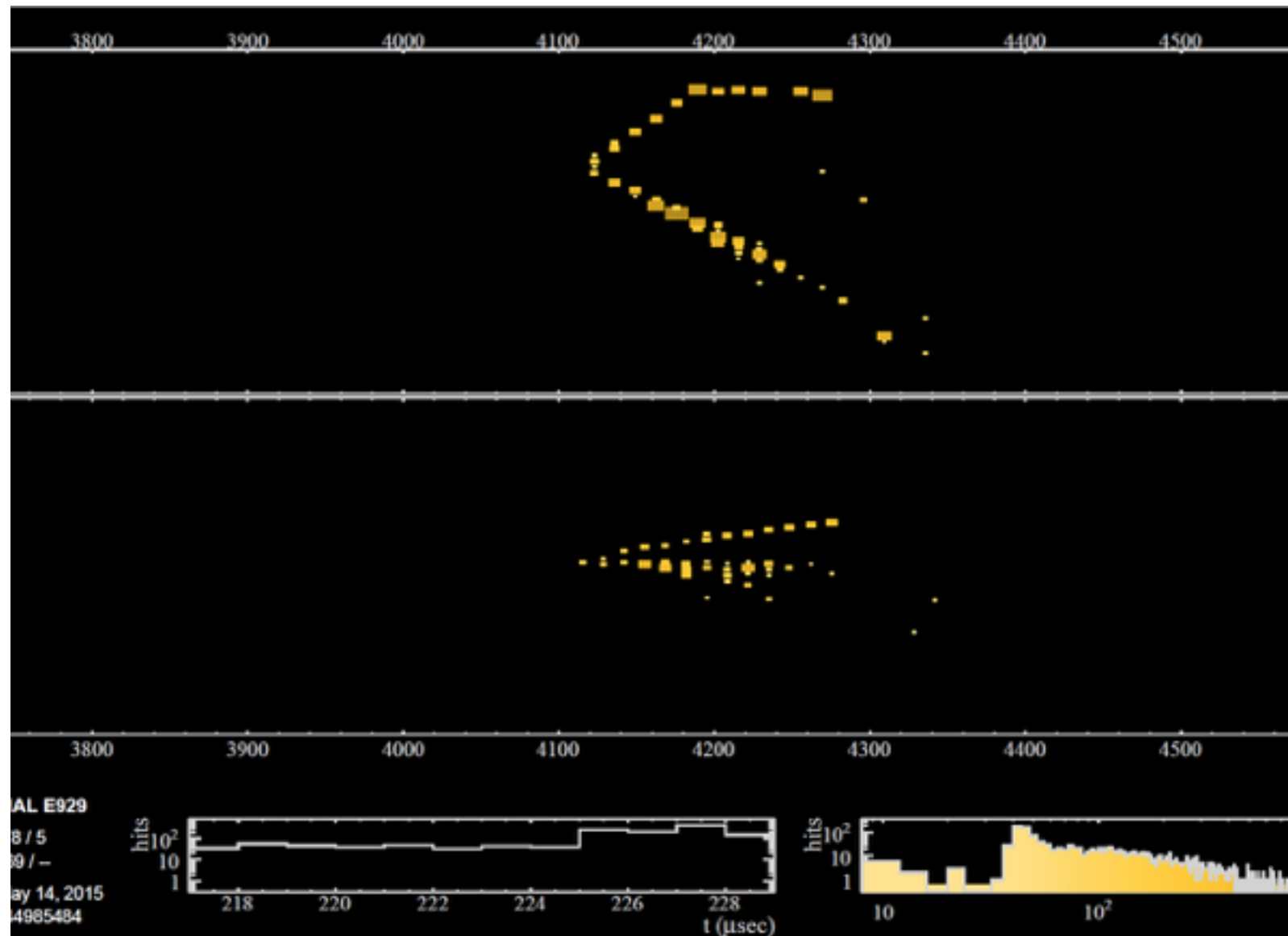


- Large detector/volume needed to gather neutrino interactions
  - neutrino detectors have long been about scalability
    - massive detectors that provide the information we need about the neutrino interactions
    - steel from decommissioned battleships
    - mineral oil/scintillator
    - large extruded PVC cells



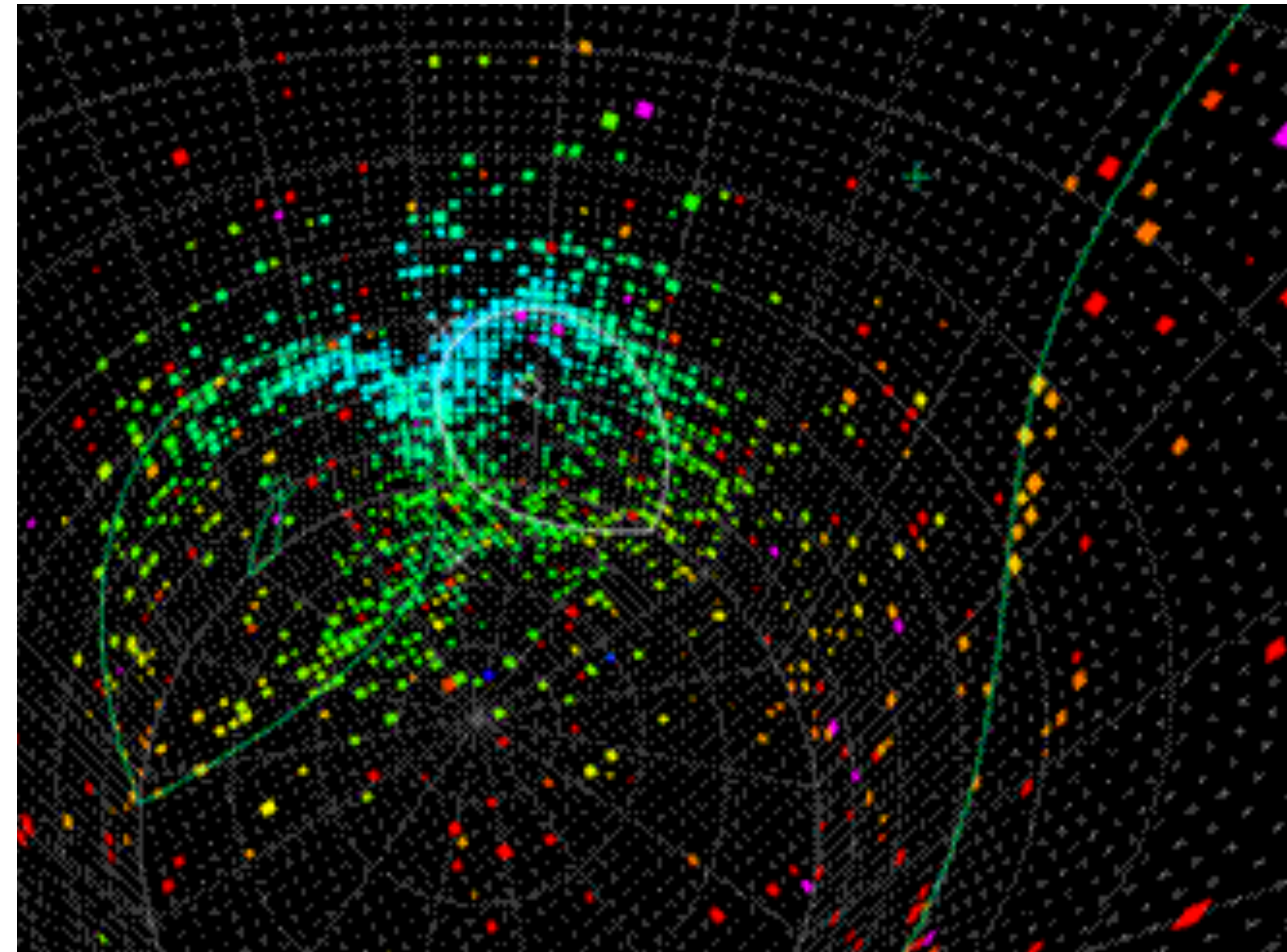
Hans Bethe: you shouldn't believe everything you read in papers

# BASIC DETECTOR TYPES



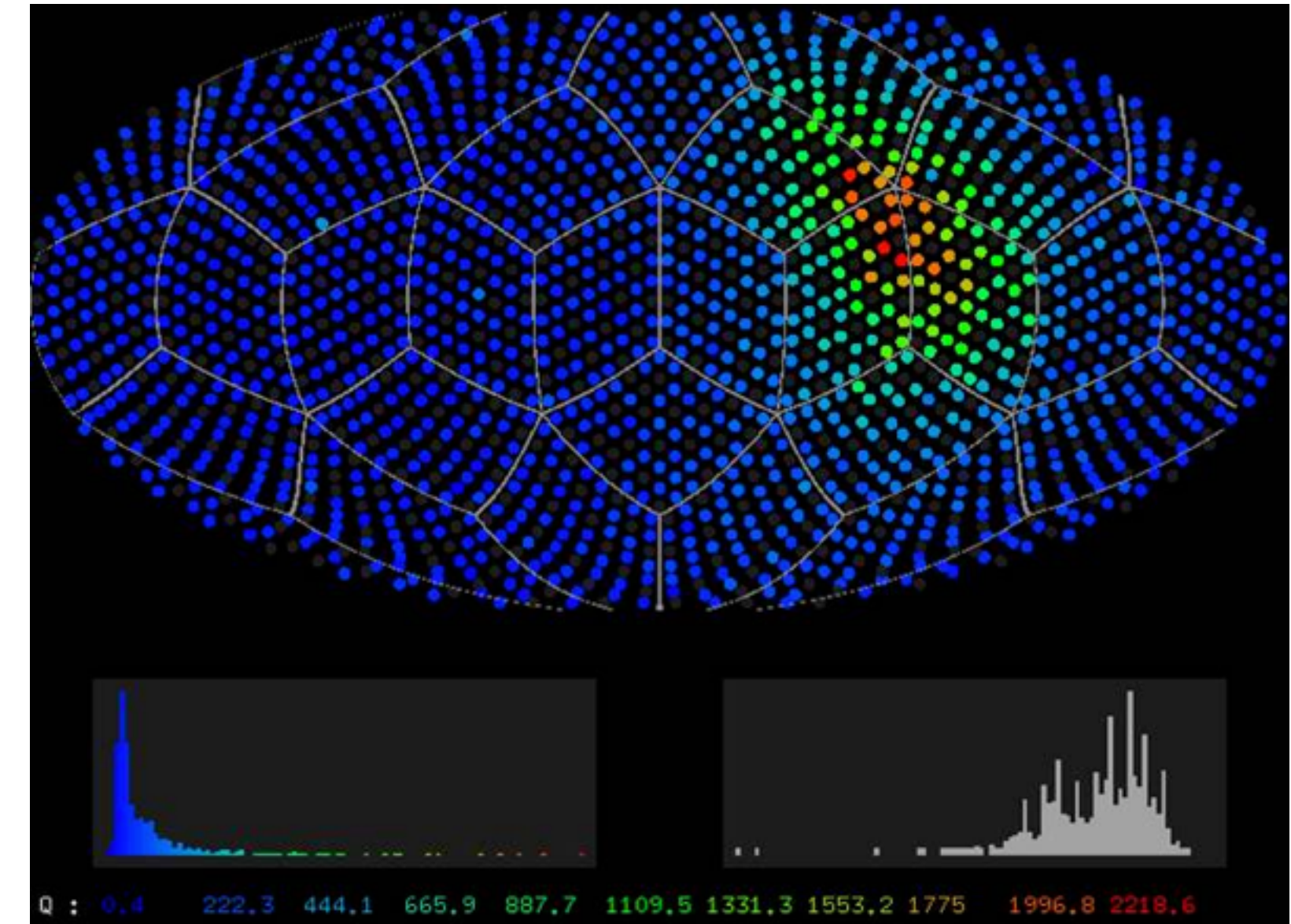
- Tracking detectors

- detector elements "track" charged particles based on ionization
- can allow detailed characterization of outgoing particles
  - segmented scintillator bars
  - photographic emission
  - drift ionization in gas or liquid
- particularly powerful in high energy interactions



- Cherenkov Detectors

- detect "fast" particles exceeding the velocity of light in a medium (e.g. water)
- cone of radiation detected with photosensors
- multiple particle final states identified by multiple rings



- Scintillation detectors

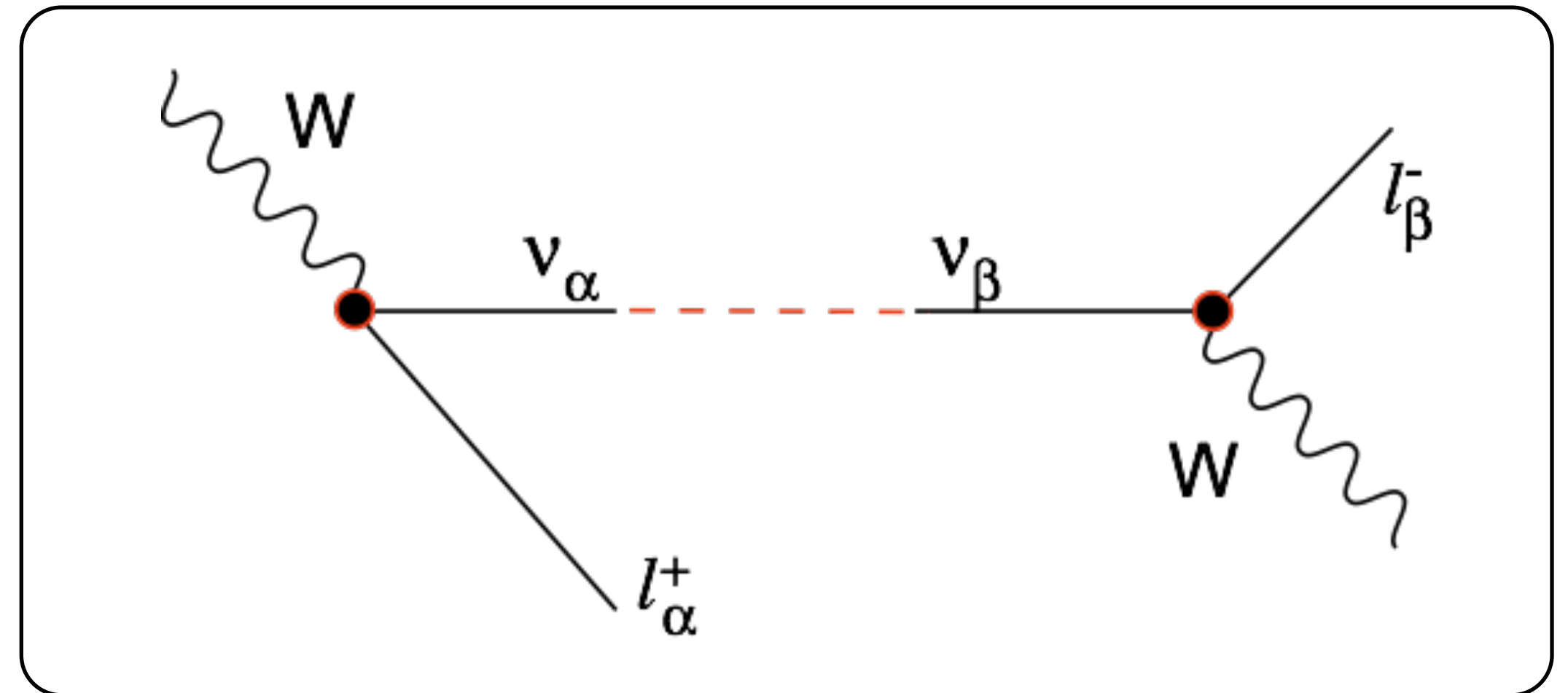
- typically large volume of liquid scintillator
- ionization converted into large yield of optical photons detected with photosensors
- often used for low energy neutrinos where energy resolution and backgrounds reduction are critical



# QUICK REVIEW OF NEUTRINO OSCILLATIONS

- Neutrino flavour states (created or interacting via the weak decays) are linear combinations of mass/energy eigenstates

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$$



- Time evolution: flavour content "oscillates" in  $L(\text{distance})/E(\text{neutrino})$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \Re(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 [1.27 \Delta m_{ij}^2 (L/E)] + 2 \sum_{i>j} \Im(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin [2.54 \Delta m_{ij}^2 (L/E)]$$

*in vacuo*

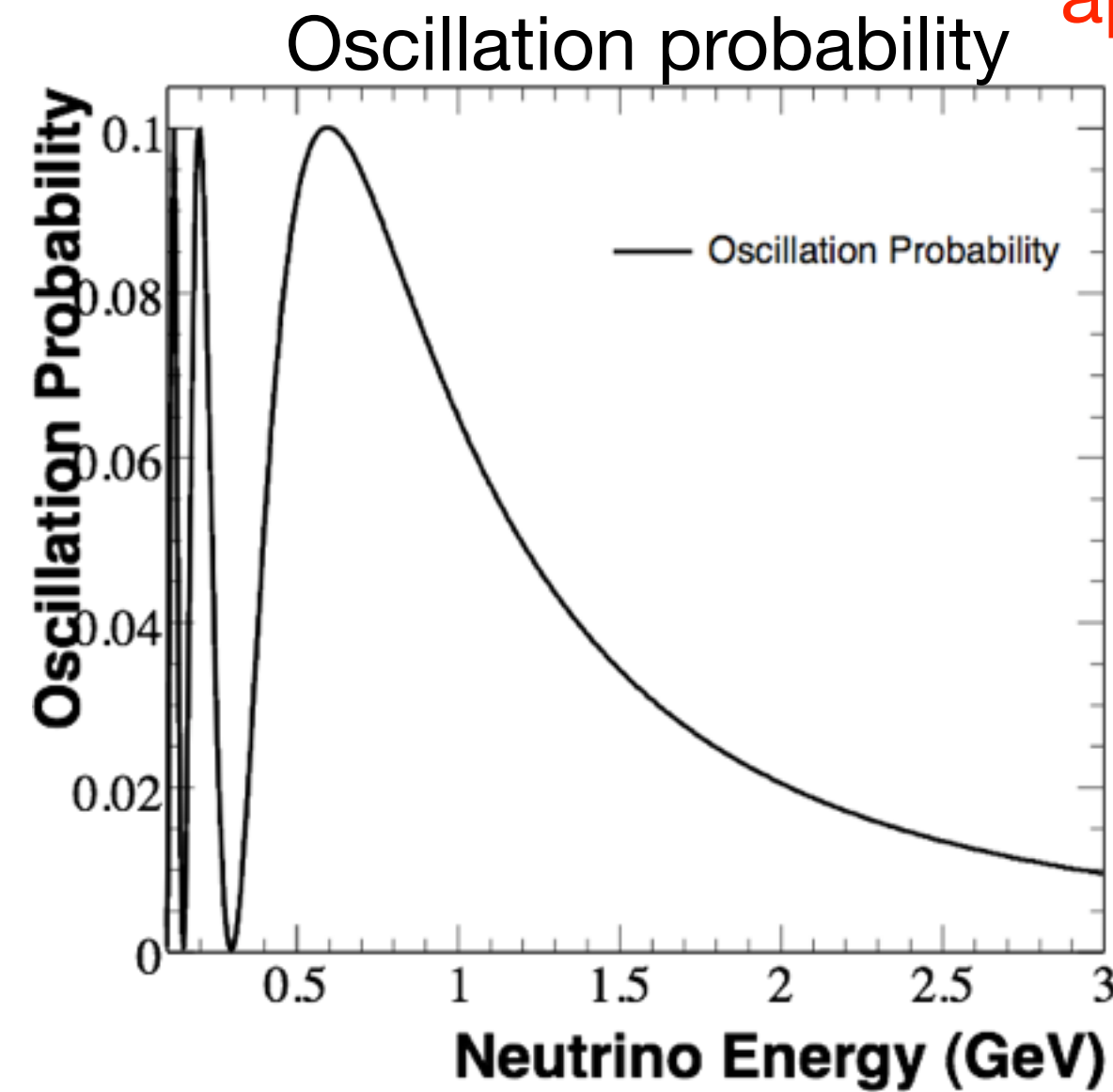
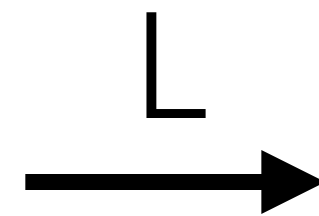
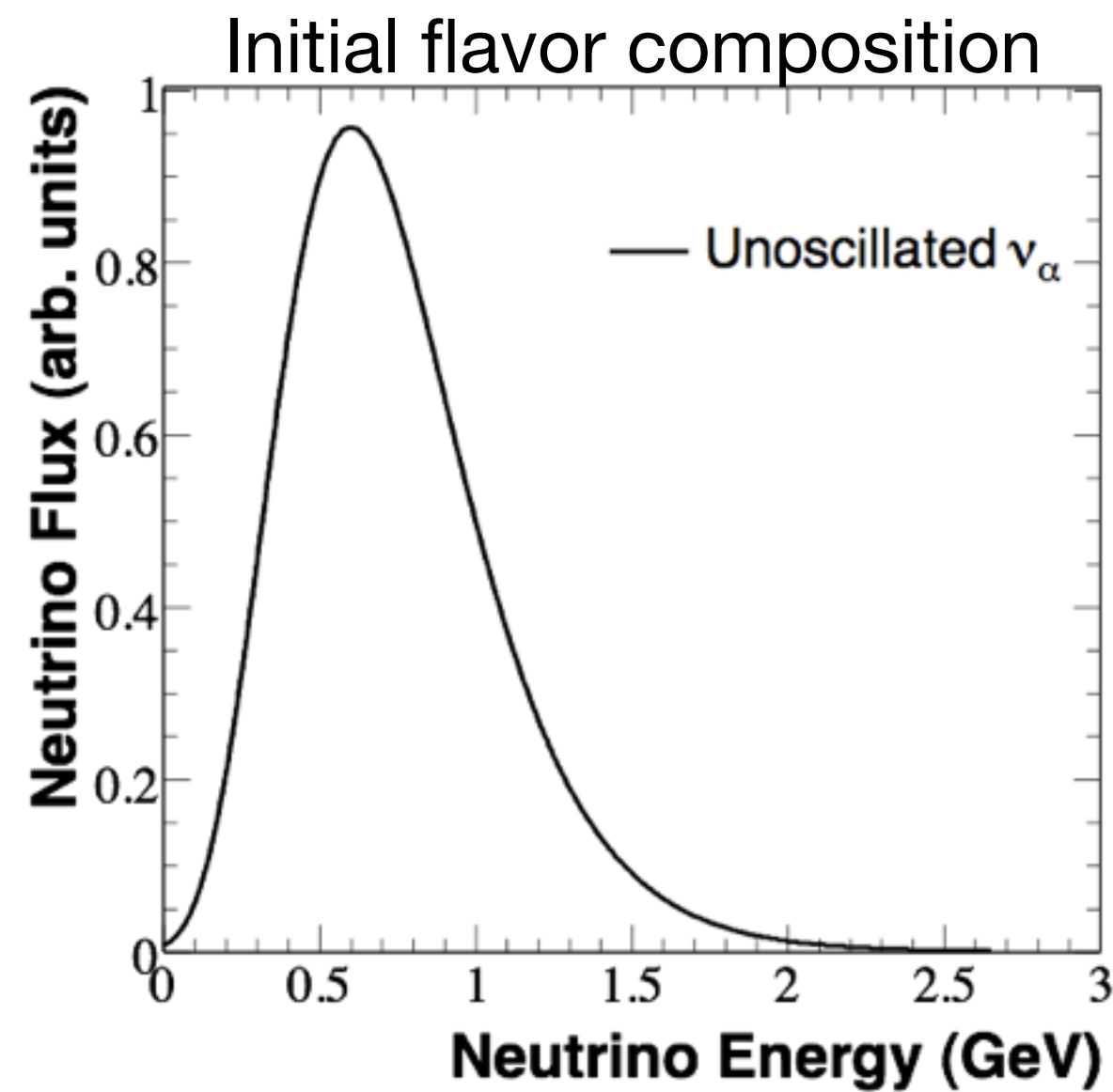
additional effects in the presence of matter

- Amplitudes determined by mixing matrix  $U_{ij}$
- Wavelengths determined by mass<sup>2</sup> differences  $\Delta m_{ij}^2$

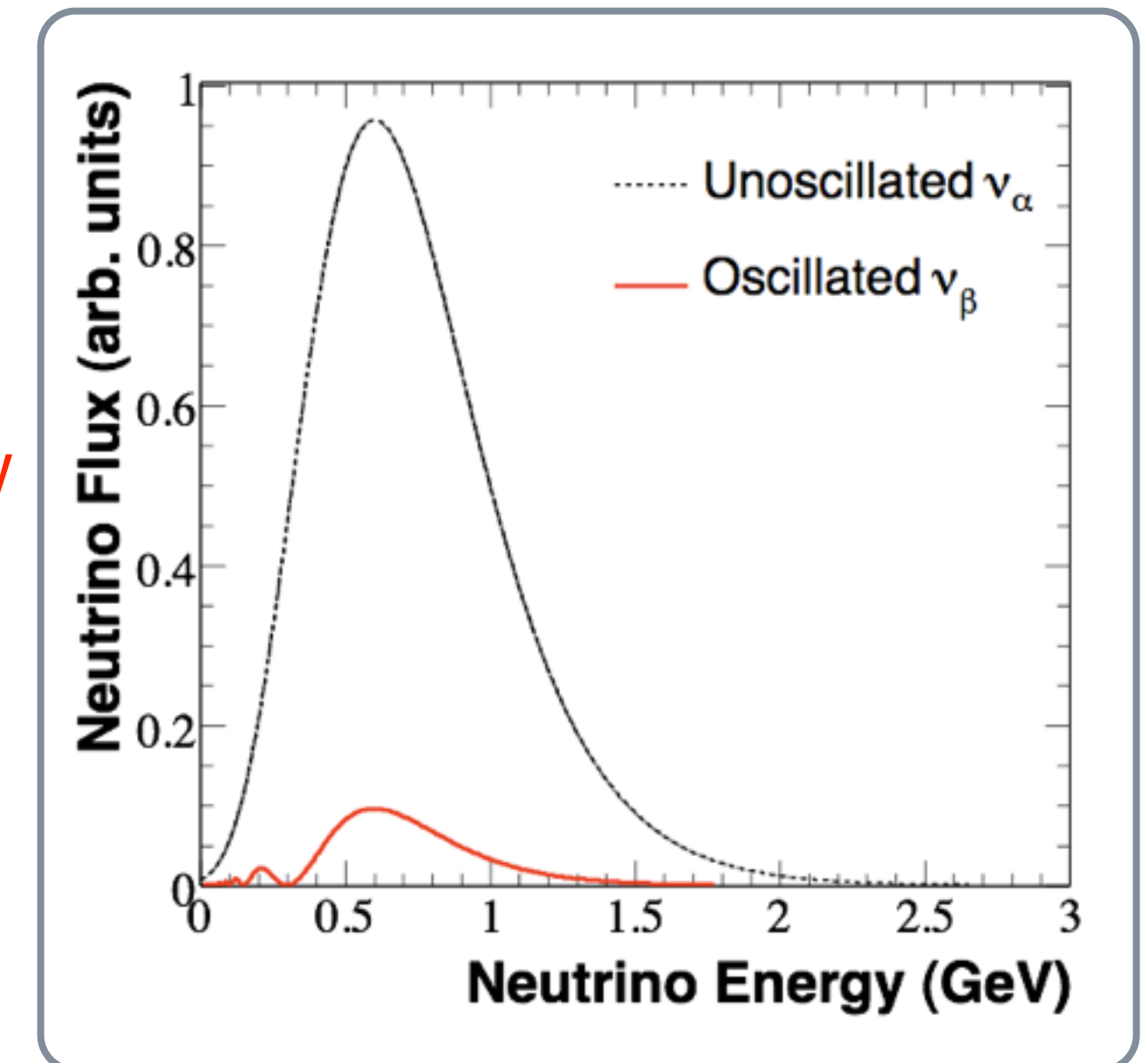
- Each mass/energy eigenstate evolves with a different frequency
- After some time, the flavour content changes

