

PHYSICS 489/1489

LECTURE 9:

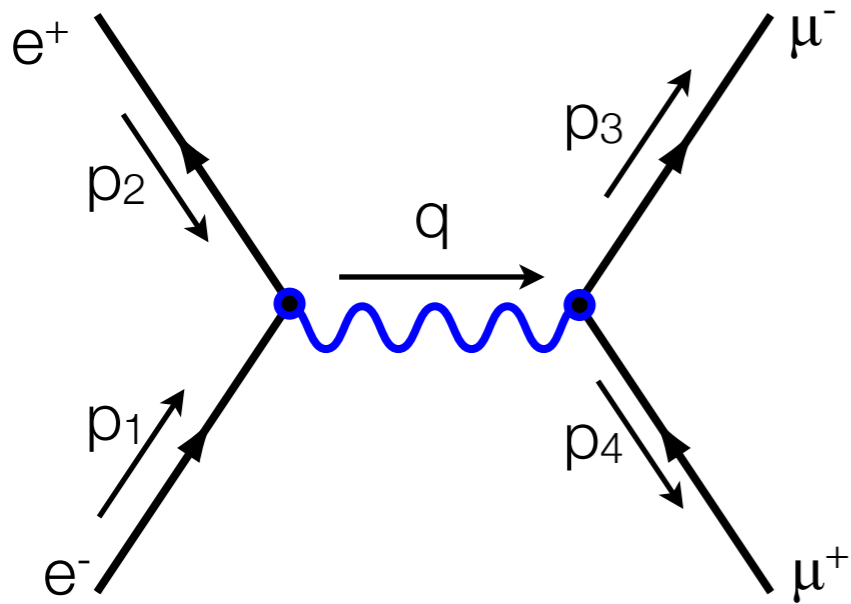
QED EXPERIMENTS

A FEW NOTES

- There were a few typos in the last lecture
 - I've placed an updated version of the slides on the website
- Please note that Problem Set 2 is posted
 - due 25 October

LAST TIME

- We calculated the cross section for $e^+e^- \rightarrow \mu^+\mu^-$



$$\mathcal{M} = -\frac{g_e^2}{(p_1 + p_2)^2} [\bar{u}(3) \gamma^\mu v(4)] [\bar{v}(2) \gamma_\mu u(1)]$$

- Evaluated the matrix element with various helicity combinations in the massless limit

$$\begin{aligned} \mathcal{M}_{LR \rightarrow LR} &= -\frac{e^2}{4E^2} [\bar{u}_{3L} \gamma^\mu v_{4R}] [\bar{v}_{2R} \gamma_\mu u_{1L}] & \mathcal{M}_{LR \rightarrow RL} &= -\frac{e^2}{4E^2} [\bar{u}_{3R} \gamma^\mu v_{4L}] [\bar{v}_{2R} \gamma_\mu u_{1L}] \\ &= e^2 (1 + \cos \theta) = \mathcal{M}_{RL \rightarrow RL} & &= e^2 \times (-\cos \theta + 1) = \mathcal{M}_{RL \rightarrow LR} \end{aligned}$$

- Obtain the differential (unpolarized, spin-summed) cross section

$$\frac{d\sigma}{d\Omega} = \frac{e^4}{256\pi^2 E^2} (1 \pm \cos \theta)^2 \qquad \frac{d\sigma}{d\Omega} = \frac{e^4}{64\pi^2 s} (1 + \cos^2 \theta)$$

A FEW NOTES:

- The derivation applies to any spin 1/2 fermion so long as
 - massless approximation(s) is appropriate
 - charge is appropriately scaled
- We can integrate over angles to get the total cross section

$$\begin{aligned} \frac{d\sigma}{d\Omega} &= \frac{e^4}{64\pi^2 s} (1 + \cos^2 \theta) \quad \Rightarrow \int d\phi \int d\cos\theta \frac{e^4}{64\pi^2 s} (1 + \cos^2 \theta) \\ &\int d\cos\theta \frac{e^4}{32\pi s} (1 + \cos^2 \theta) \\ \frac{e^4}{12\pi s} &= \frac{4\pi\alpha^2}{3s} \end{aligned}$$