# NEUTRINO OSCILLATIONS

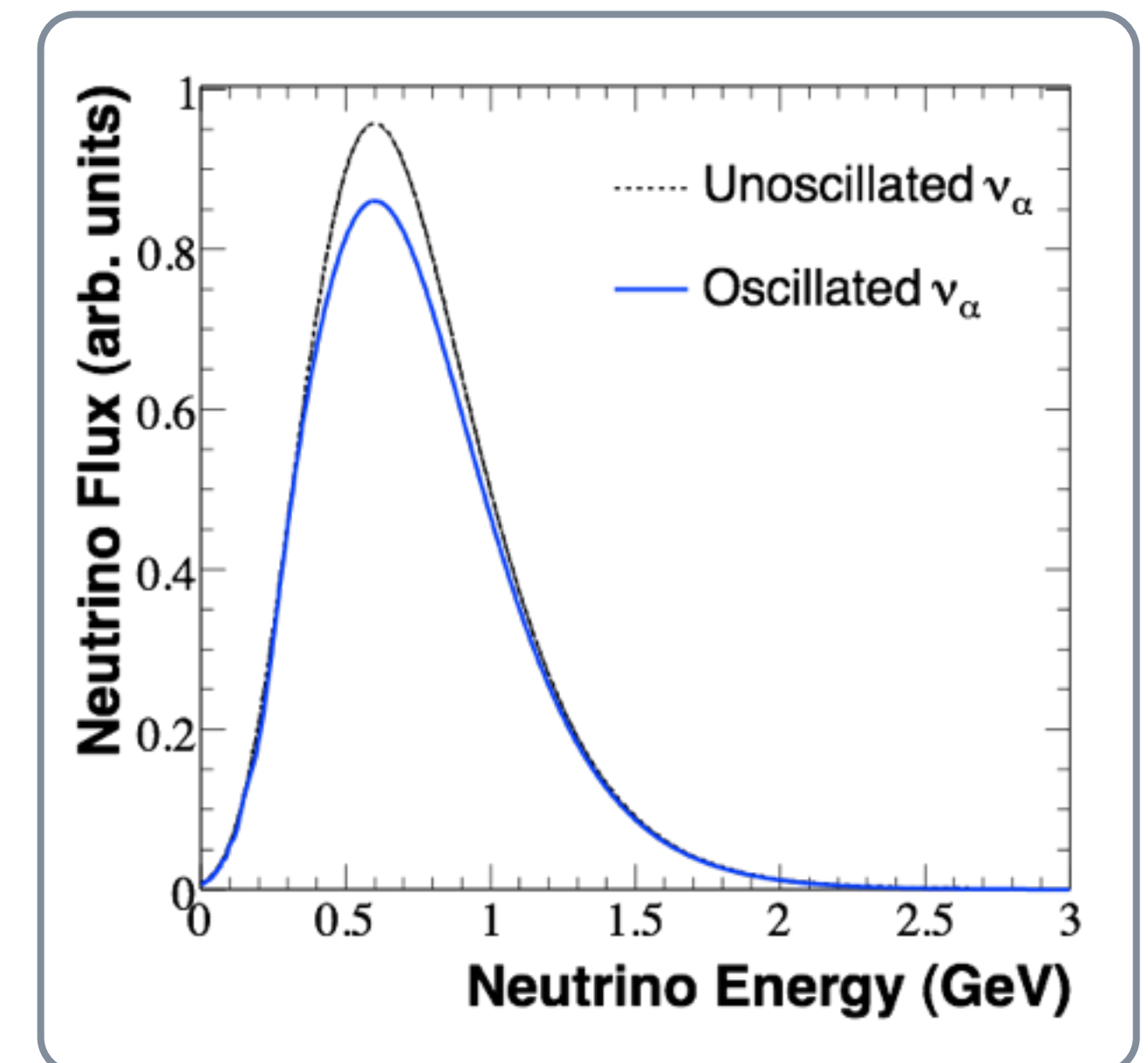
$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \times \sin^2 \left[ 1.27 \Delta m^2 \frac{L(\text{km})}{E(\text{GeV})} \right]$$



appearance of new flavor



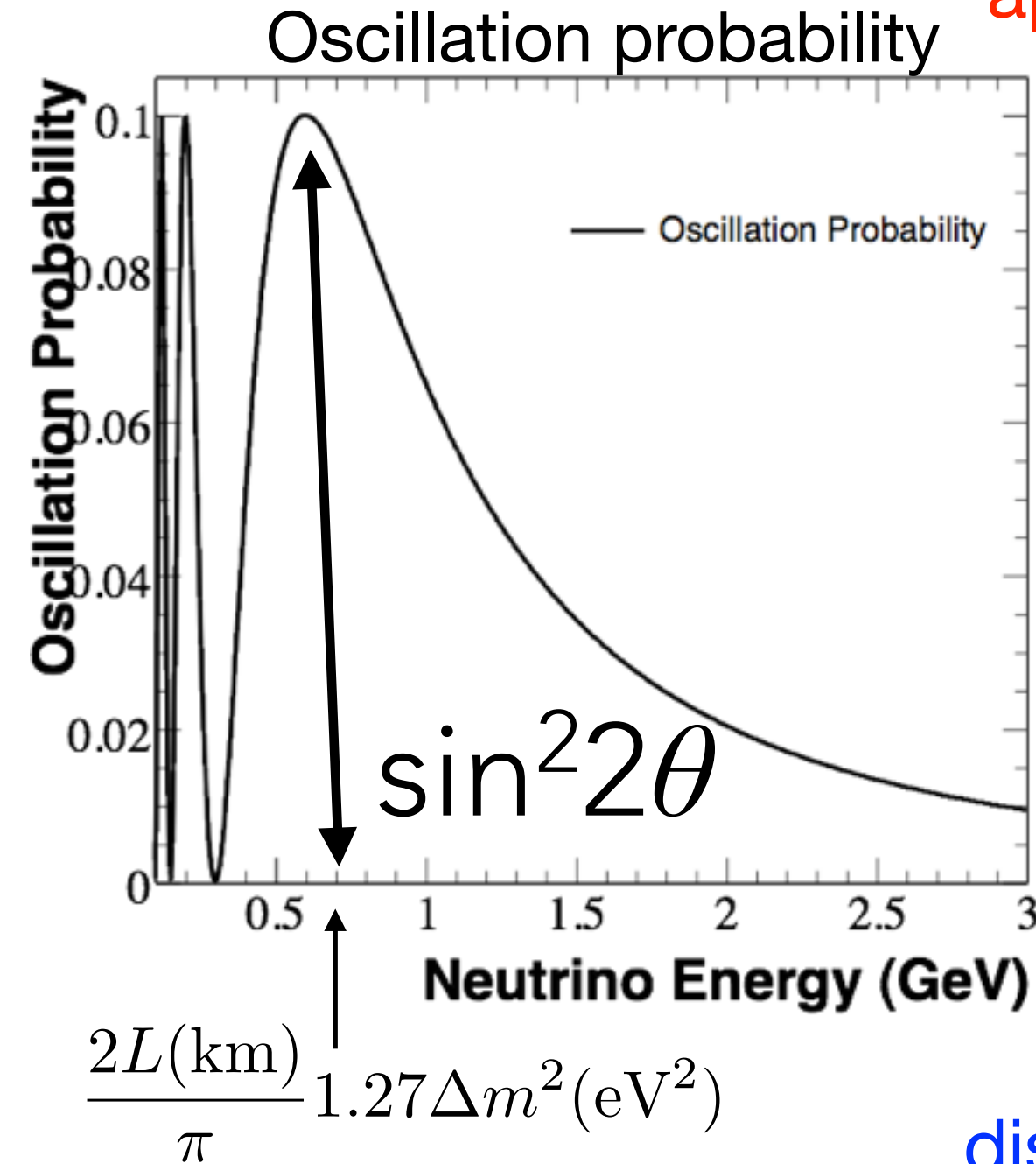
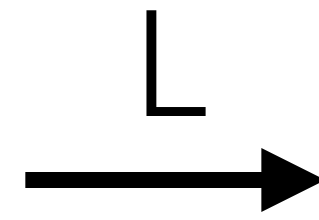
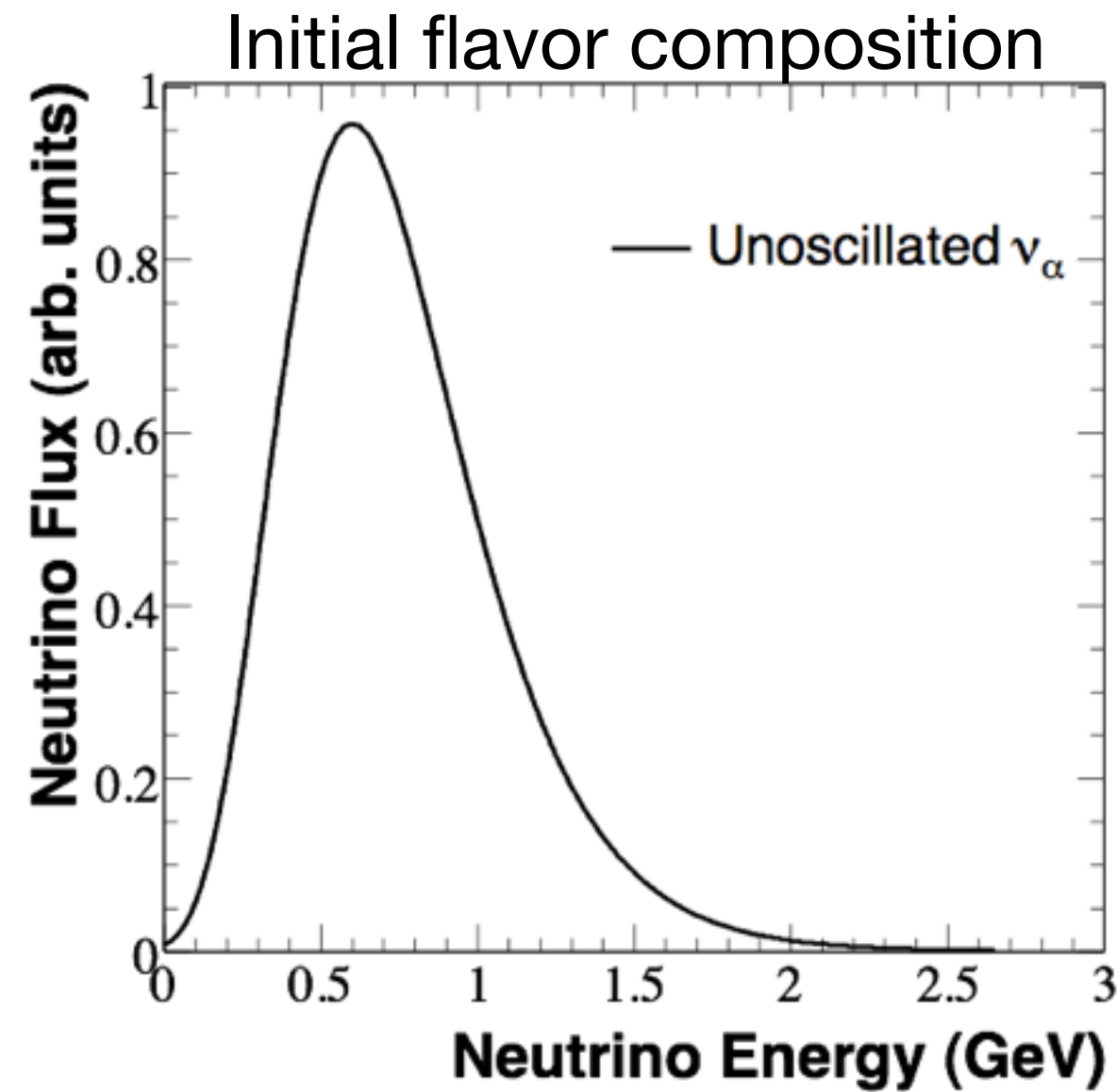
disappearance of initial flavor



- Typical experiment:
  - prepare a pure beam of  $\nu_\alpha$
  - neutrino oscillations then result in  $\nu_\alpha \rightarrow \nu_\beta$  transitions ( $\alpha \neq \beta$ )
- Two basic types of measurements
  - Deficit of  $\nu_\alpha$  relative to initial state
  - Appearance of  $\nu_\beta$  not present in initial state
- Both have definitive energy dependences

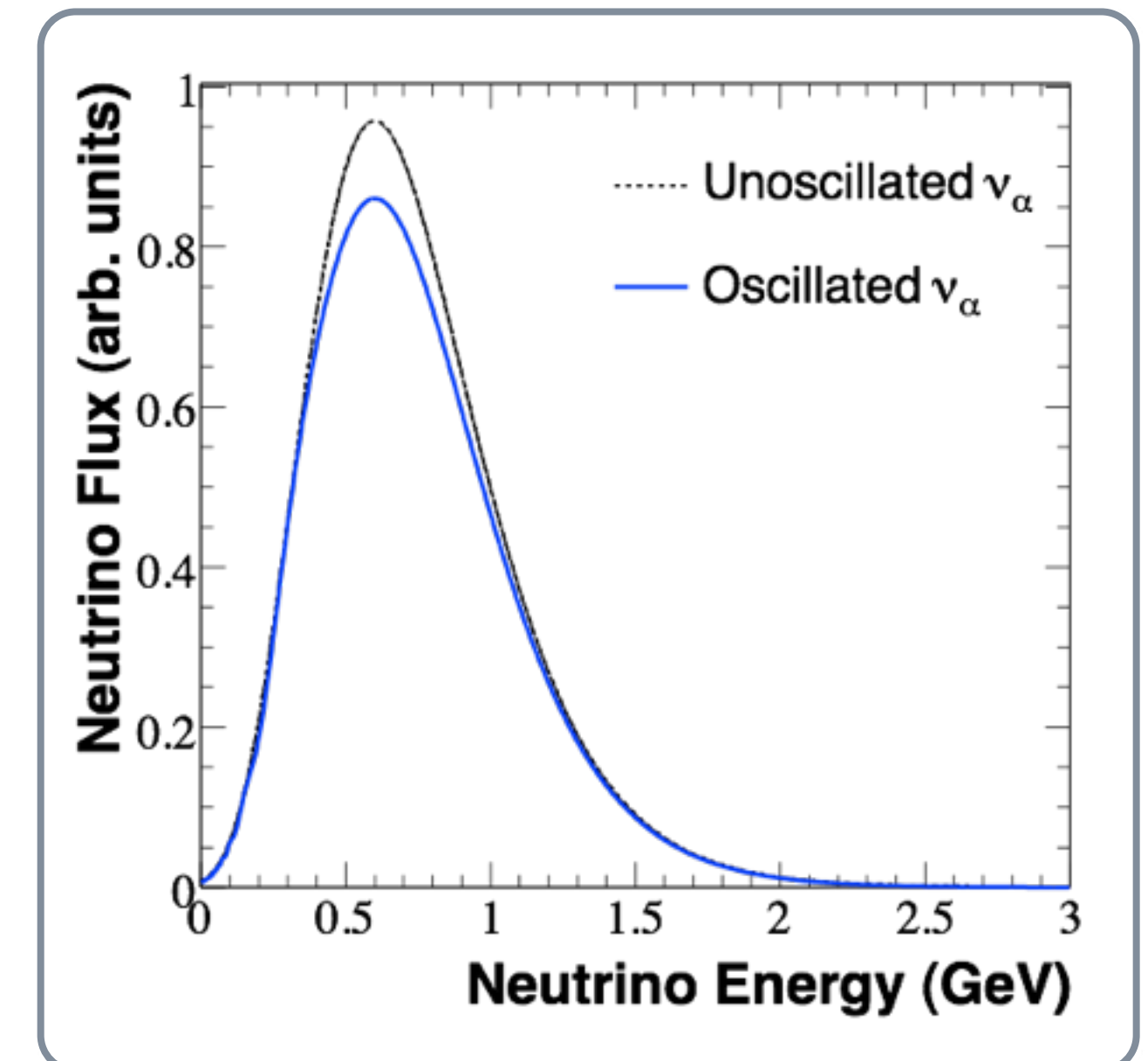
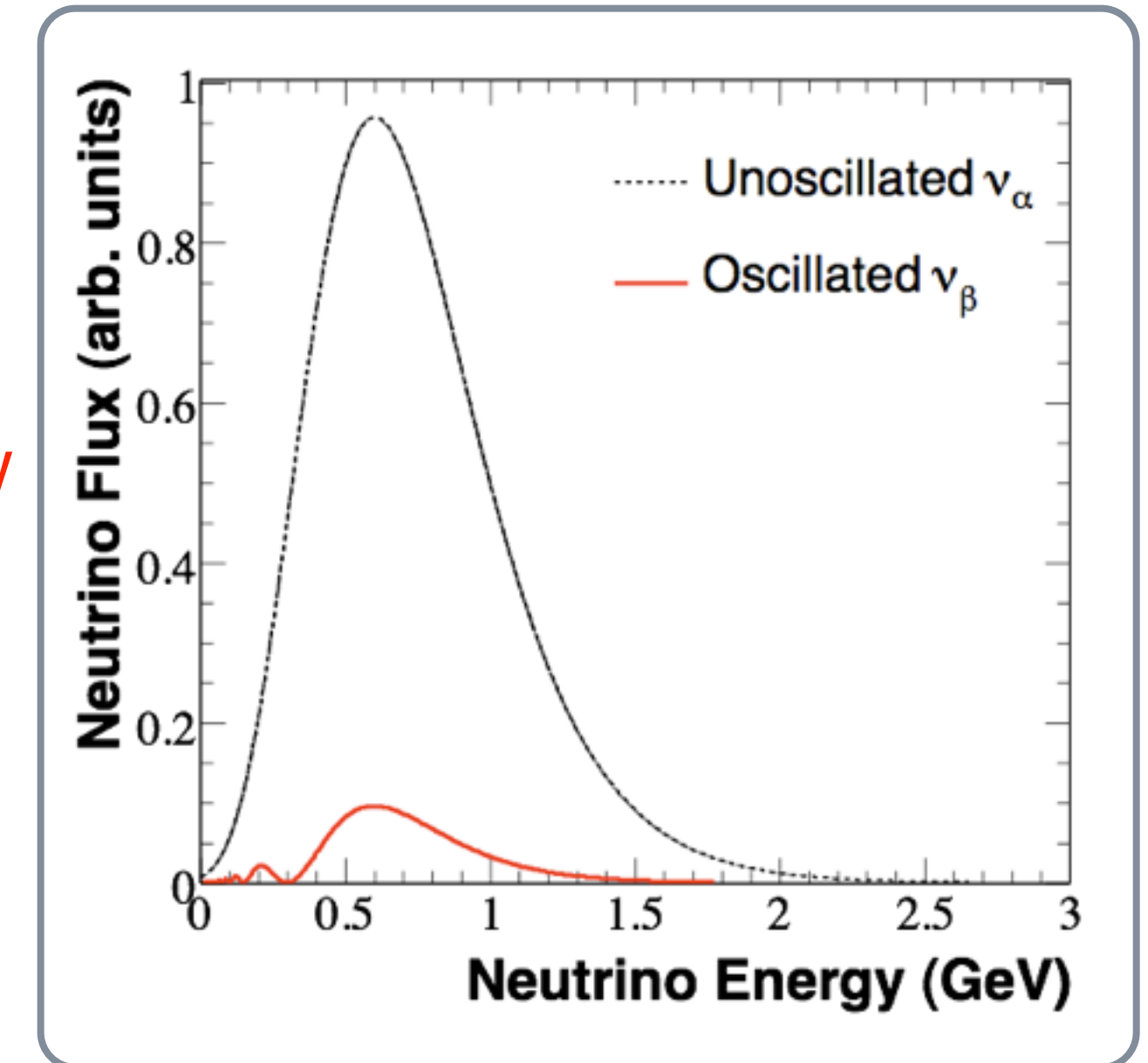
# NEUTRINO OSCILLATIONS

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \times \sin^2 \left[ 1.27 \Delta m^2 \frac{L(\text{km})}{E(\text{GeV})} \right]$$



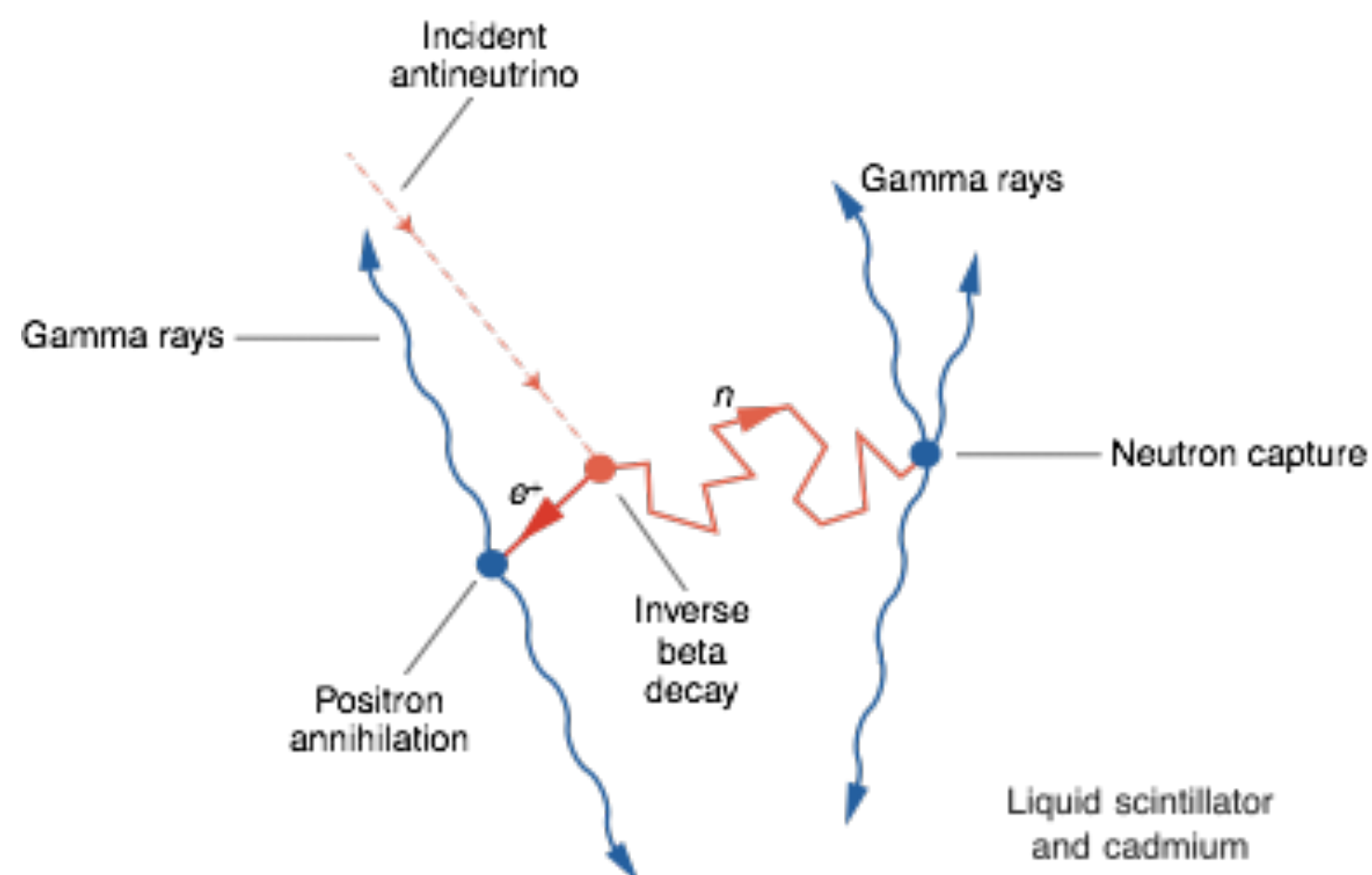
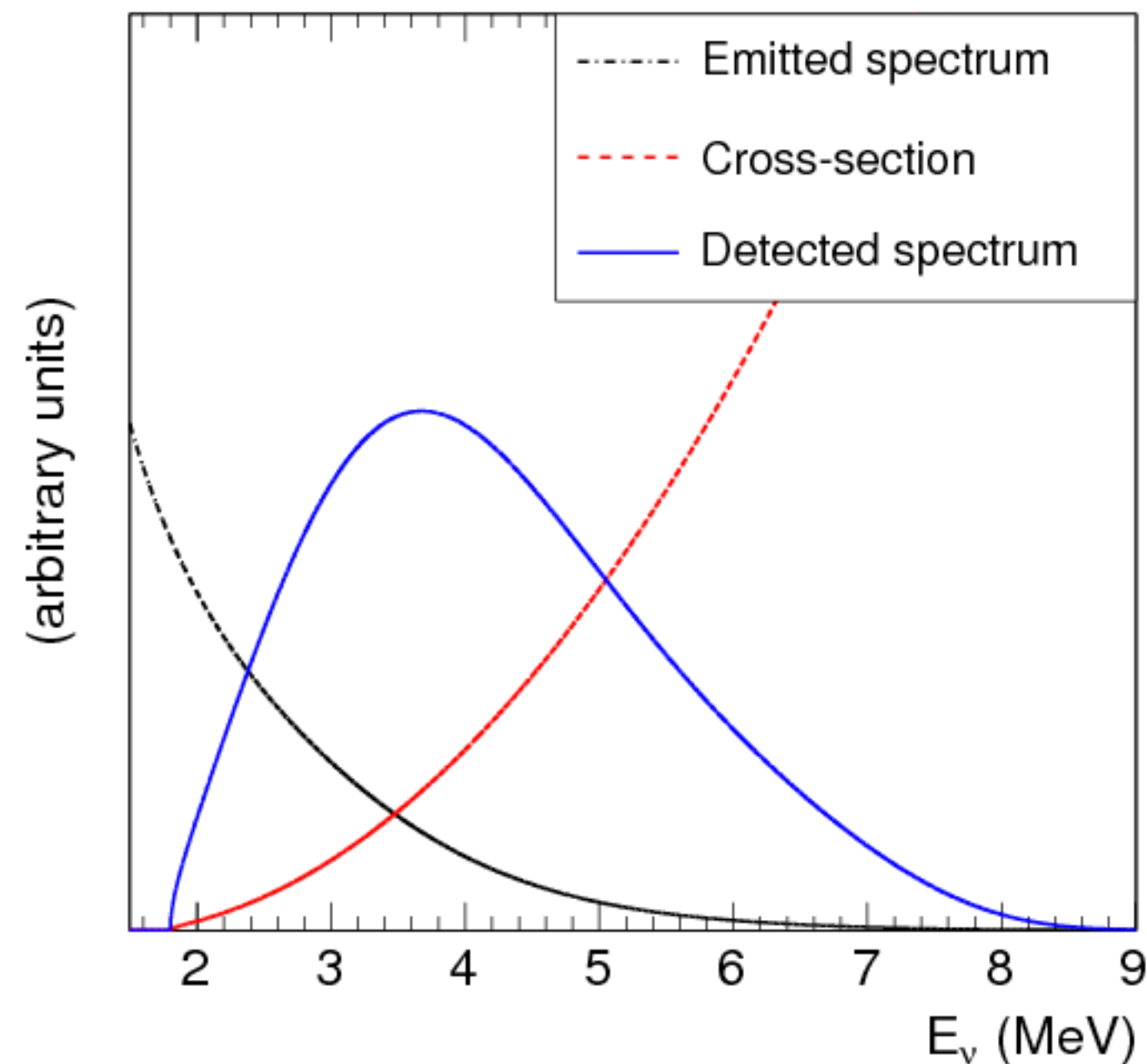
appearance of new flavor

disappearance of initial flavor

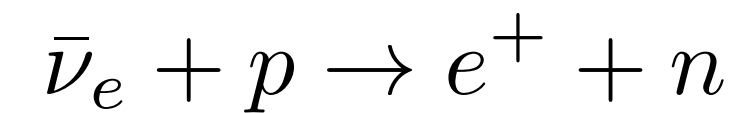


- Amplitude of appearance or disappearance gives  $\sin^2 2\theta$ 
  - or more generally the matrix elements ( $U_{ij}$ )
- Location of maximum in energy gives  $\Delta m^2$ , assuming  $L$  is fixed
- Essential to determine flavour and energy of neutrino

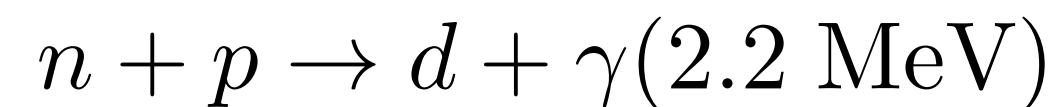
# REACTOR EXPERIMENTS



- detect antineutrinos using “inverse beta decay” process



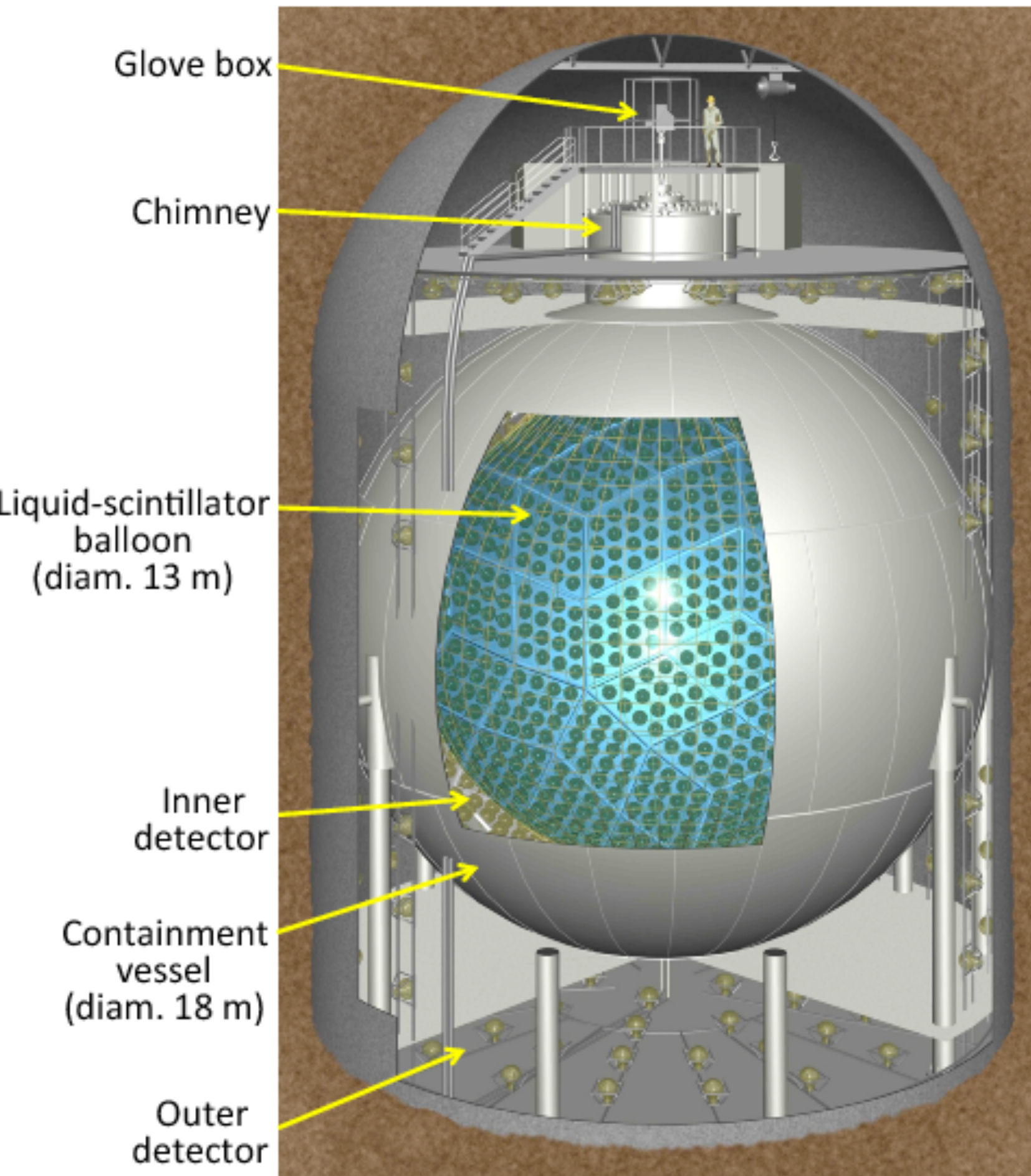
- two-step signature pioneered by Reines and Cowan
  - “prompt” signature from positron
  - “delayed” signature from neutron capture
- Due to low energies involved, large liquid scintillator detectors have been the preferred technology
  - large light yield from scintillation for good energy resolution
  - free protons allow neutron detection from capture process



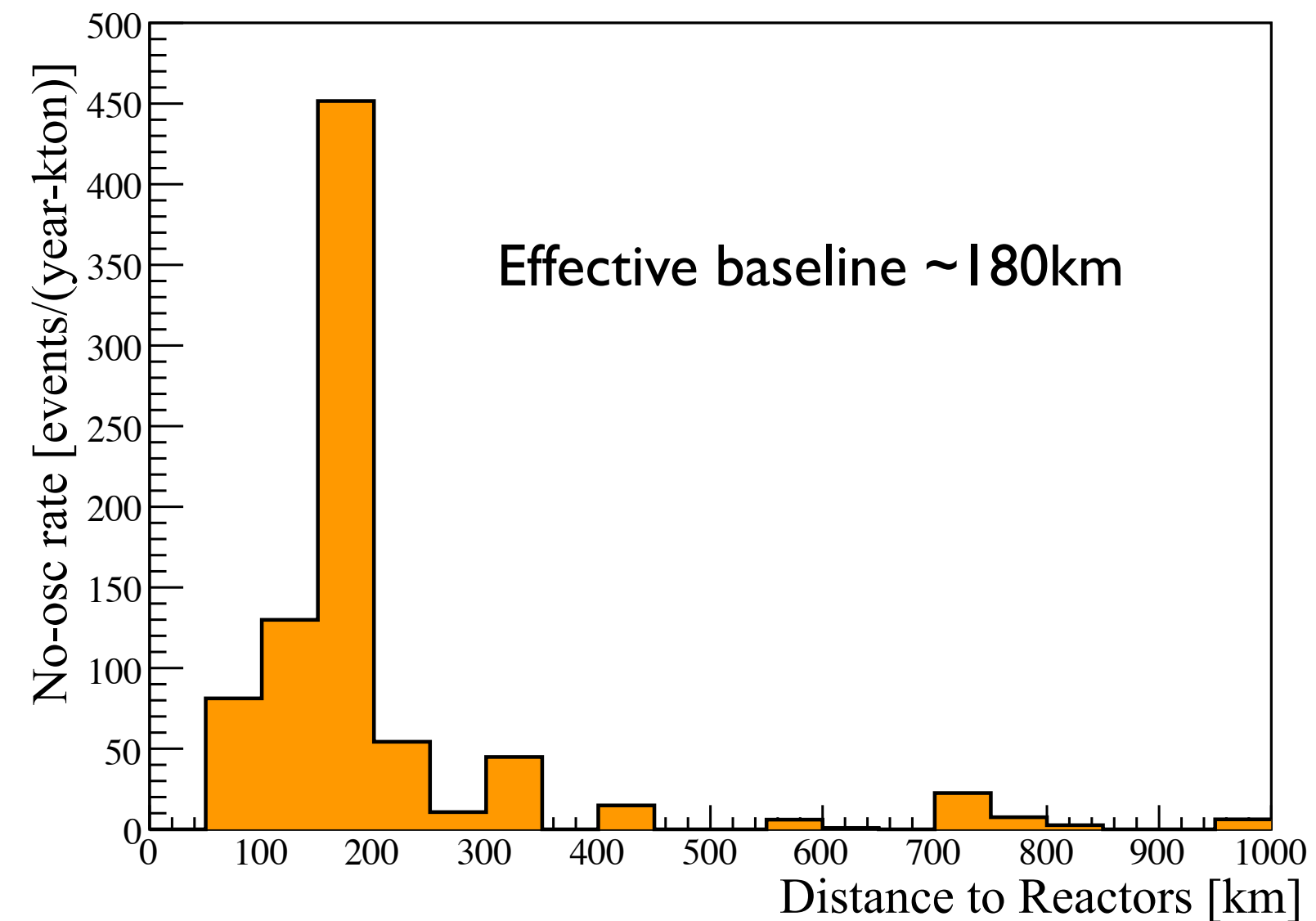
- photon detection can be enhanced by doping with other nuclei with high neutron capture cross section and photon energy emission
- antineutrino energy can be reconstructed as:

$$E_{\bar{\nu}} \sim E_e + \langle E_n \rangle + 0.8 \text{ MeV}$$

# KAMLAND



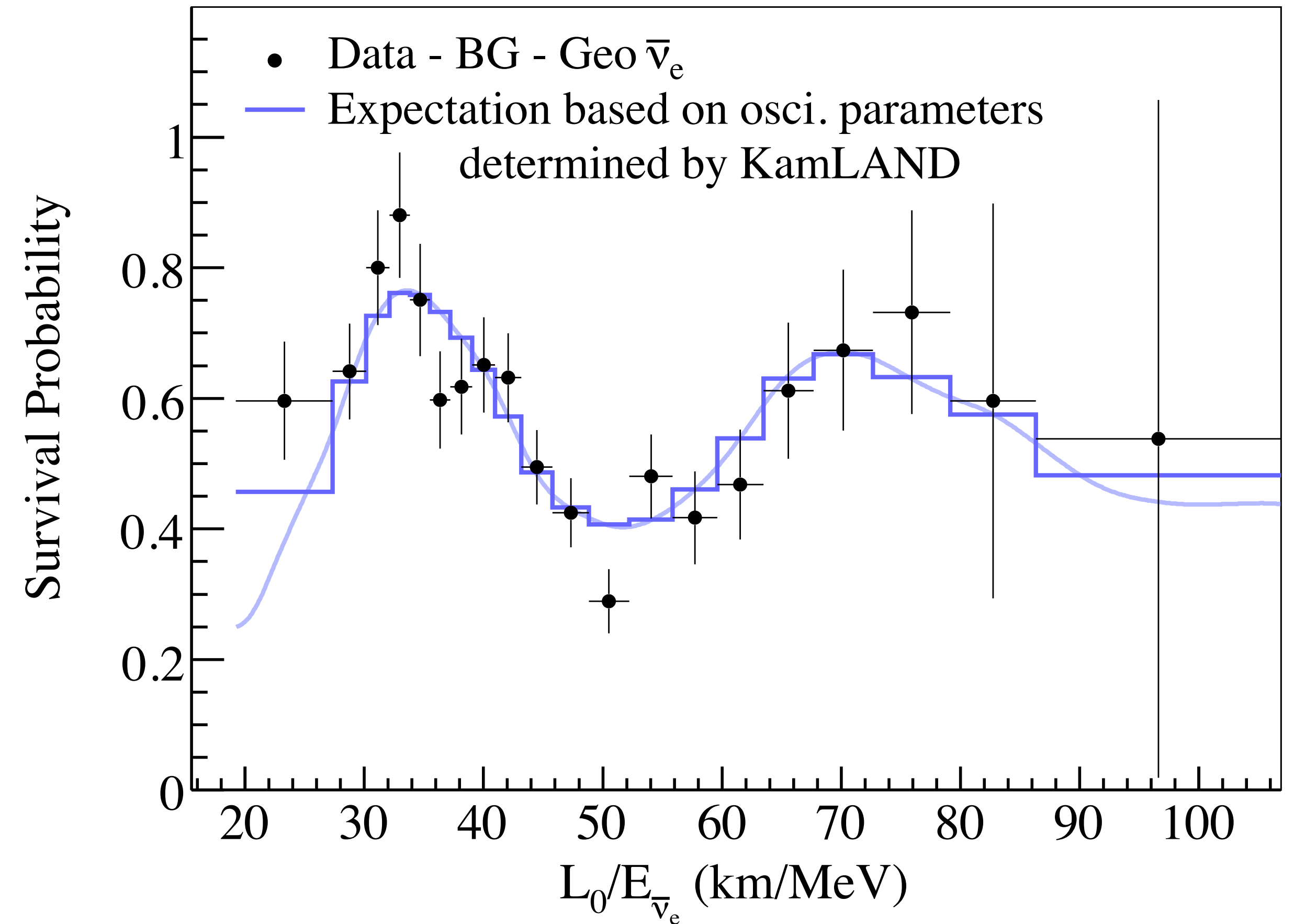
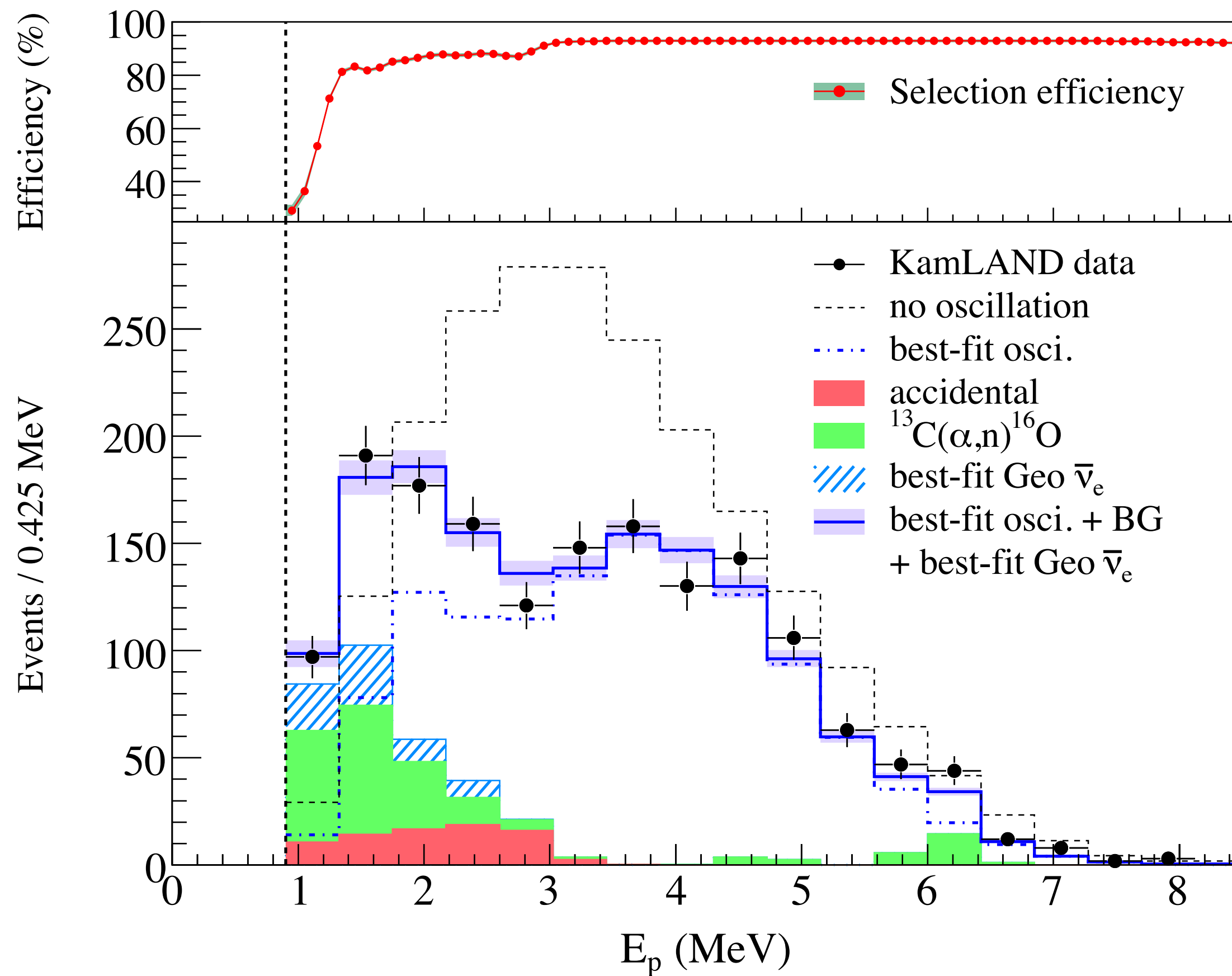
- Large liquid scintillator detector in the Kamioka mine (2002-2007)
  - 1 kT of liquid scintillator suspended in pure mineral oil
  - 1879 50 cm photomultiplier tubes to detect scintillation light
- detect antineutrinos from 55 nuclear reactors in Japan
  - 80% of antineutrinos produced by reactors between 130-220 km



- Known distances to reactors allow  $\bar{\nu}_e$  disappearance vs. L/E to be measured

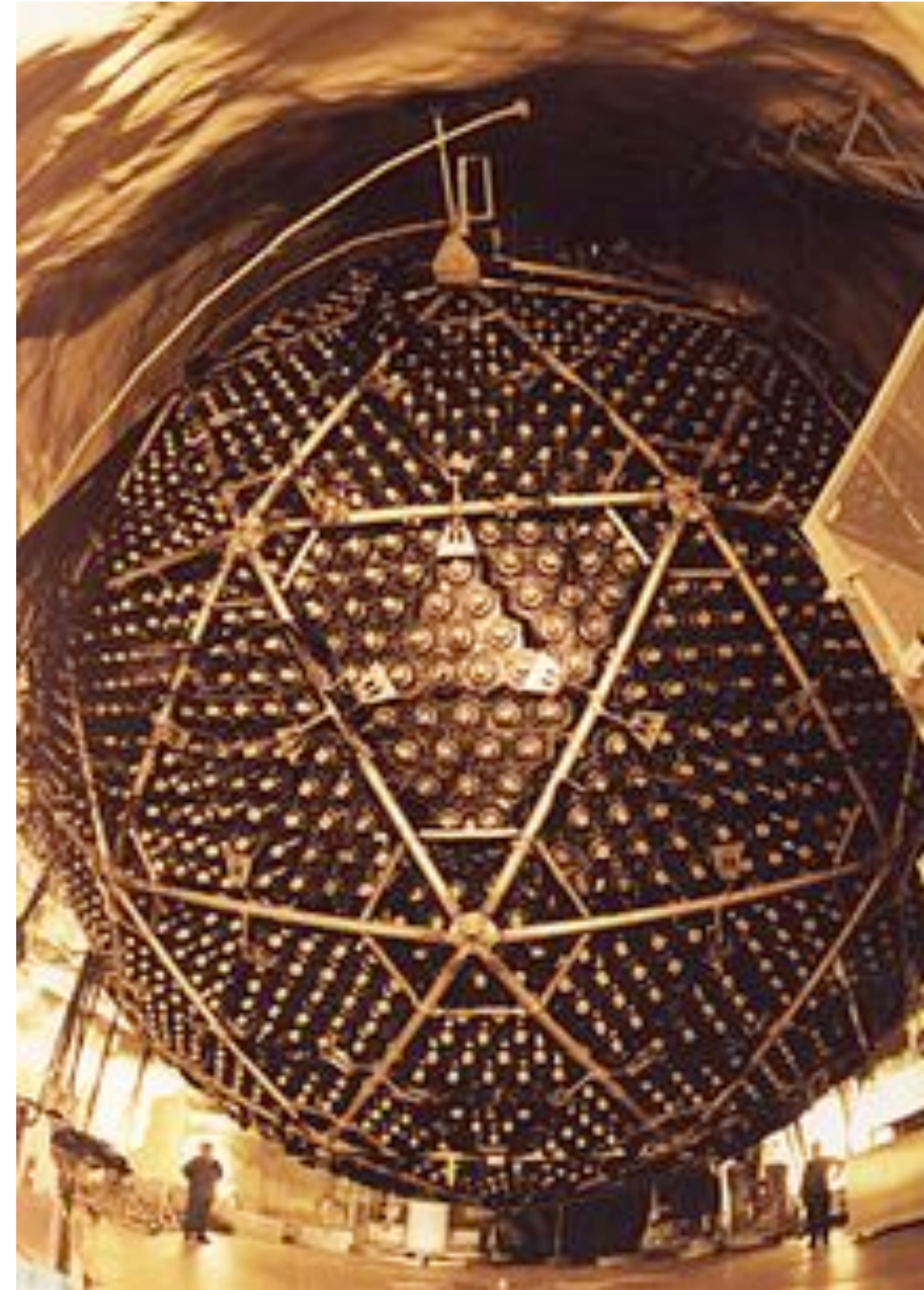
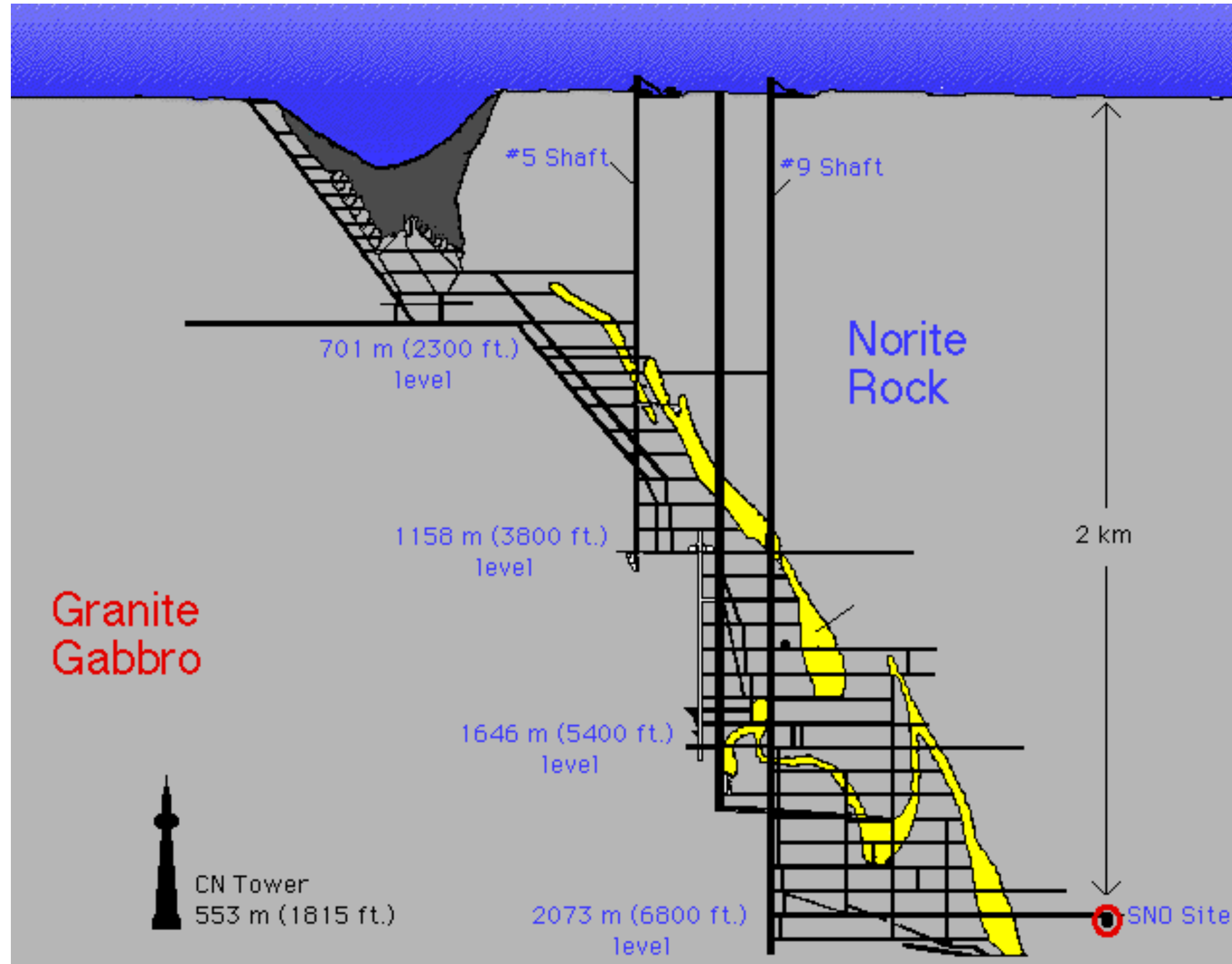
# RESULTS