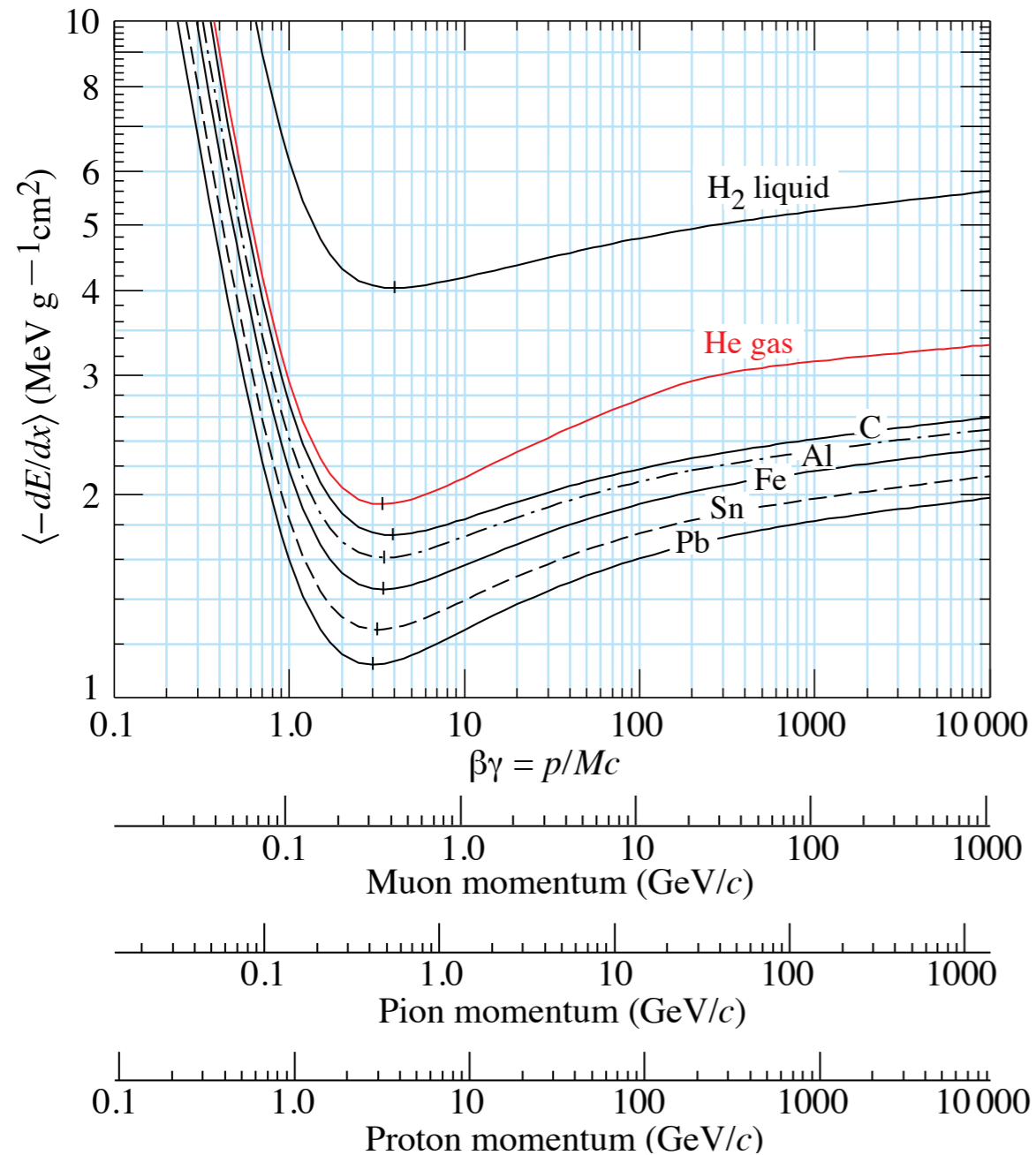
- If we did not neglect the masses, we would obtain:

$$\langle |\mathcal{M}|^2 \rangle = g_e^4 \left[1 + \left(\frac{mc^2}{E} \right)^2 + \left(\frac{Mc^2}{E} \right)^2 + \left[1 - \left(\frac{mc^2}{E} \right)^2 \right] \left[1 - \left(\frac{Mc^2}{E} \right)^2 \right] \cos^2 \theta \right]$$