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \times \sin^2 \left[ 1.27 \Delta m^2 \frac{L(\text{km})}{E(\text{GeV})} \right]$$



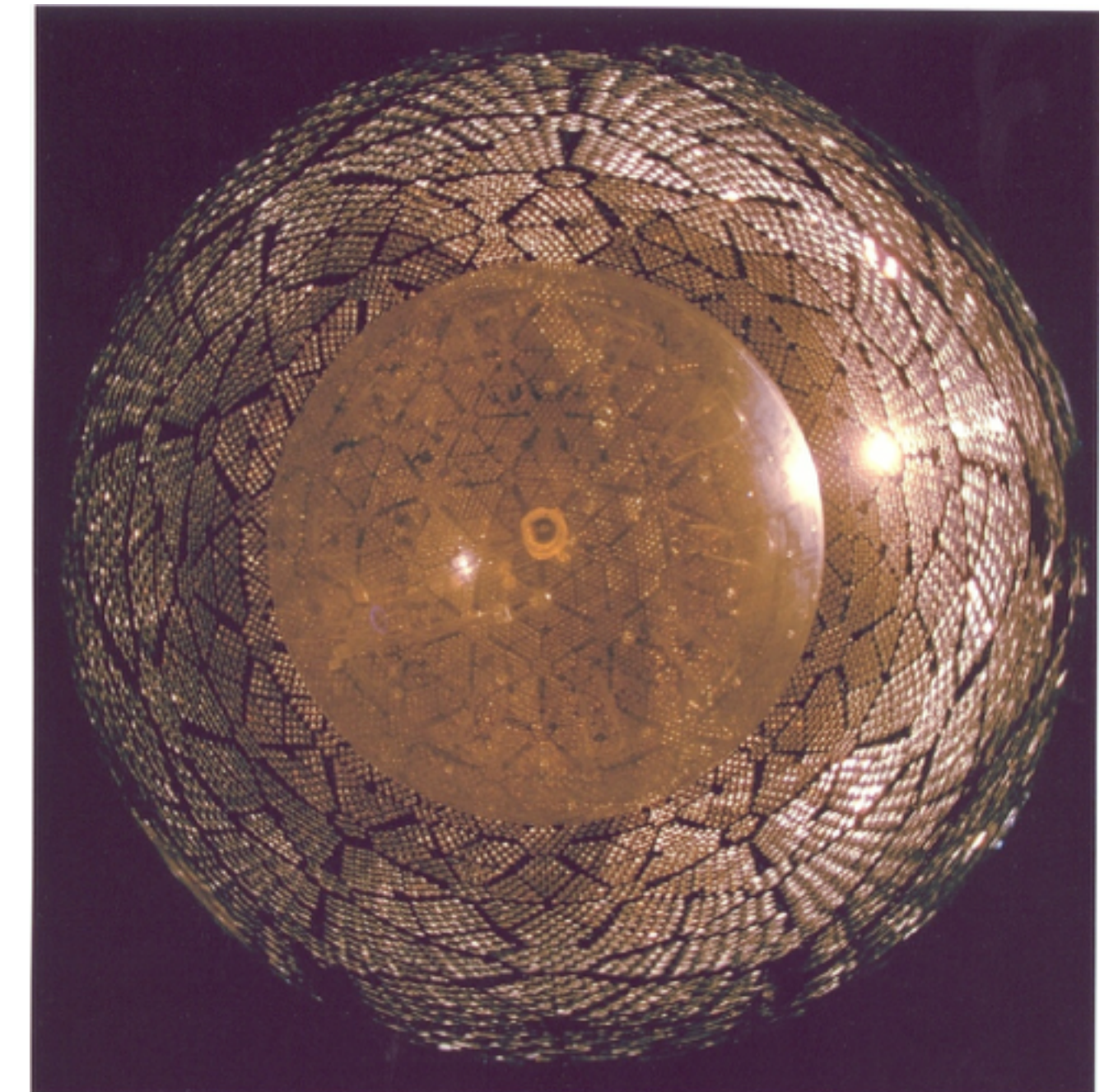
- Energy-dependent deficit of  $\bar{\nu}_e$  measured
- Plotting deficit (ratio to expectation without oscillations) versus  $L/E$  shows oscillation pattern
  - large amplitude:  $\sin^2 2\theta_{12} \sim 0.85$
  - 1st maximum of oscillation at  $L/E \sim 16000$  km/GeV: mass splitting of  $\Delta m^2_{21} \sim 7.5 \times 10^{-5} \text{ eV}^2$

# SNO

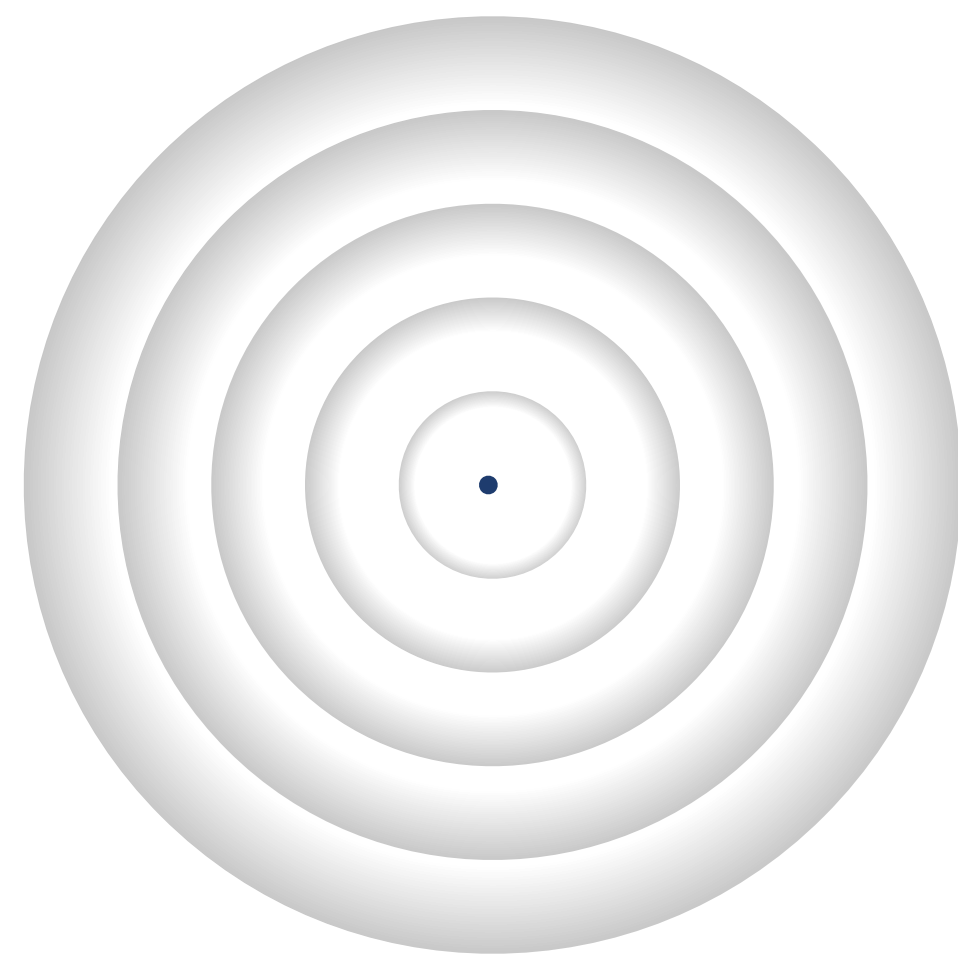


- Operated in three phases
  - "D2O"
  - "Salt"
  - "NCD"

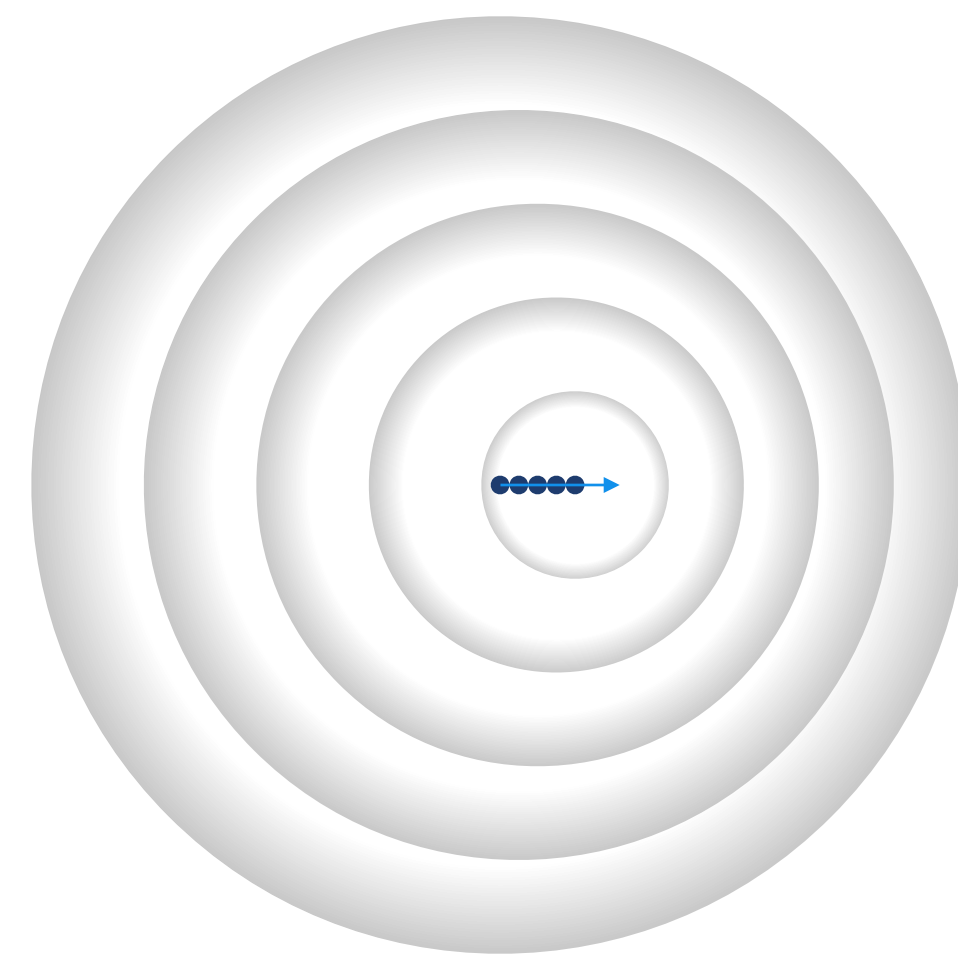
- Large (heavy) water Cherenkov detector 2 km underground in Sudbury, ON
  - "Sudbury Neutrino Observatory"
- 1 kton of heavy water ( $D_2O$ ) in an acrylic vessel suspended in light water ( $H_2O$ )
- viewed by 9456 20 cm photomultiplier tubes



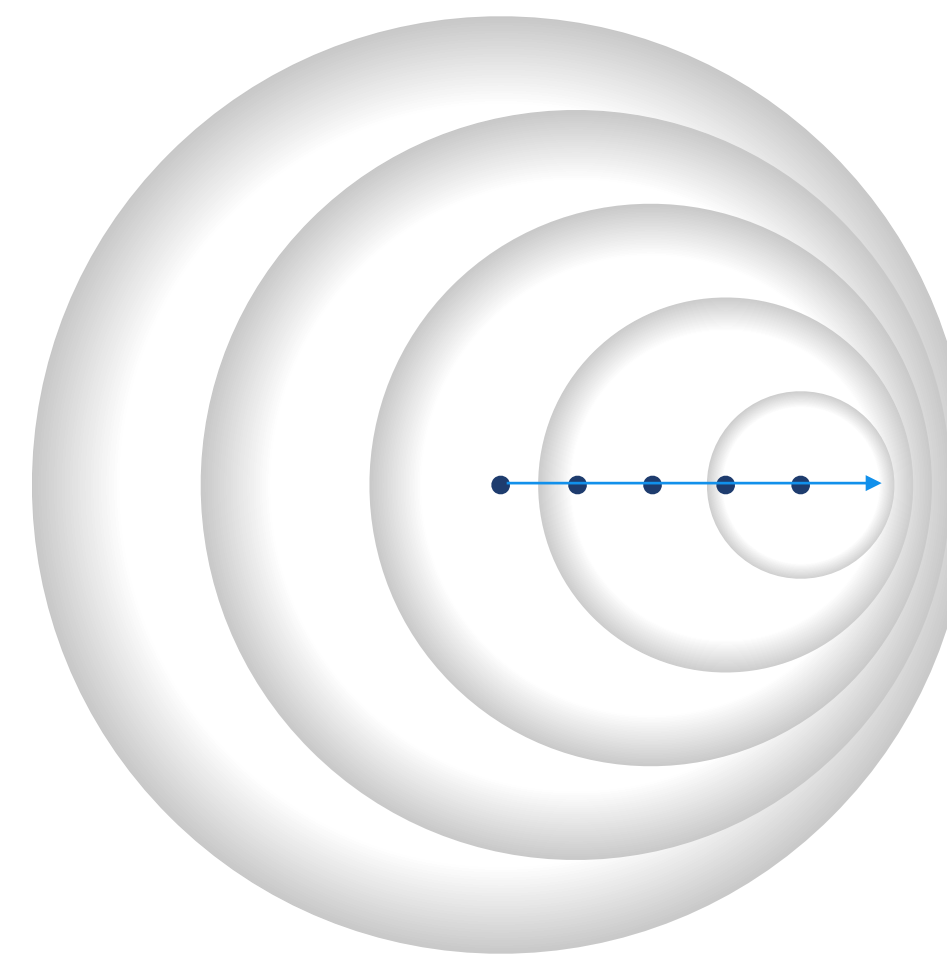
# CHERENKOV RADIATION



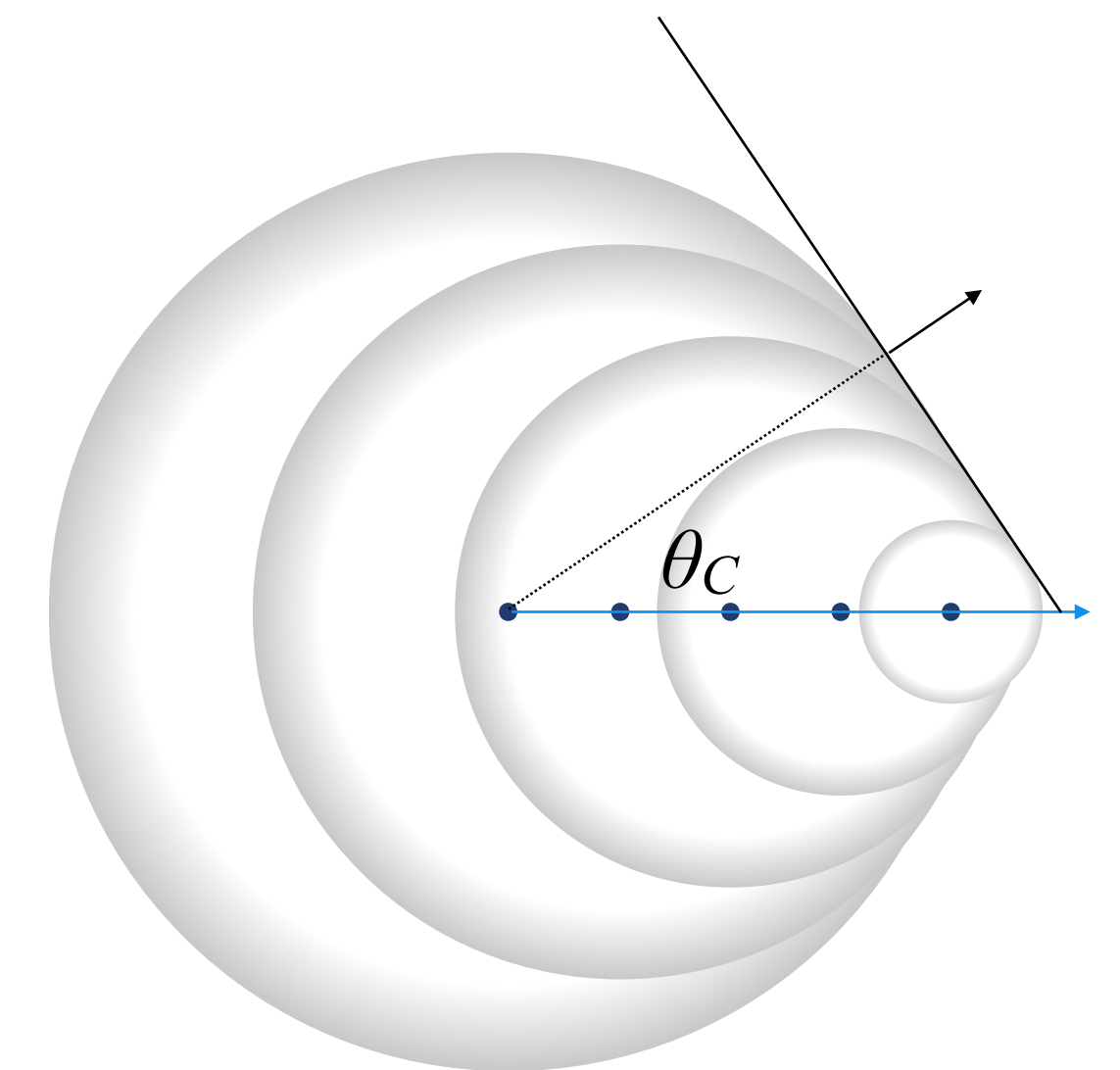
$$v=0 \times c_n$$



$$v=0.2 \times c_n$$



$$v=0.8 \times c_n$$



$$v=1.2 \times c_n$$

- Charged particle passing through a dielectric medium ( $n > 1$ ) induces a EM disturbance that propagates at speed  $c_n=c/n$
- If  $v > c_n$ , the disturbance piles up
  - electromagnetic "shock wave" emitted with angle  $\theta_C$

$$\cos \theta_C = \frac{c}{nv} = \frac{1}{n\beta}$$

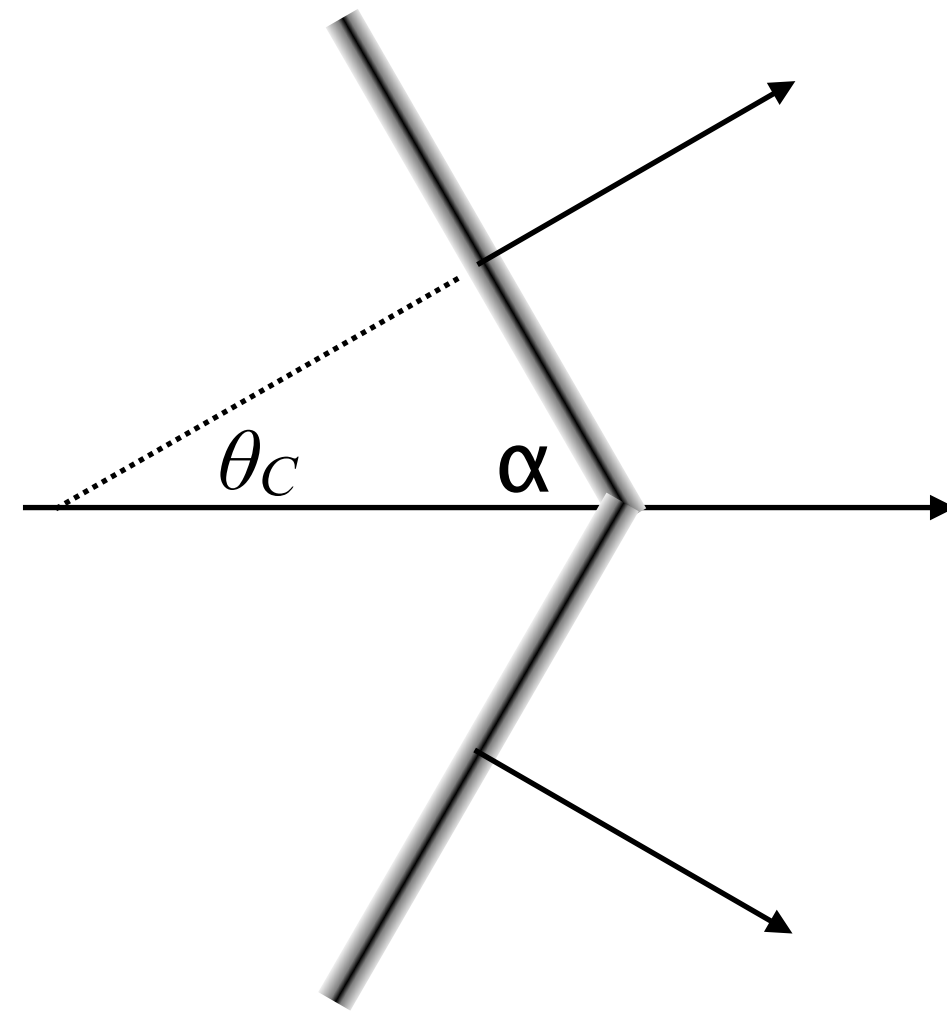
- This is Cherenkov (Č) radiation



# SONIC ANALOGY

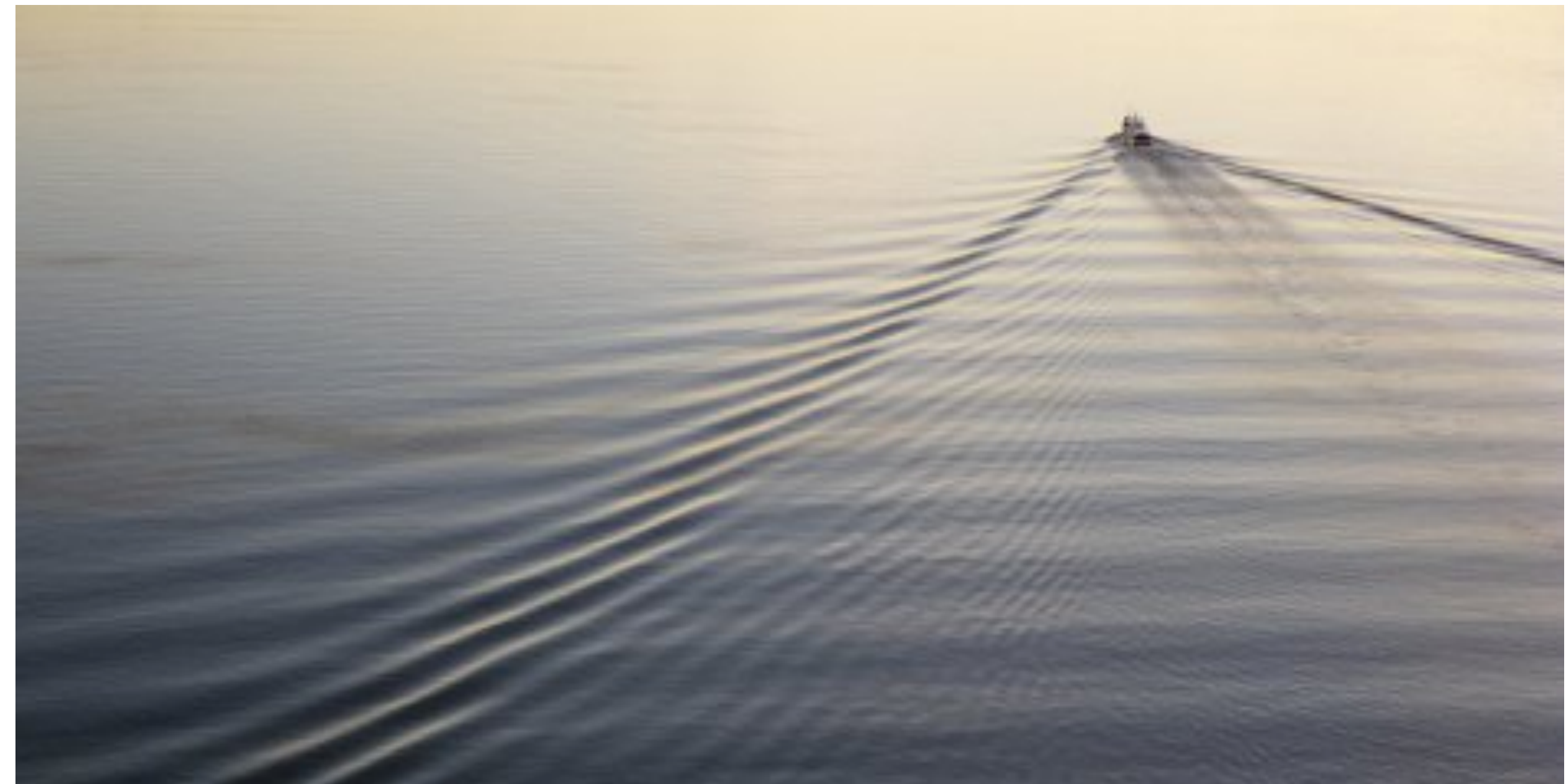
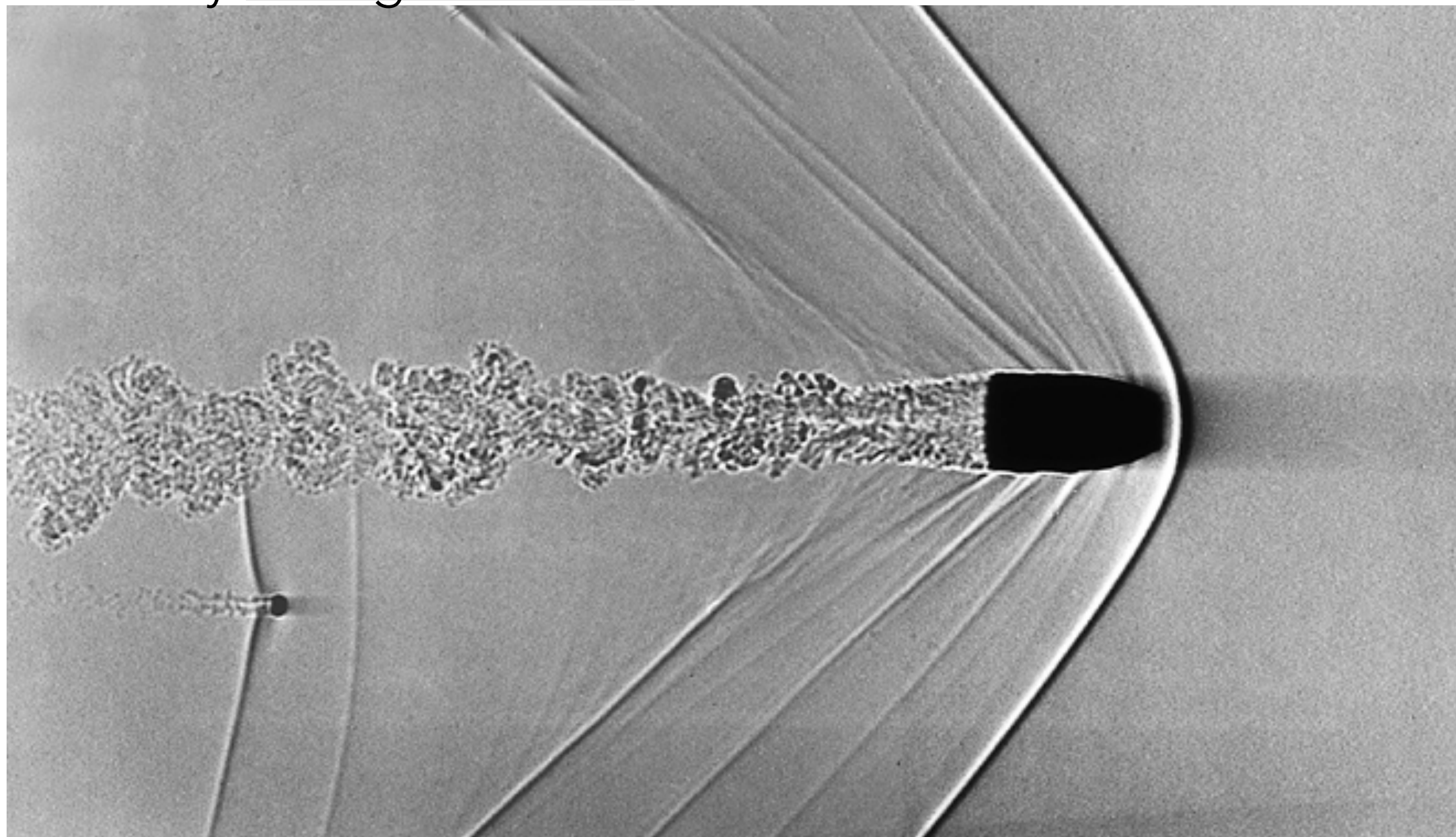


courtesy [findagrave.com](http://findagrave.com)



- Analogous to other (mechanical) systems where a disturbance exceeds the propagation velocity
- e.g. "sonic boom" from supersonic object

$$\sin \alpha = \frac{v_s}{v} \quad \alpha = \frac{\pi}{2} - \theta_C$$



# PROPERTIES OF CHERENKOV RADIATION

- Considerations of “spatial singularity”:

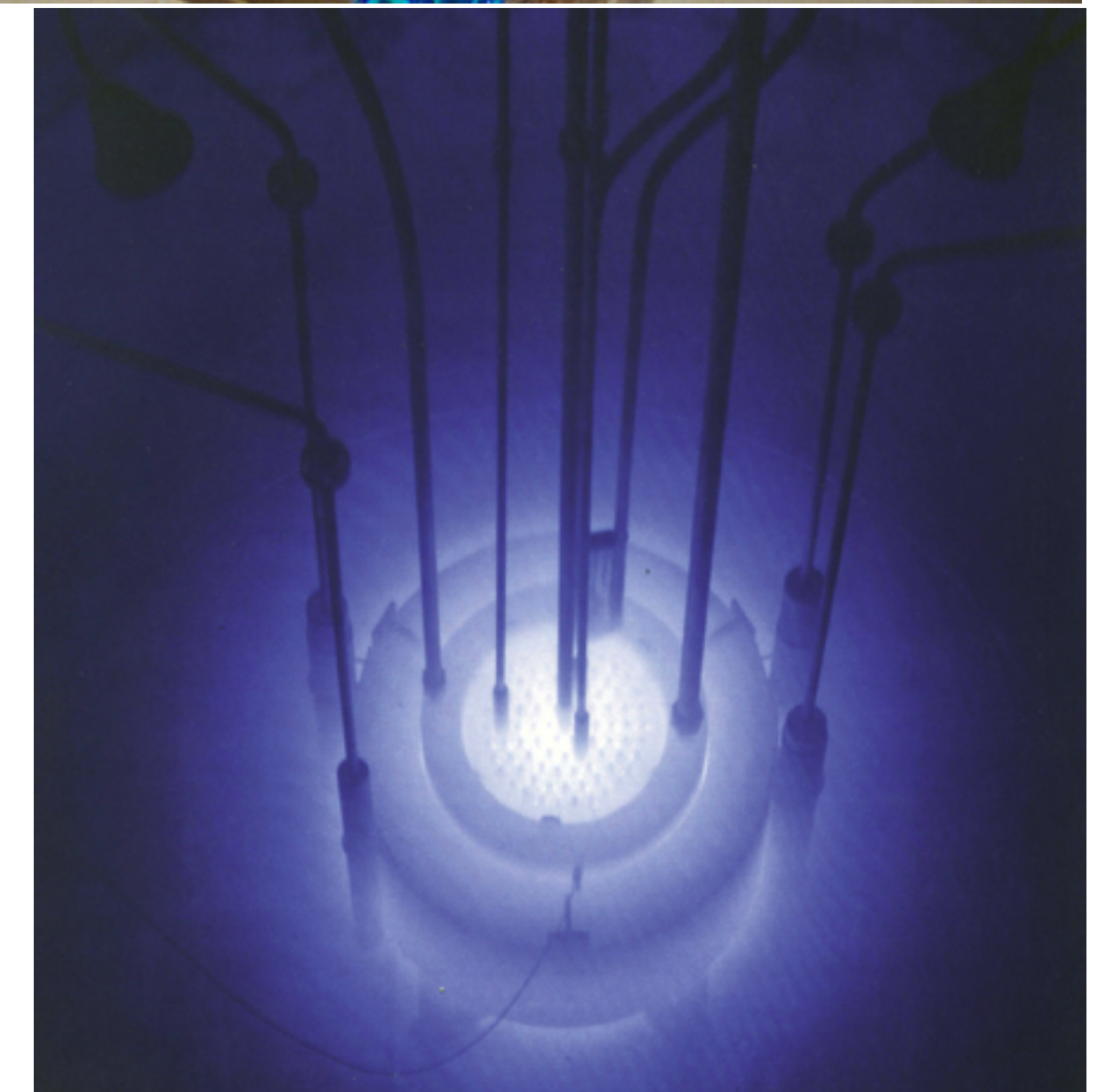
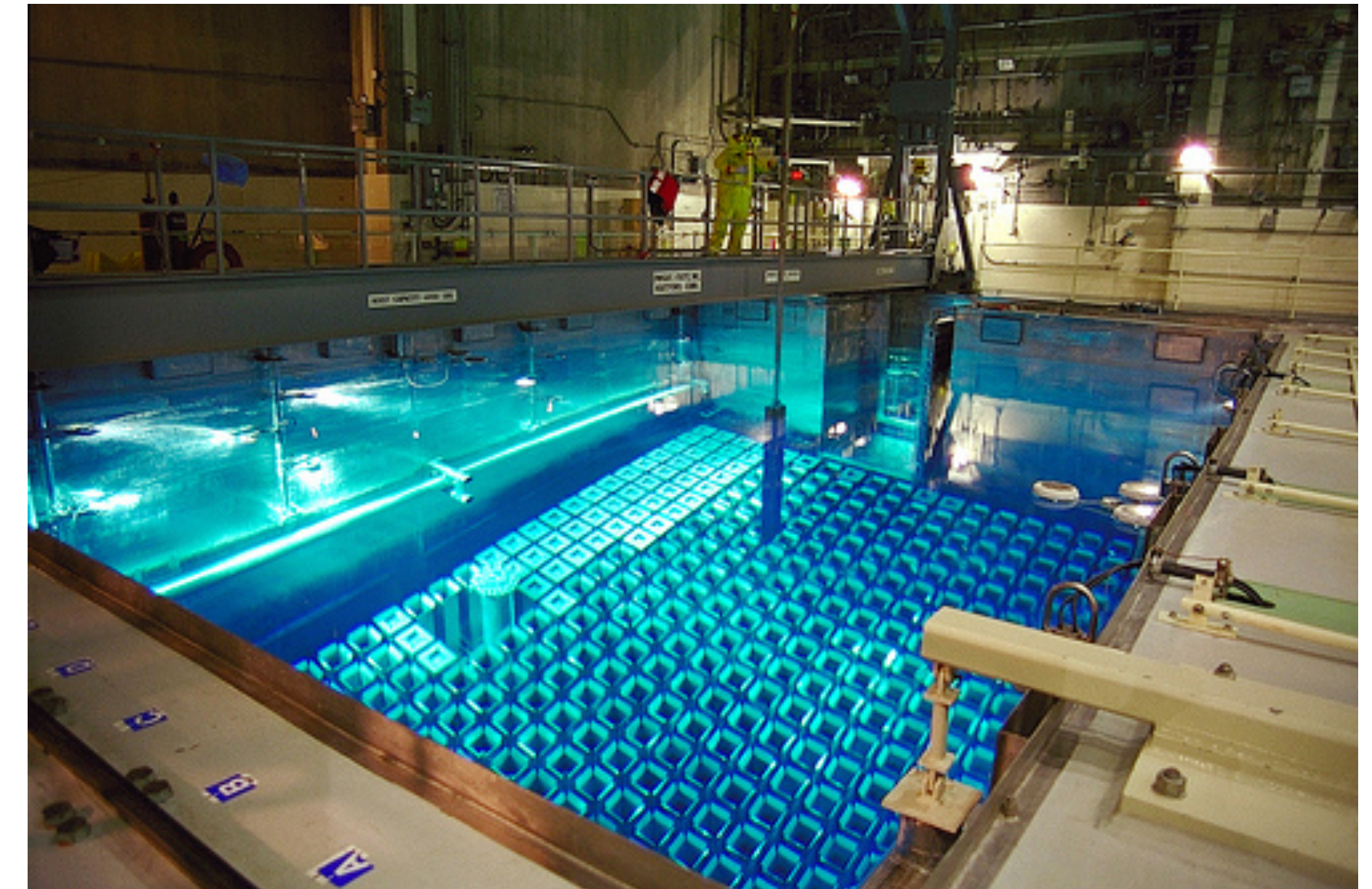
- $k$  = wavenumber, so that  $p = \hbar k$
- expect light to be emitted “flat” in  $k$

$$k = \frac{2\pi}{\lambda} \quad dk = -\frac{2\pi}{\lambda^2} d\lambda$$

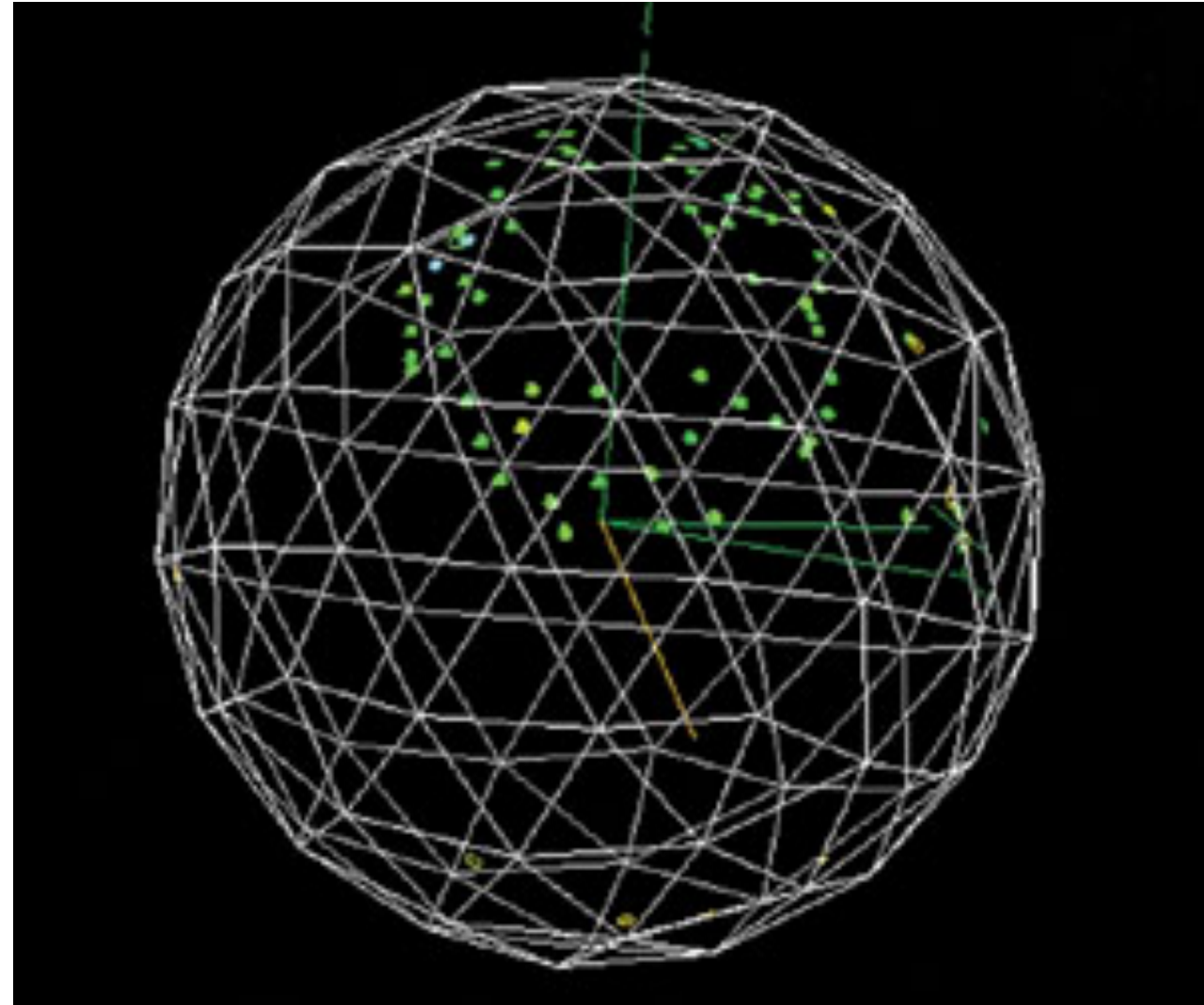
- wavelength spectrum is  $1/\lambda^2$
- Frank-Tamm Equation

$$\frac{d^2 N}{dE dx} = \frac{\alpha z^2}{\hbar c} \sin^2 \theta_C \sim 370 \sin^2 \theta_C \text{ eV}^{-1} \text{ cm}^{-1}$$

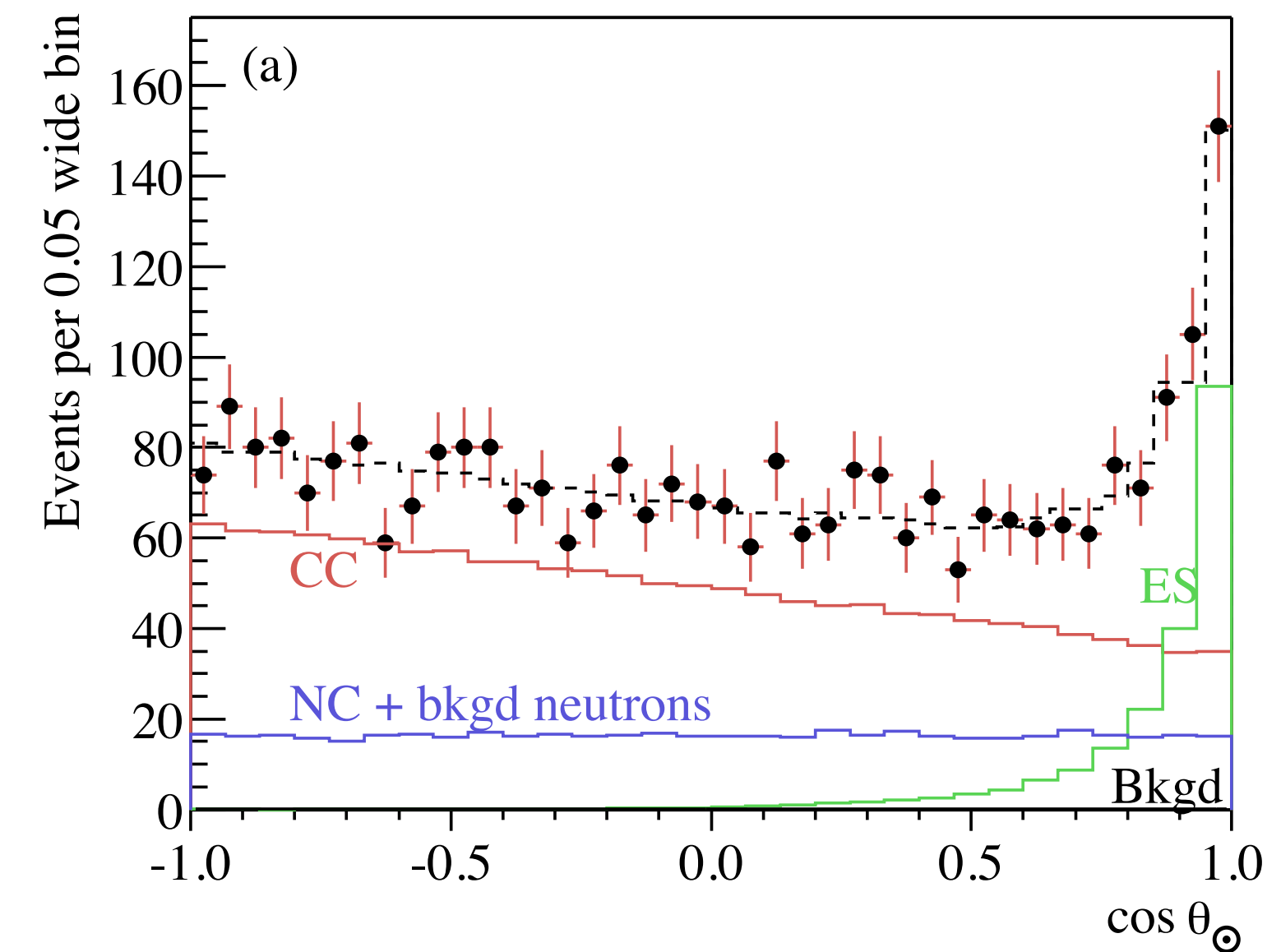
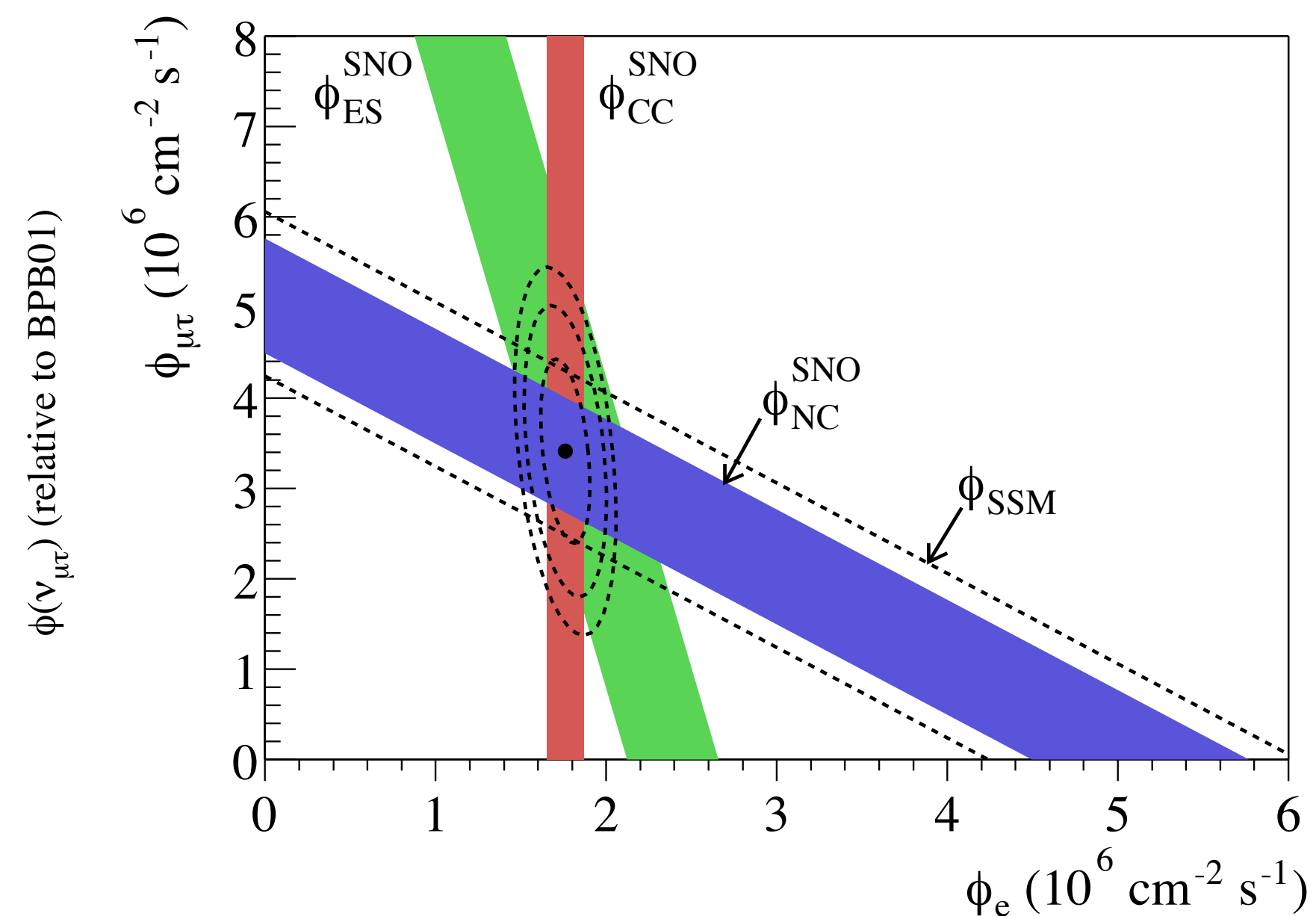
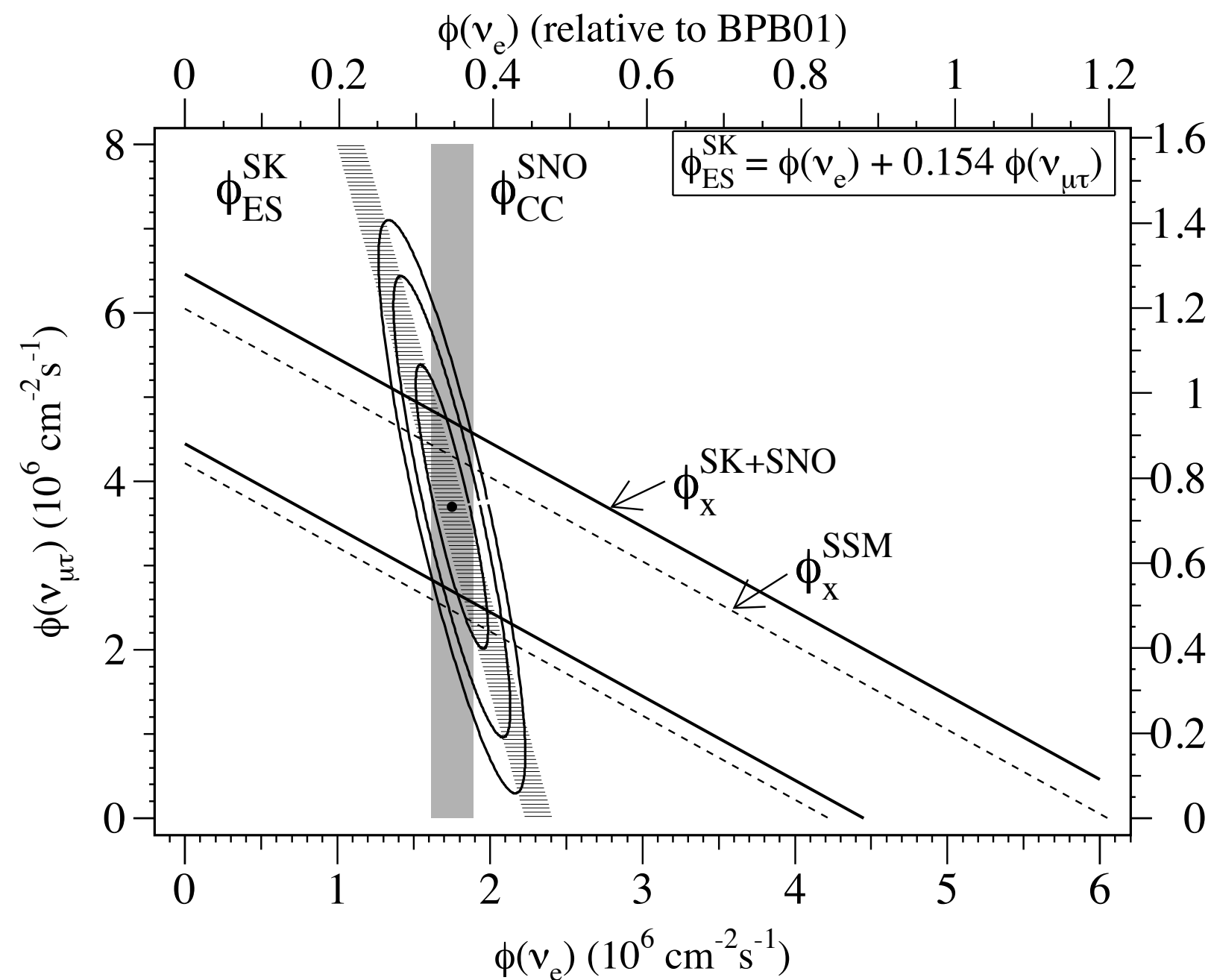
- For water,  $n \sim 1.34$ ,  $\sin^2 \theta_C = 0.44$ 
  - “~160 photons/cm for  $\beta=1$  particle in 1 eV interval of photon energy”
  - ~250 photons emitted/cm in the visible light region
  - “Collapse” of Č cone: as  $v \sim c_n$  (threshold),  $\theta_C$  and  $\sin^2 \theta_C$  goes to zero



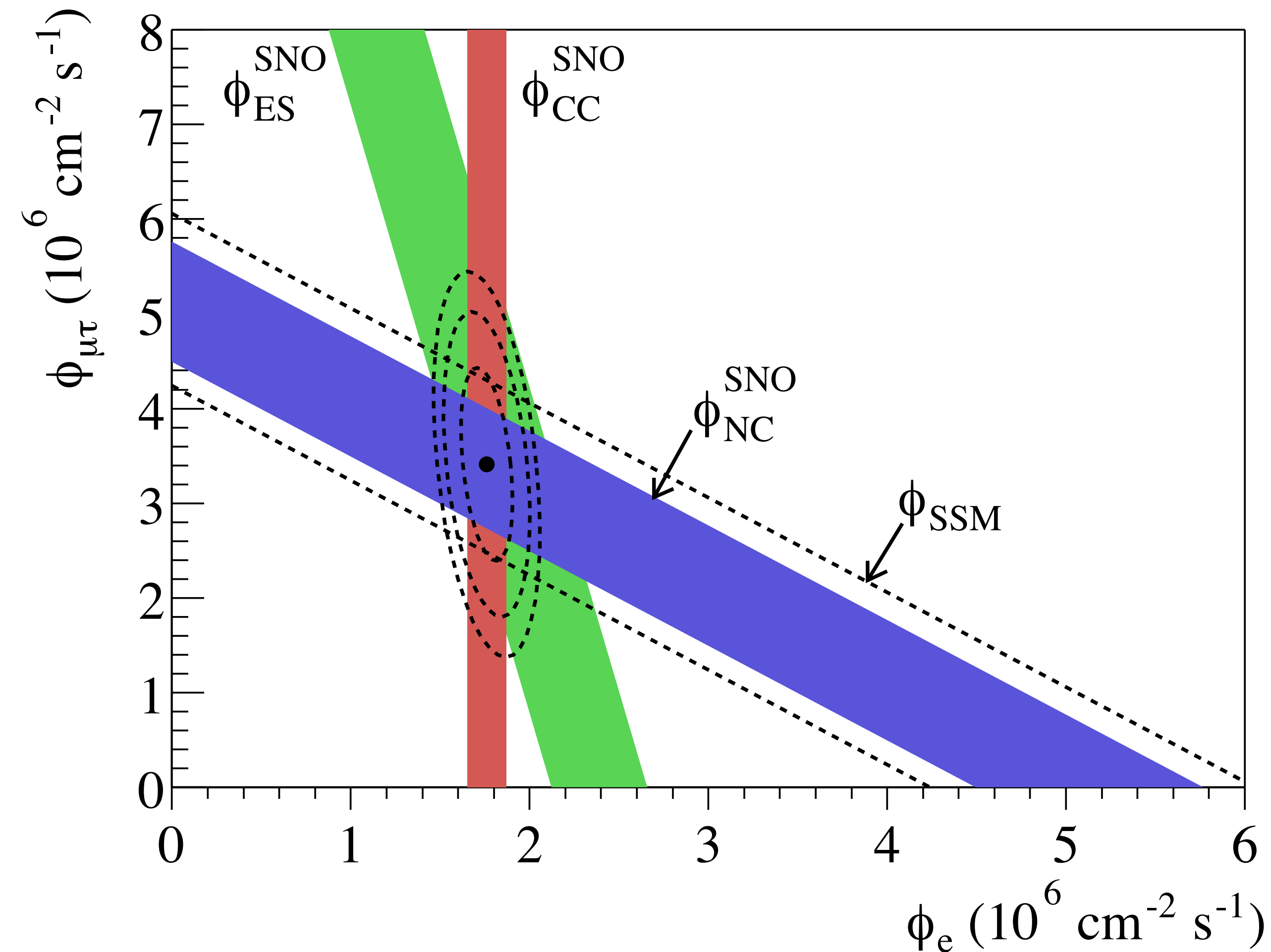
# NEUTRINO INTERACTIONS AT SNO



- Three channels observed:
- "CC":  $\nu_e + d \rightarrow e^- + p + p$ 
  - sensitive only to  $\nu_e$  from the sun
- "NC":  $\nu_x + d \rightarrow \nu_x + n + p$  ( $n + d \rightarrow t + \gamma(6.25 \text{ MeV})$ )
  - equally sensitive to all neutrino flavours ( $\nu_e, \nu_\mu, \nu_\tau$ )
- "ES":  $\nu_x + e^- \rightarrow \nu_x + e^-$ 
  - interactions in all neutrino flavors, but higher for  $\nu_e$  ( $\sigma(\nu_e) \sim 6.5 \times \sigma(\nu_\mu)$  or  $\sigma(\nu_\tau)$ )



# BOTTOM LINE FROM SNO



- Total neutrino flux from the sun is consistent with expectation ( $10^6/\text{cm}^2/\text{sec}$ )

$$\phi_{\text{NC}}^{\text{SNO}} = 6.42_{-1.57}^{+1.57} (\text{stat.})_{-0.58}^{+0.55} (\text{syst.})$$

$$\phi_{\text{SSM}} = 5.05_{-0.81}^{+1.01}$$

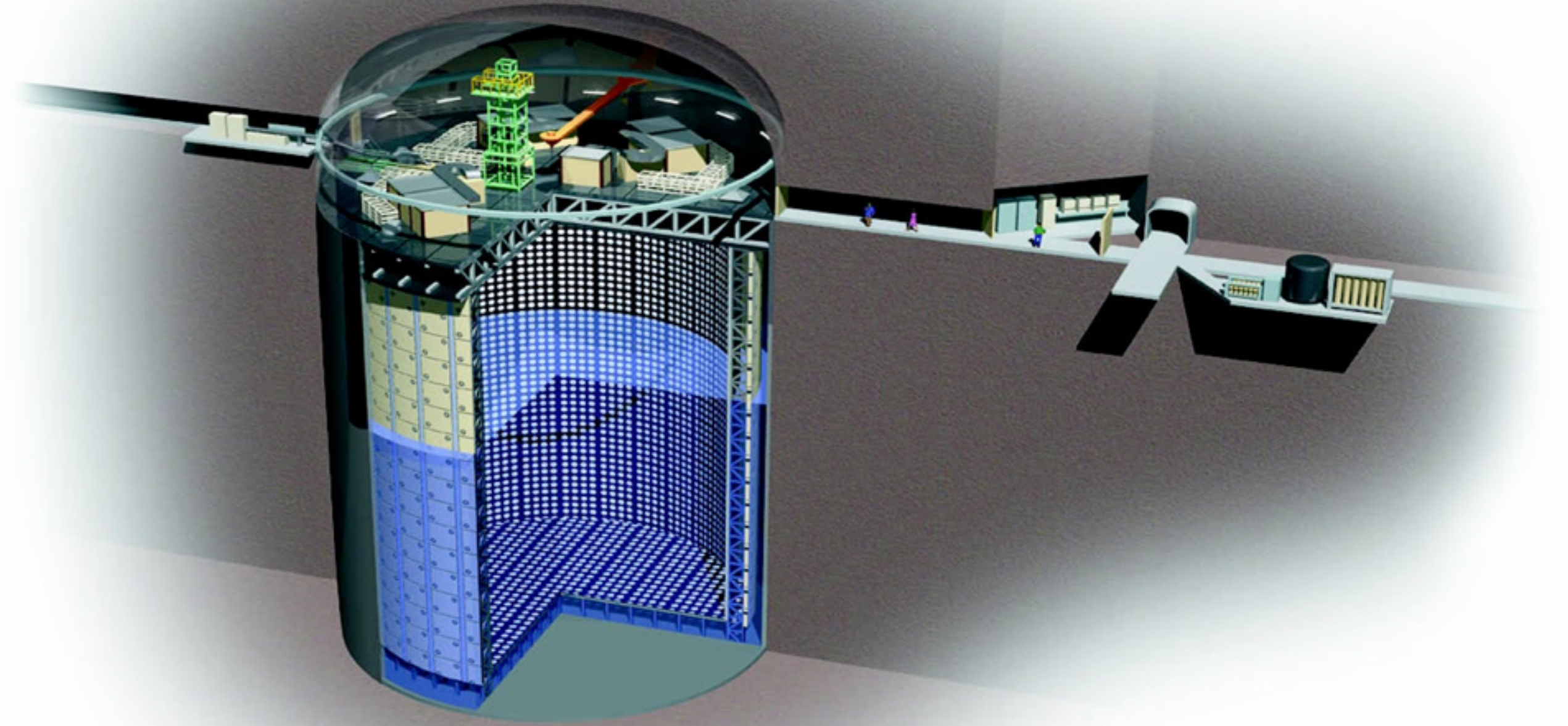
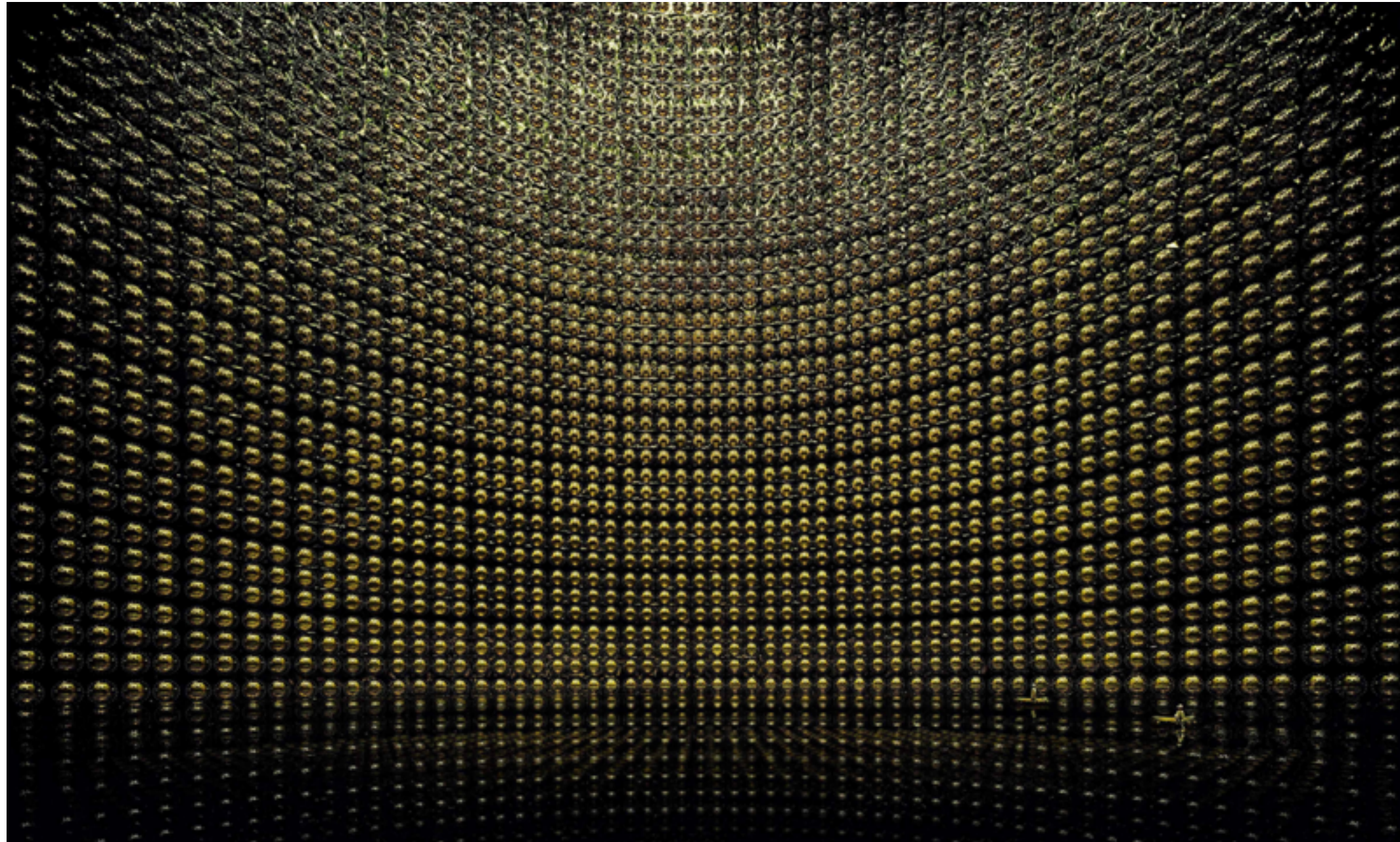
- Only a fraction of this is  $\nu_e$ , the rest  $\nu_\mu, \nu_\tau$

$$\phi_e = 1.76_{-0.05}^{+0.05} (\text{stat.})_{-0.09}^{+0.09} (\text{syst.})$$

$$\phi_{\mu\tau} = 3.41_{-0.45}^{+0.45} (\text{stat.})_{-0.45}^{+0.48} (\text{syst.})$$

- Solution to the solar neutrino problem:
  - experiments sensitive to only  $\nu_e$  observe only a small fraction (1/3) of the total neutrinos
  - SNO showed that the other 2/3 are there in the form of  $\nu_\mu$  and  $\nu_\tau$

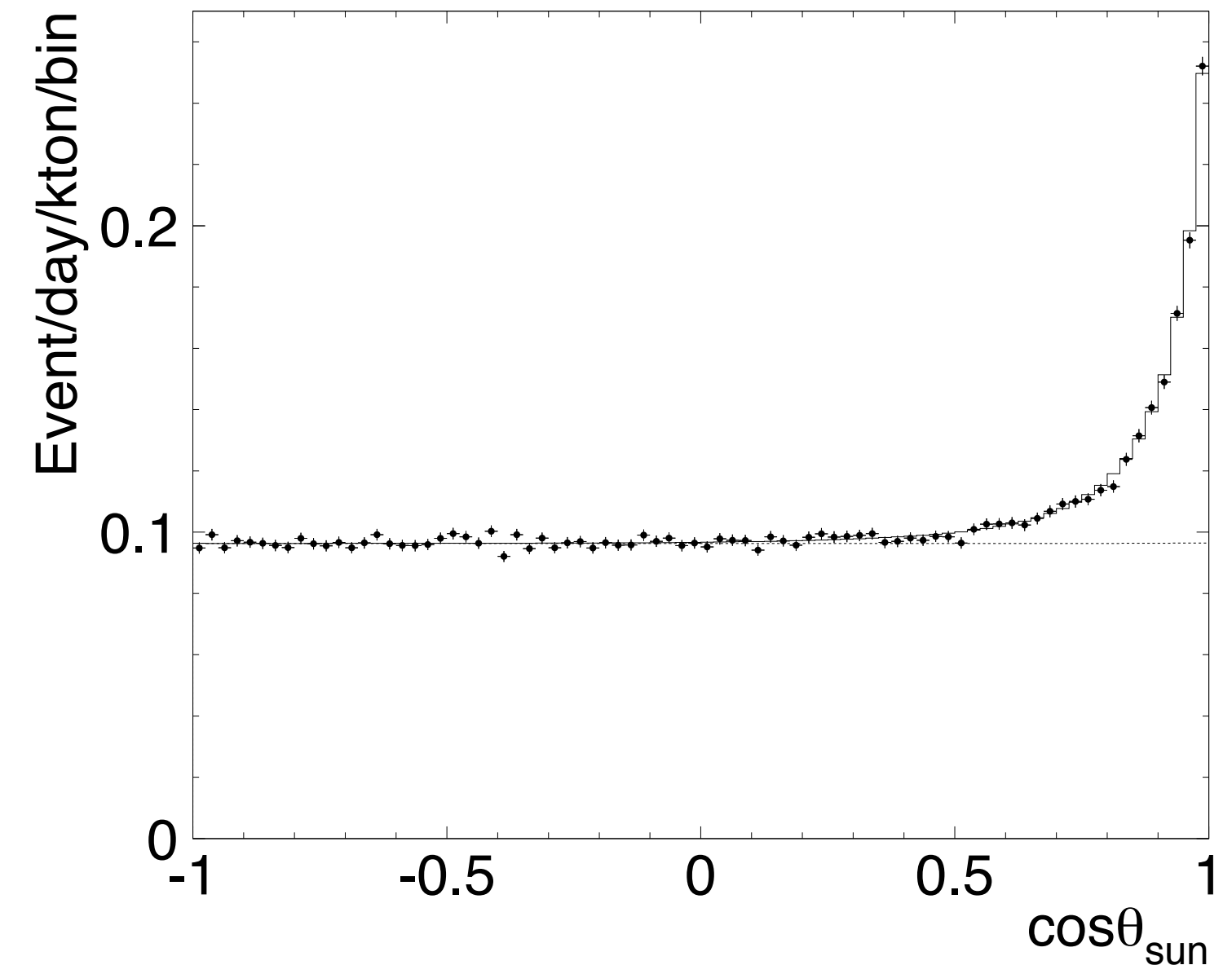
# SUPER-KAMIOKANDE



- 50 kt water Cherenkov detector with 1000 m of overburden
  - light water (no D<sub>2</sub>O like SNO)
- 32 kt inner volume viewed by 11,129 50 cm PMTs
  - typically events at least 2 m from the PMTs are used in analysis. This defines a 22.5 kton “fiducial volume”.
- Outer “veto” volume viewed by 1,885 20 cm PMTs
  - tag particles entering from outside the detector or particles exiting the detector

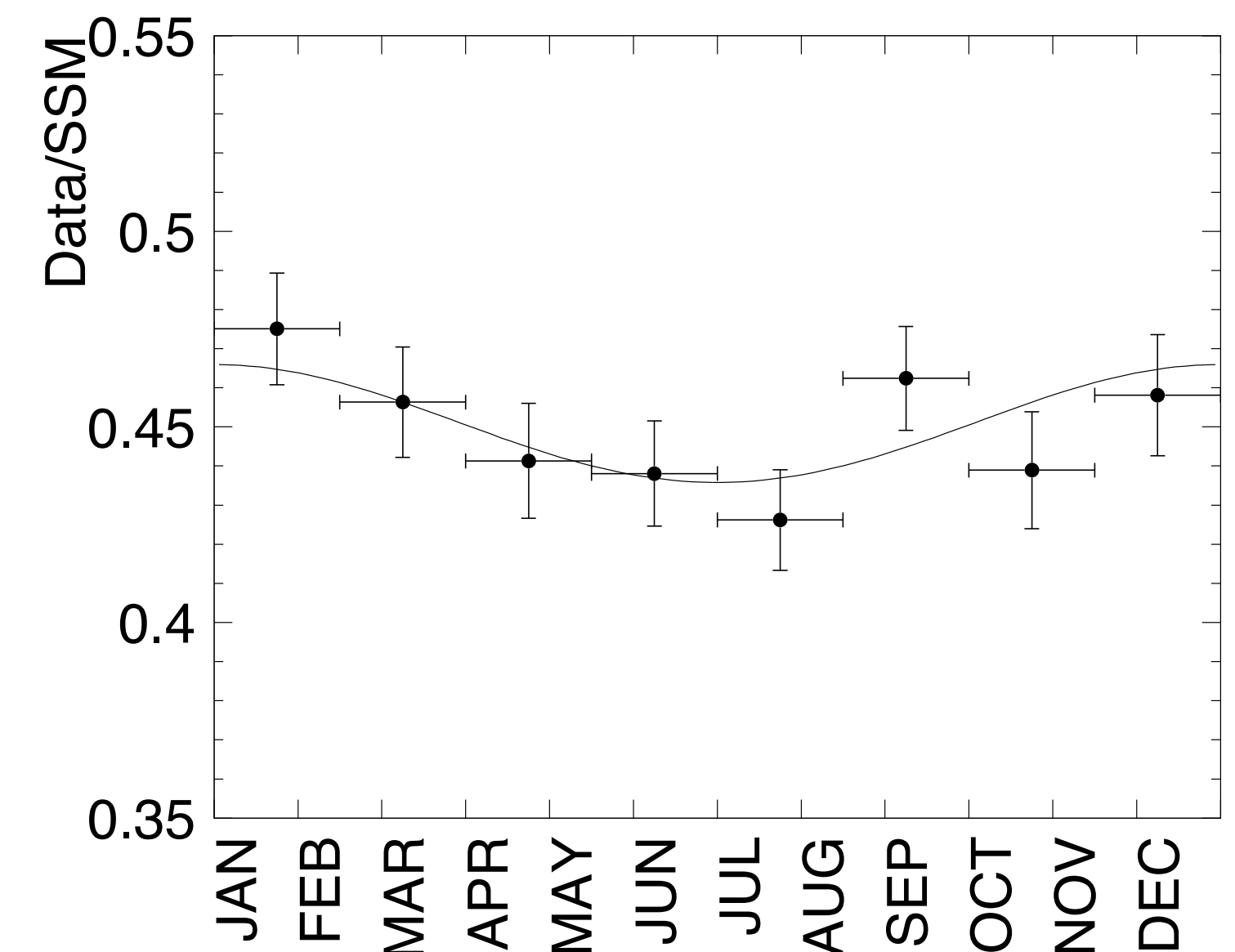
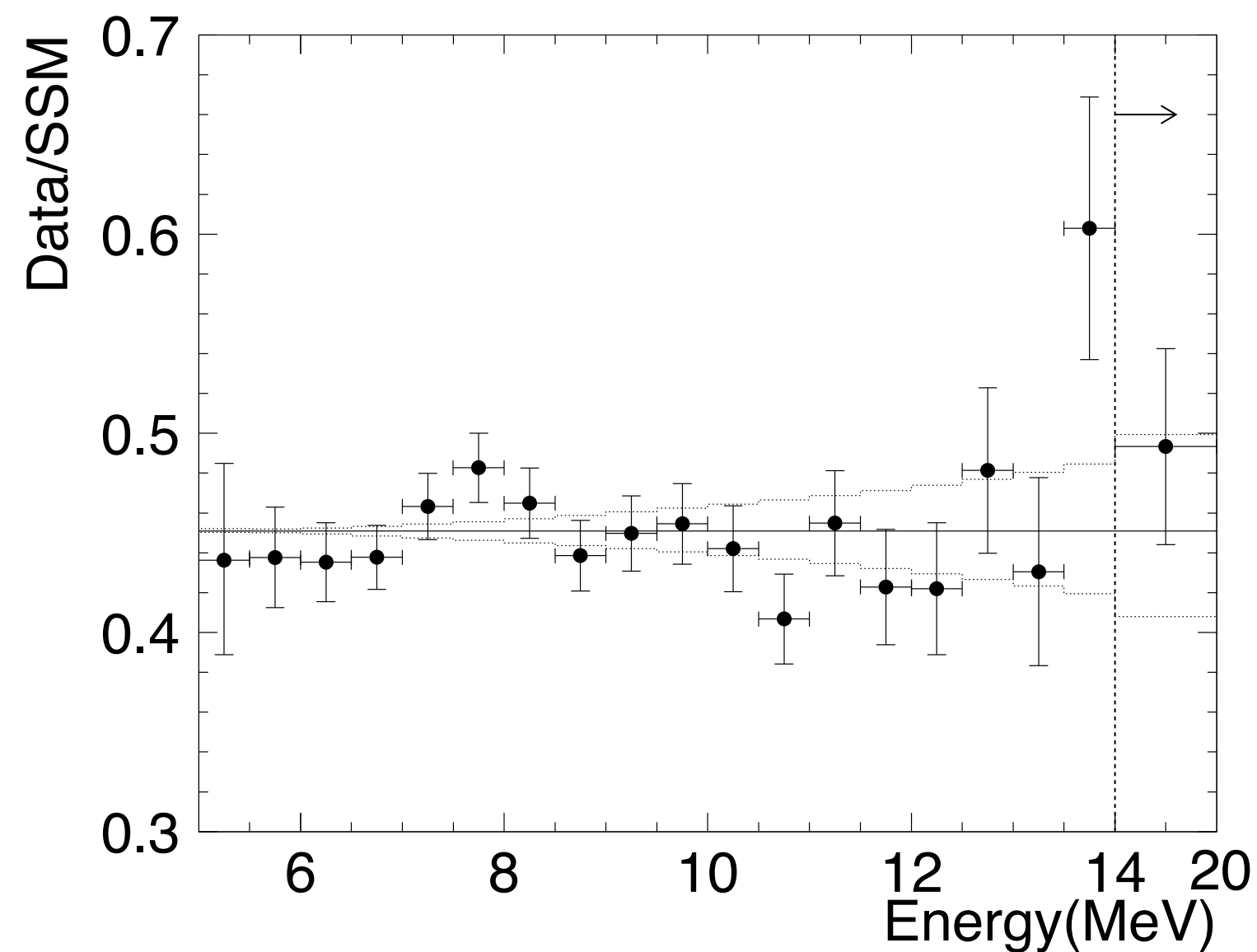
# SOLAR DATA FROM SUPER-KAMIOKANDE

- Very high statistics of elastic scattering events due to large volume
  - ~20x SNO
- Allows detailed study of:
  - energy dependence of solar neutrino deficit
    - none observed . . . .
  - seasonal dependence
    - expected  $R^2$  dependence observed . . . . .

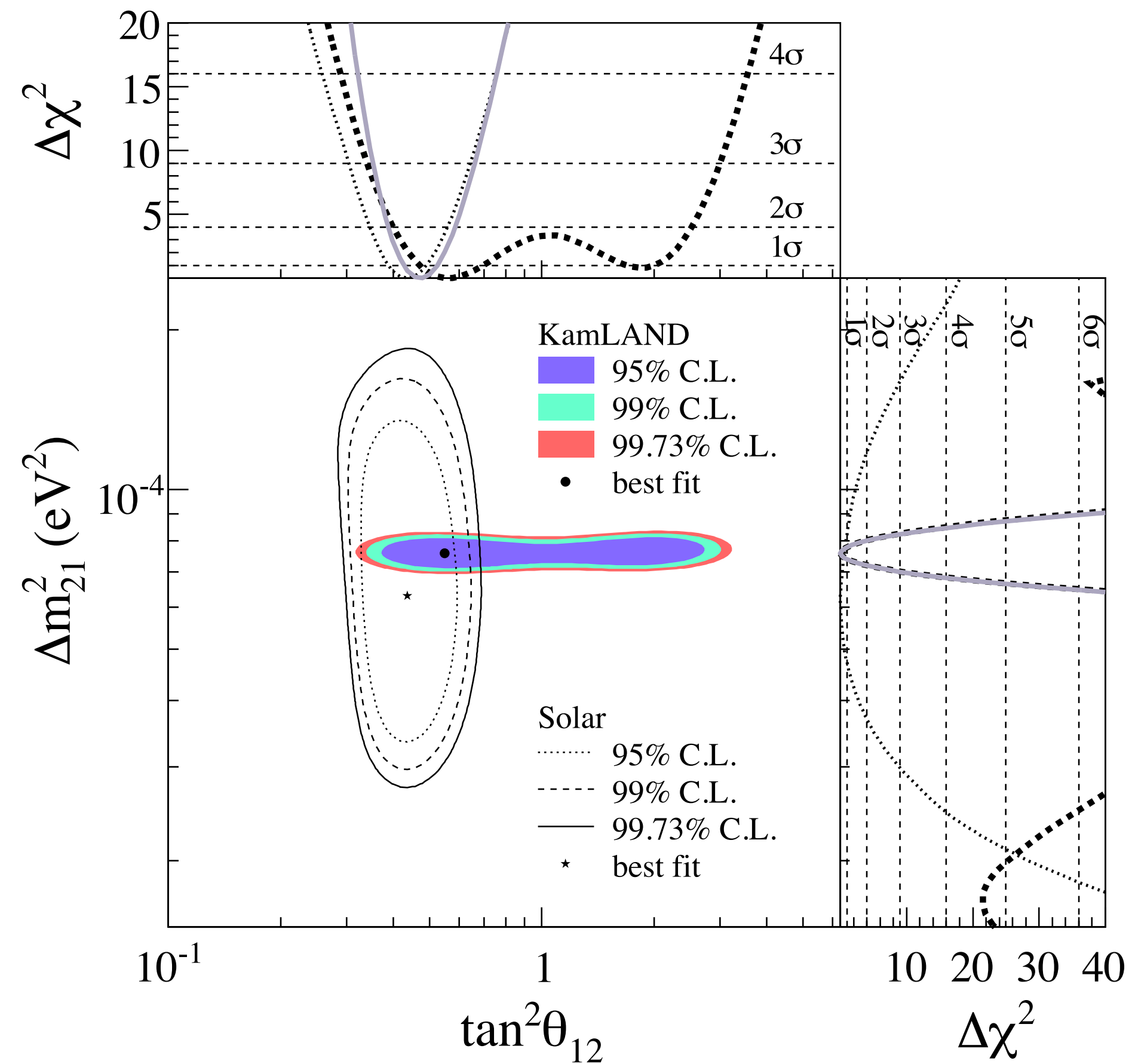


$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \times \sin^2 \left[ 1.27 \Delta m^2 \frac{L(\text{km})}{E(\text{GeV})} \right]$$

- No evidence of oscillatory behaviour in energy or distance . . .
- Just an overall deficit . . .



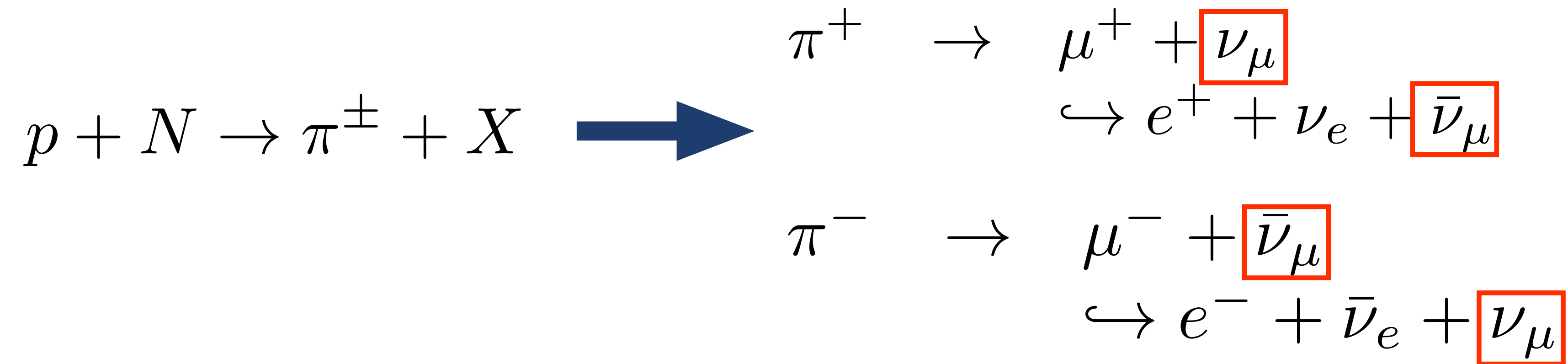
# THE SOLUTION



- SNO observes that  $\sim 2/3$  of  $\nu_e$  from the sun have converted to  $\nu_\mu, \nu_\tau$
- SK however observes that there is no energy dependence or distance dependence of the  $\nu_e$  survival probability
- KamLAND, on the other hand, sees a very clear oscillatory behaviour with  $\Delta m^2 = 7.6 \times 10^{-5} \text{ eV}^2$
- The strong matter effects in the sun make  $\nu_e$  (electron neutrinos)  $\sim$  energy eigenstate
- As the neutrino propagates through the sun and out into the vacuum of space, they stay as an energy eigenstate corresponding to  $\nu_2$  (the heavier of the mass eigenstates)
- $\nu_2$  is an energy eigenstate. It doesn't oscillate!
  - flavour content is "locked in" on its transit to earth
  - no E or L dependence . . . . .

# ATMOSPHERIC NEUTRINOS

- Atmospheric neutrinos are produced by the interaction of cosmic ray protons on nuclei in the atmosphere

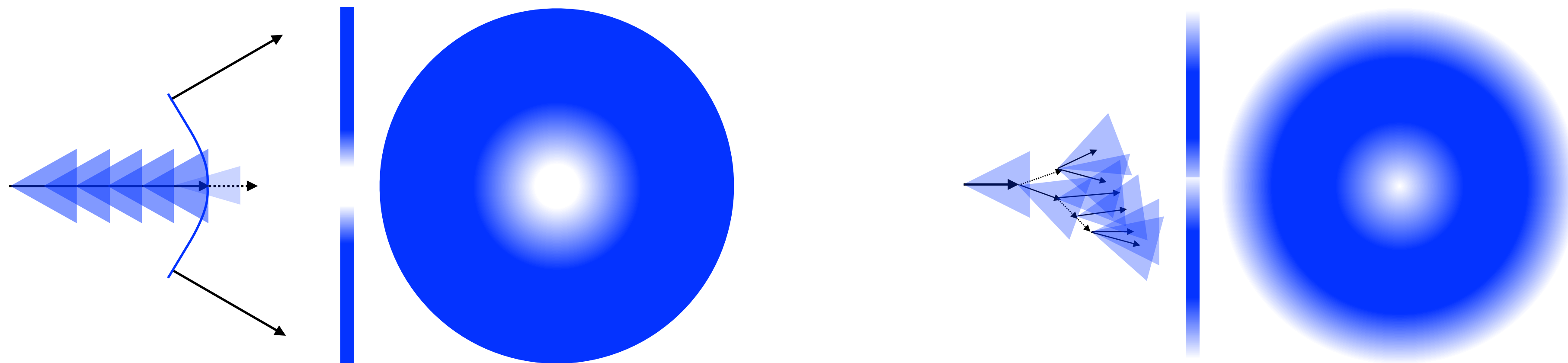
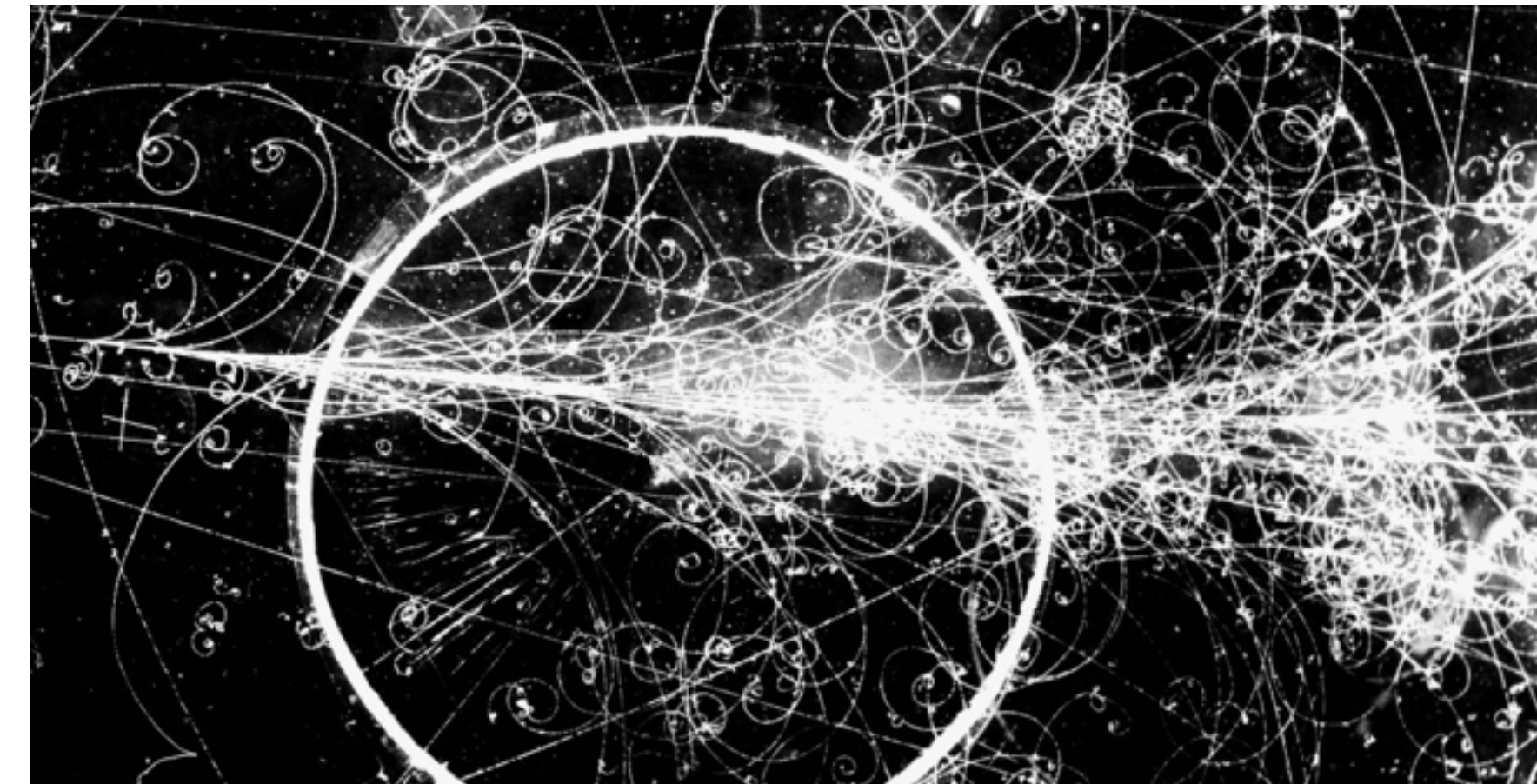
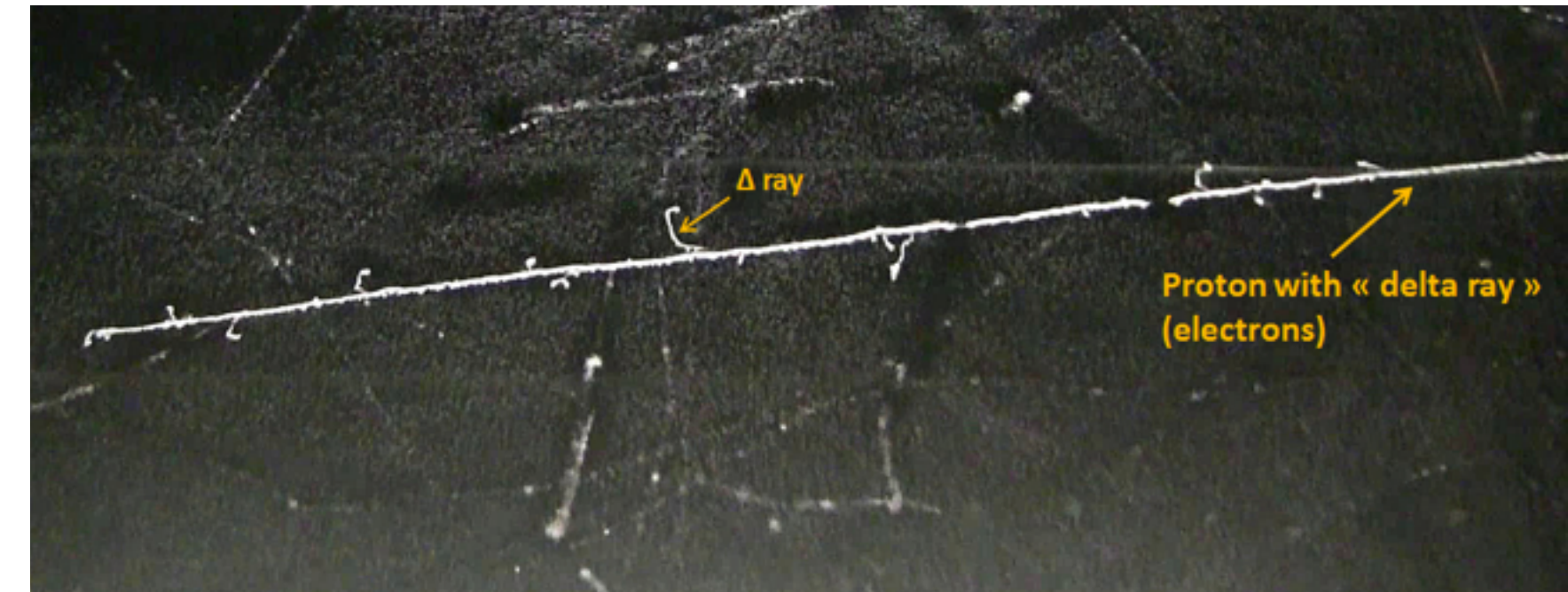


- Naively, expect a 2:1 ratio of muon (anti)neutrino to electron (anti)neutrino ratio in the absence of oscillations
  - can we test this by identifying muon neutrinos and electron neutrinos?
  - look for muon production (from  $\nu_{\mu}$ ) and electron production (from  $\nu_e$ ).

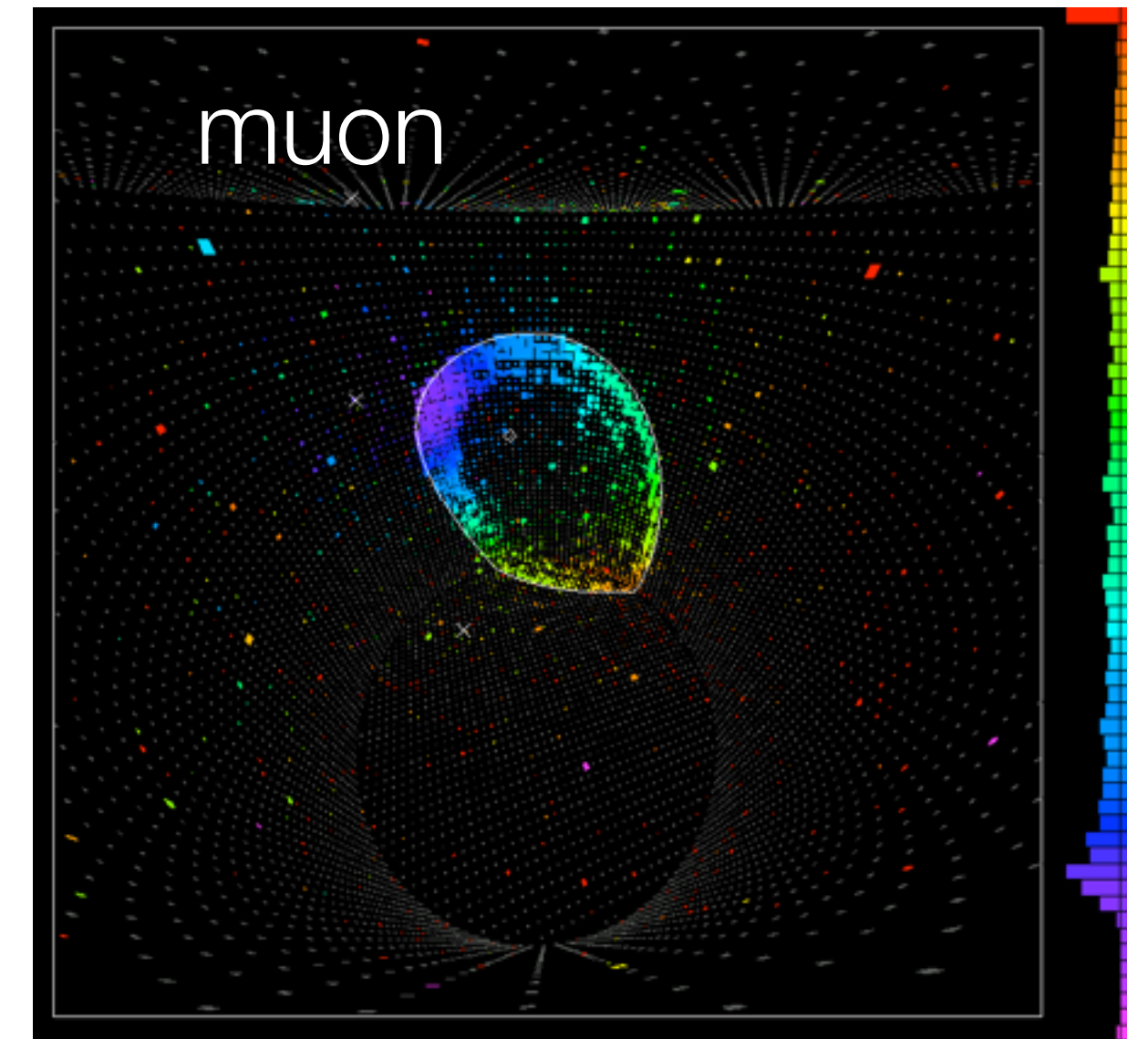
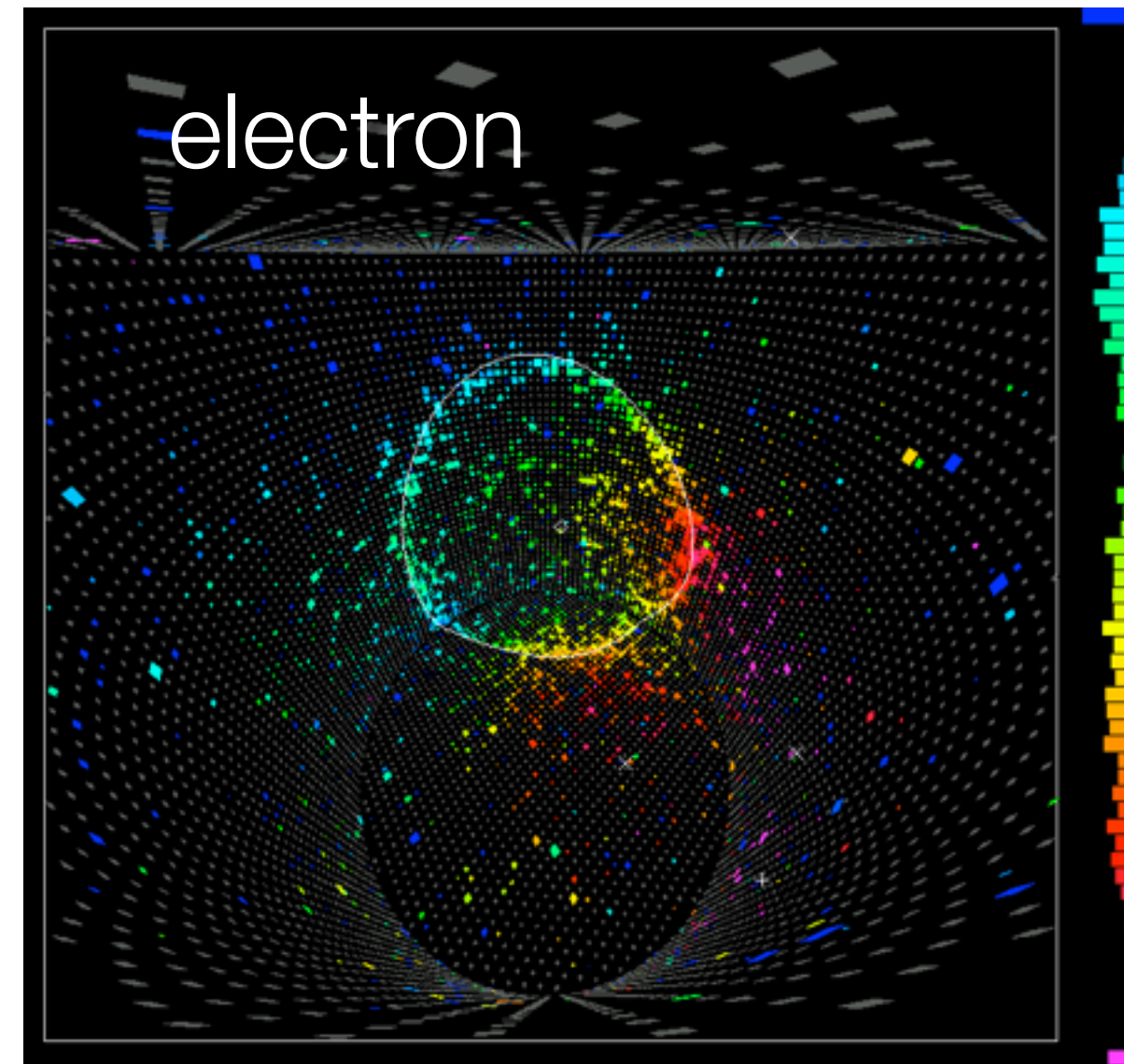
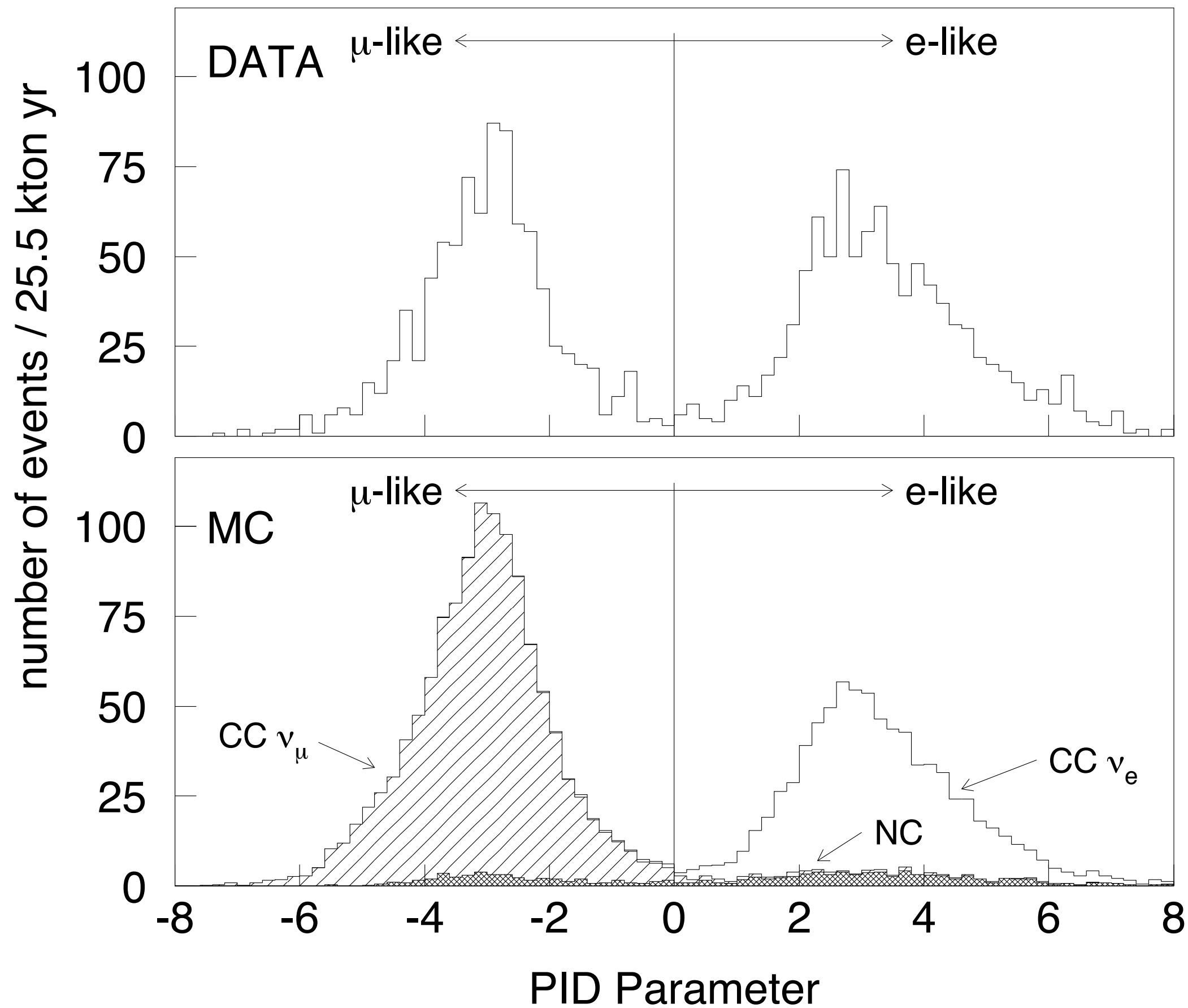


# PARTICLE IDENTIFICATION

- Other processes as charged particles passes through media
- Ionization loss: steady energy transfer by ionizing atoms.
- Bremsstrahlung:
  - photon emission from acceleration of particle in field of atomic nucleus
    - Photon can then Compton scatter, pair produce
    - electrons/positrons from this can in emit more photons
    - "Electromagnetic shower"
- Č Ring can tell us:
  - position/direction/energy of the particle "track reconstruction"
  - identify the particle as non-showering ( $\mu$ ,  $\pi$ ,  $p$ ) vs.  $e/\gamma$

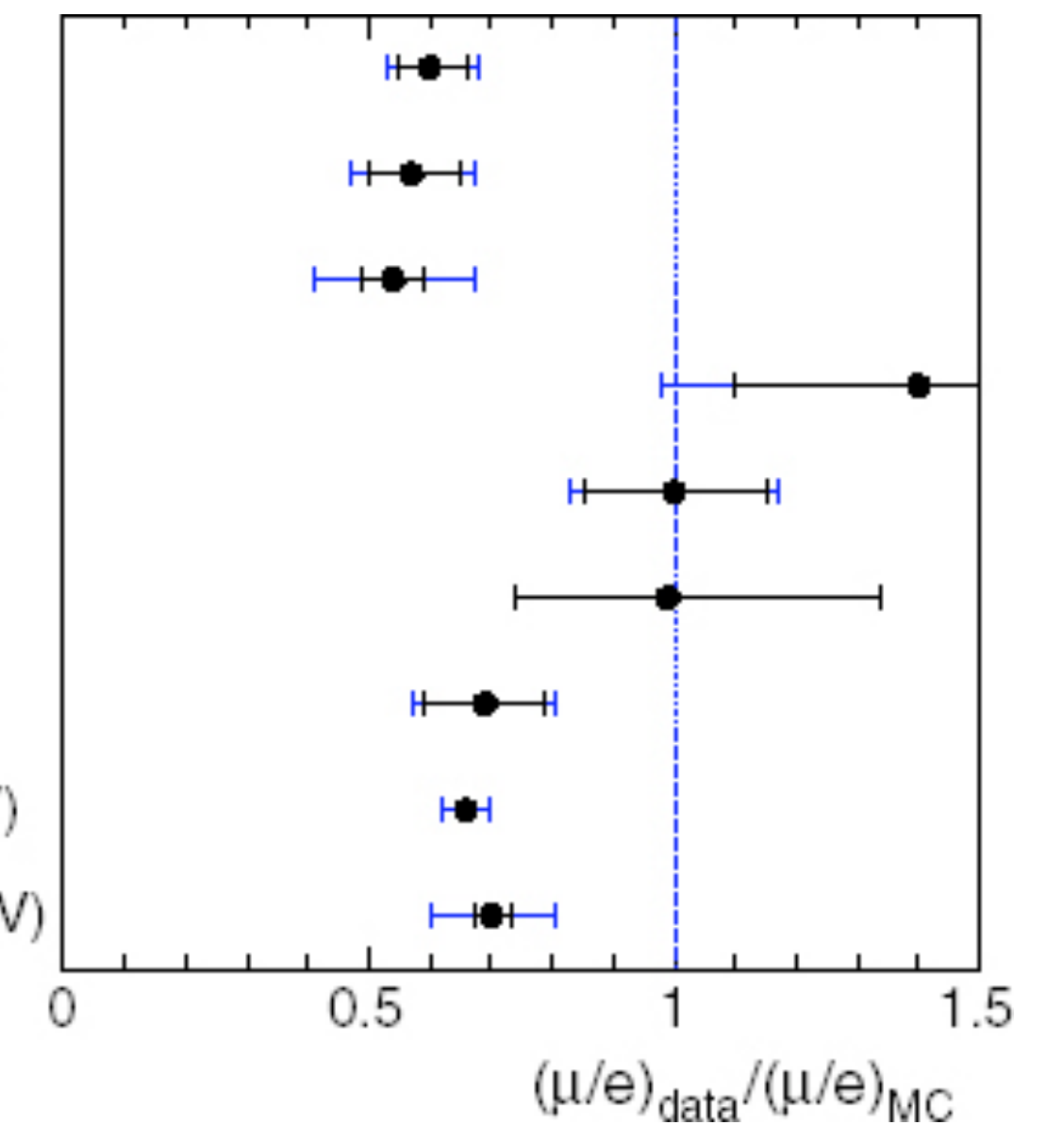


# PARTICLE IDENTIFICATION IN SK



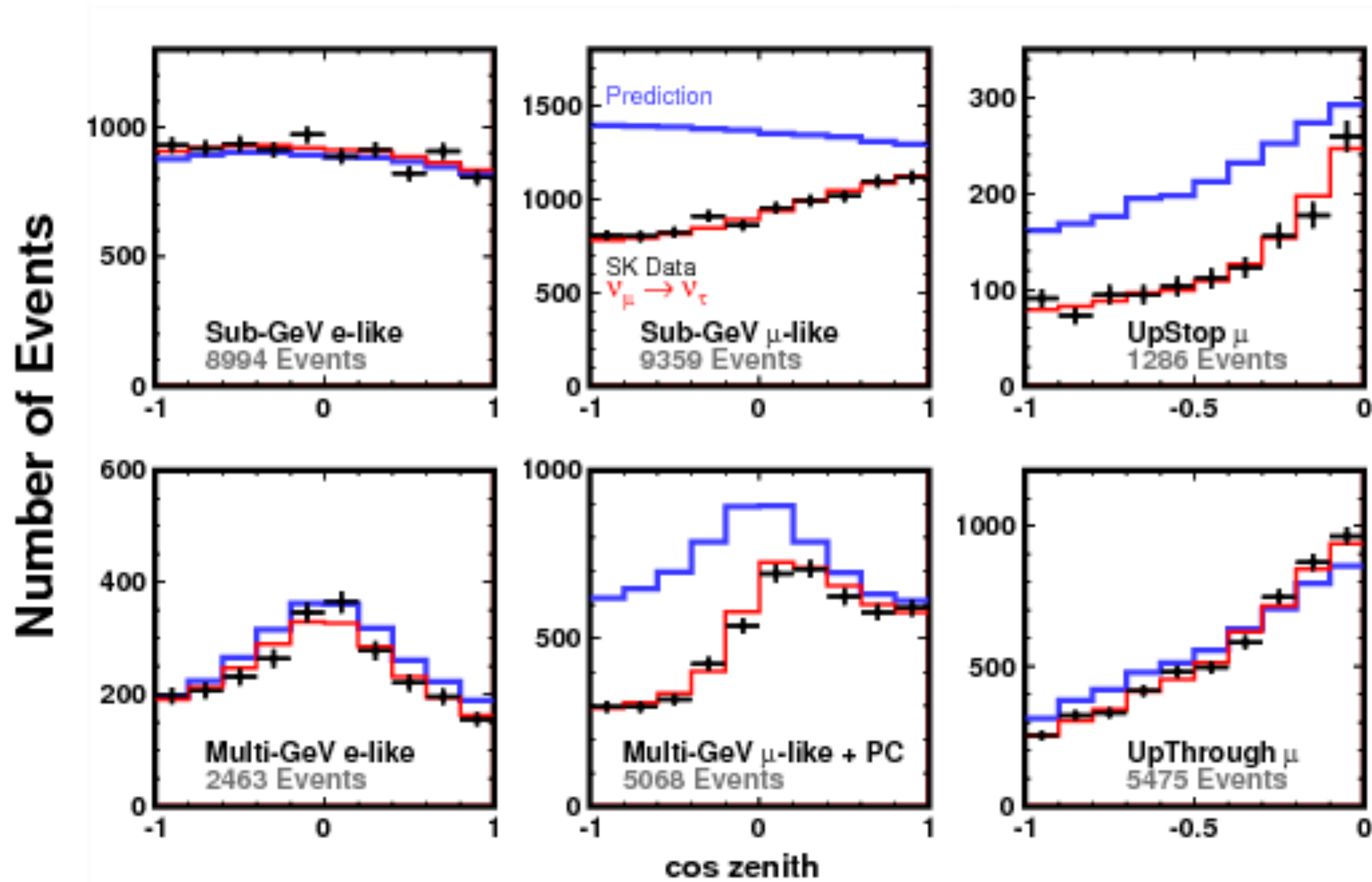
- particle identification variable to separate electron-like and muon-like Cherenkov rings in the Super-Kamiokande detector
- can separate electrons and muons (hence  $\nu_e$  and  $\nu_\mu$ ) at the 99% level

Kam.(sub-GeV)  
 Kam.(multi-GeV)  
 IMB-3(sub-GeV)  
 IMB-3(multi-GeV)  
 Frejus  
 Nusex  
 Soudan-2  
 Super-K(sub-GeV)  
 Super-K(multi-GeV)



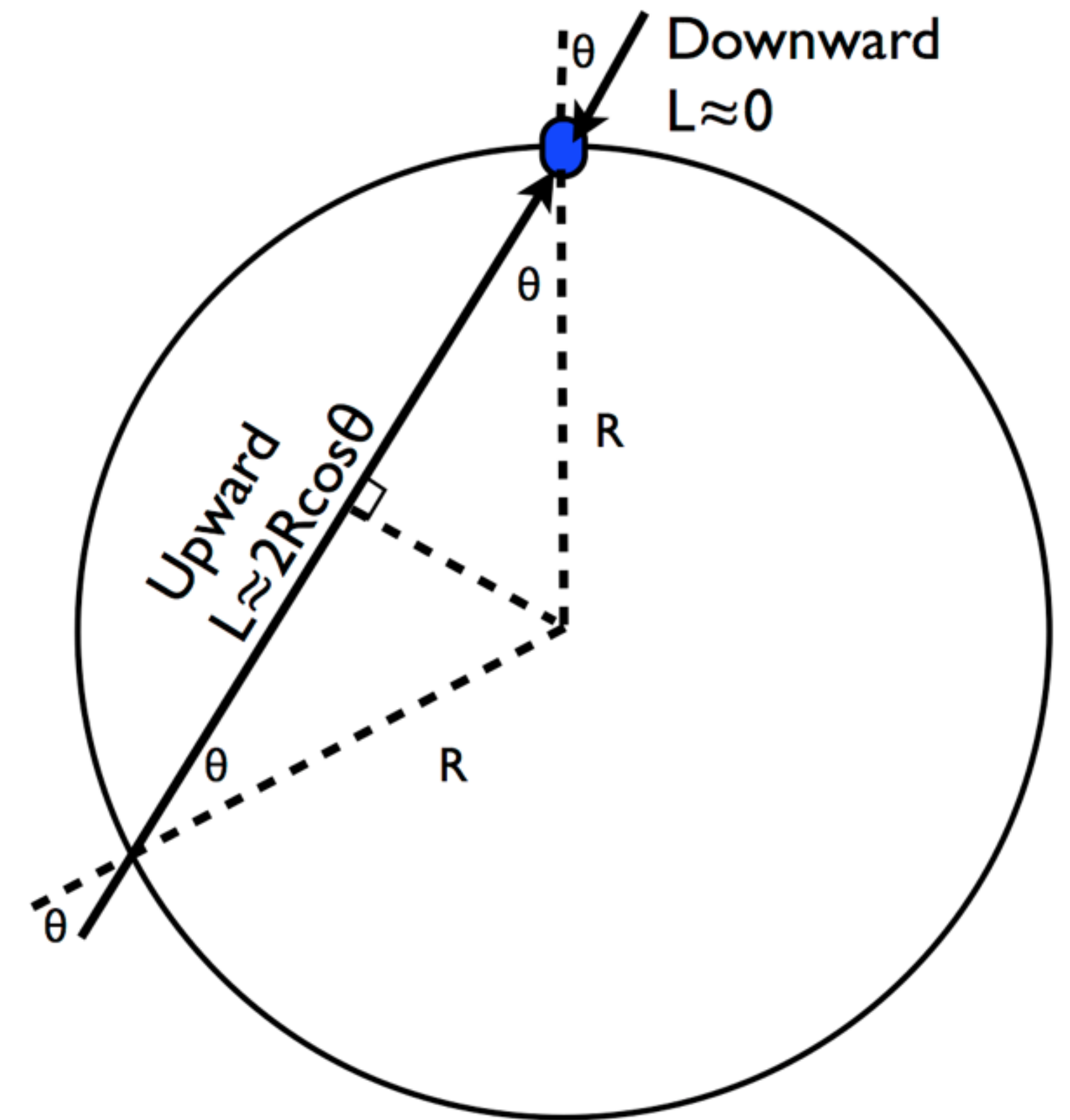
# FURTHER EVIDENCE

SK-I+II+III+IV, 4581 Days



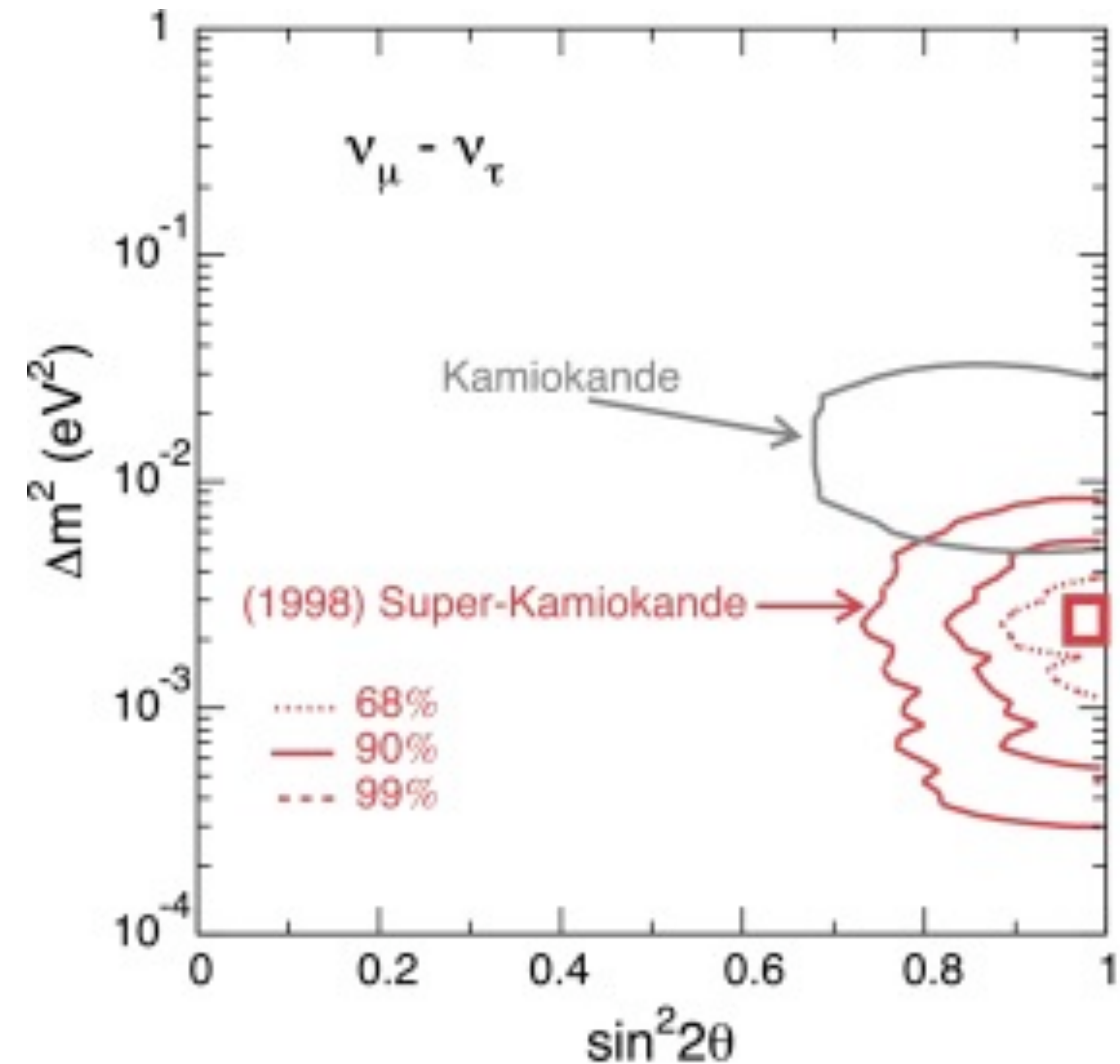
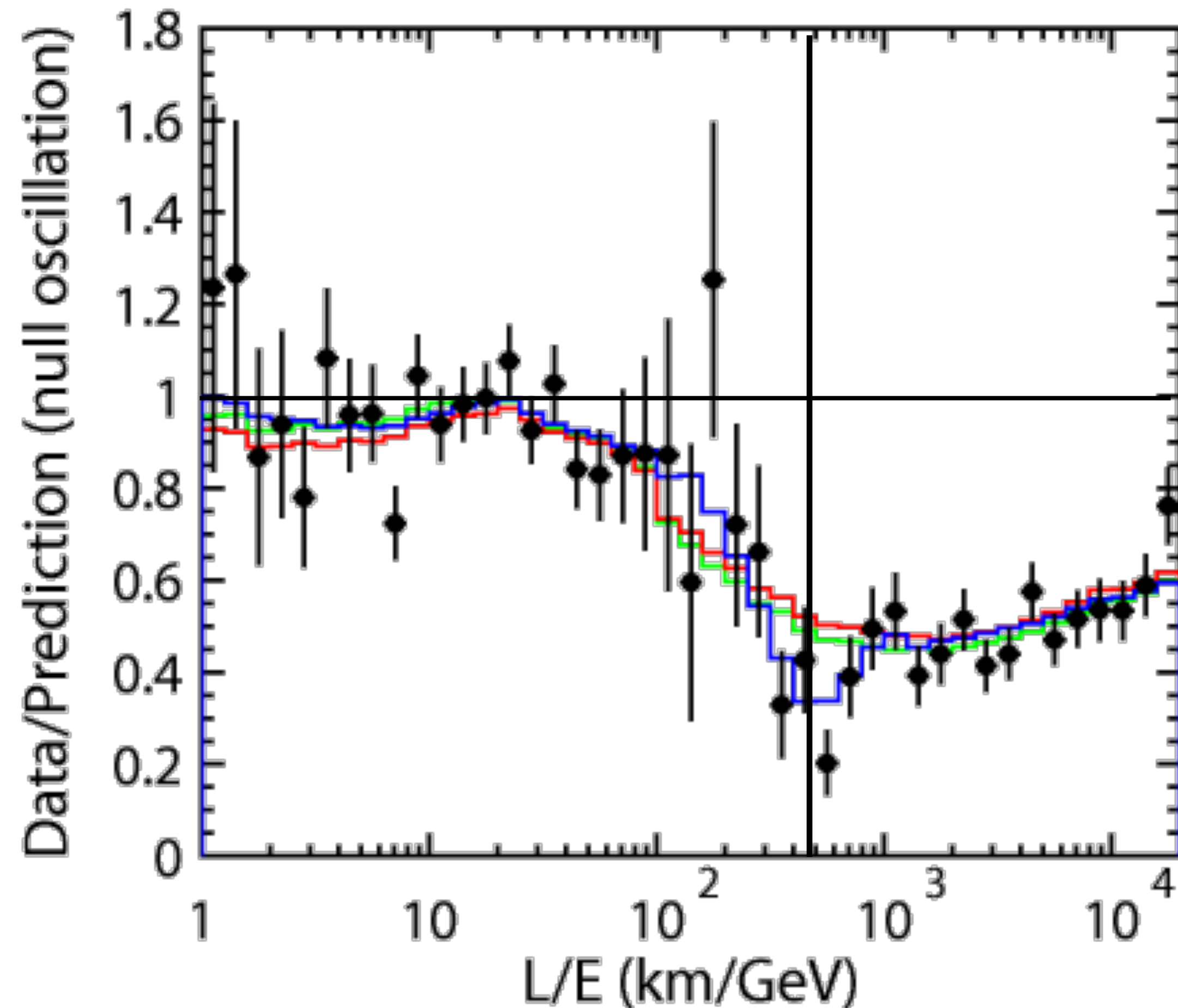
- Zenith angle distribution of deficit agrees with neutrino oscillations

- Neutrino oscillations should have a dependence on the path length from production to detection.
- For atmospheric neutrinos, is related to the "zenith angle" of the neutrino



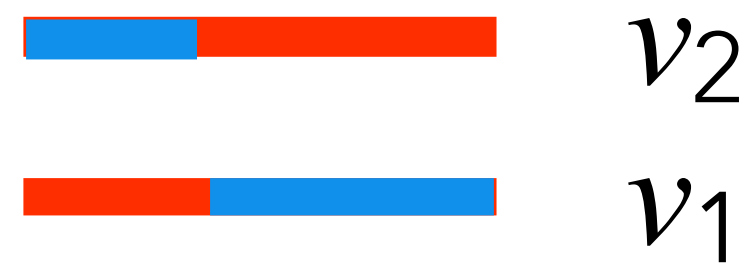
# ANOTHER LOOK

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \times \sin^2 \left[ 1.27 \Delta m^2 \frac{L(\text{km})}{E(\text{GeV})} \right]$$



- Plot deficit directly as a function of  $L/E$  using subset of interaction where “pointing” accuracy is good.
- Location of minimum tells us  $\Delta m^2$ :  $1.27 \times \Delta m^2(\text{eV}^2) \times 600 \text{ km/GeV} = \pi/2 \rightarrow \Delta m^2 \sim 2.5 \times 10^{-3} \text{ eV}^2$
- “Depth” of minimum tells us  $\sin^2 2\theta$ :  $\sin^2 2\theta \sim 1$  (maximal mixing)

# WHAT DO WE KNOW?



$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} \\ -\sin \theta_{12} & \cos \theta_{12} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

- From solar measurement:
  - $\nu_e$  component of  $\nu_2$  is  $\sim 1/3 \rightarrow \sin^2 \theta_{12} = 1/3$
  - $\theta_{12} \sim 35$  degrees
- From KamLAND
  - $\sin^2 2\theta_{12} = 0.85 \rightarrow \theta_{12} \sim 34$  degrees
  - $\Delta m_{21}^2 \sim 7.5 \times 10^{-5} \text{ eV}^2$



$$\begin{pmatrix} \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} \cos \theta_{23} & \sin \theta_{23} \\ -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \nu_a \\ \nu_b \end{pmatrix}$$

- From atmospheric measurement
  - $\nu_\mu$  disappearance is  $\sim$  maximal
  - $\theta_{23} \sim 45$  degrees
  - $\Delta m_{ba}^2 \sim 2.5 \times 10^{-5} \text{ eV}^2$
  - excess of  $\nu_e$  not observed:
    - $\nu_y$  is primarily  $\nu_\tau$

# The Nobel Prize in Physics 2015

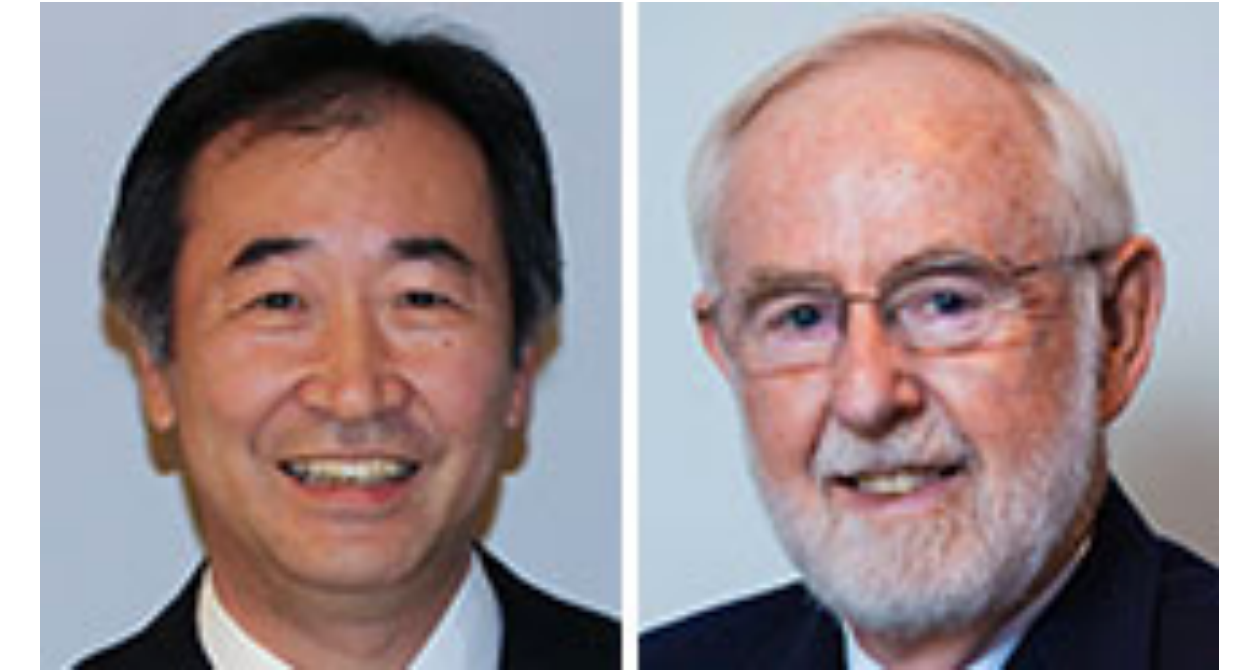
The Royal Swedish Academy of Sciences has decided to award the Nobel Prize in Physics for 2015 to

## Takaaki Kajita

Super-Kamiokande Collaboration  
University of Tokyo, Kashiwa, Japan

## Arthur B. McDonald

Sudbury Neutrino Observatory Collaboration  
Queen's University, Kingston, Canada



*“for the discovery of neutrino oscillations, which shows that neutrinos have mass”*