DETECTING PARTICLES

- For the most part, we can only detect charged particles
 - neutral particles can be detected if they
 - interact with charged particles which are in turn detected
 - decay to produce charged particles
- Detection methods:
 - ionization
 - scintillation
 - Cherenkov radiation
 - acoustic
 -

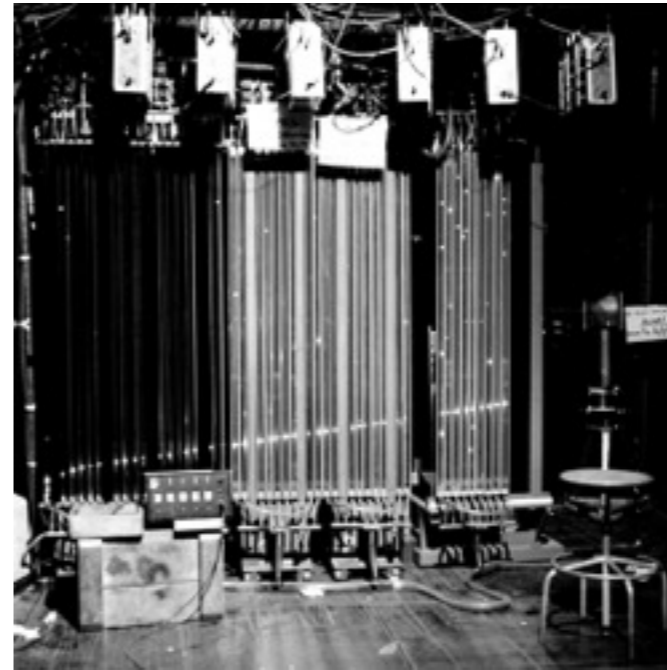
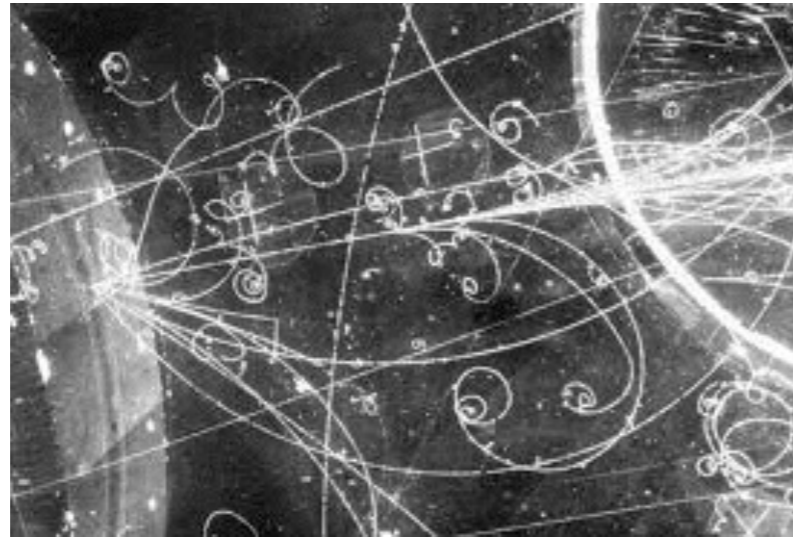
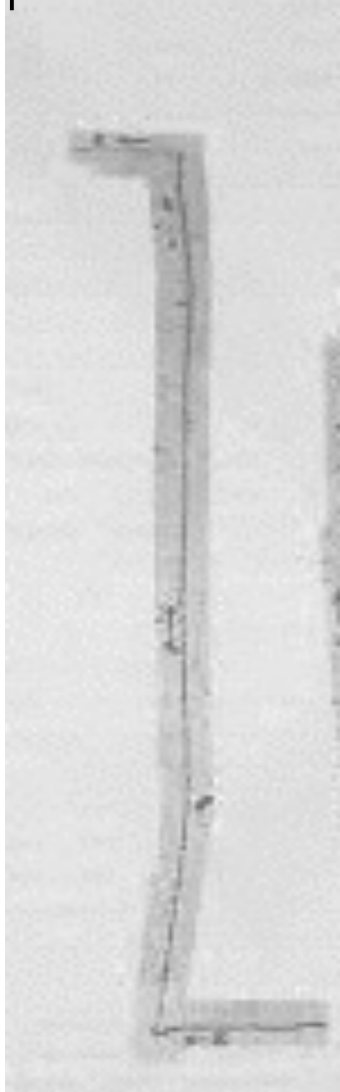
IONIZATION:



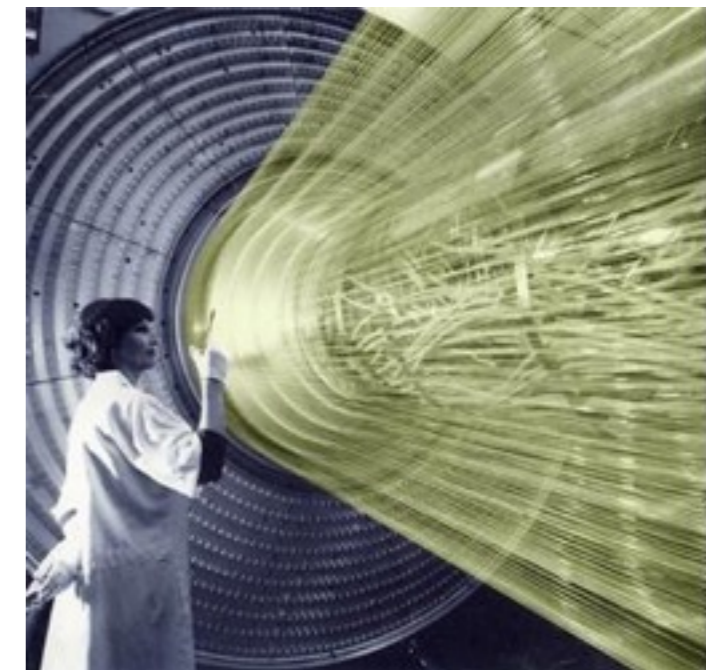
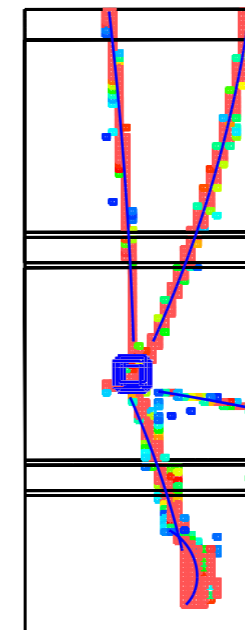
- Knock out of electrons from atom as a charged particle passes through a medium
- Ionization rate depends on velocity of particle
 - if we independently know the velocity of momentum of the particle, we can determine the particle identity
 - e.g. if the medium of
- “Tracking” detectors which determine the trajectory of a particle typically use ionization

HOW TO DETECT IONIZATION

phase transitions

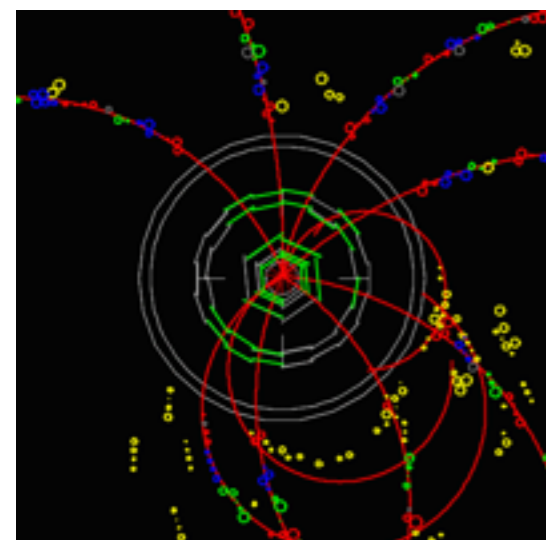
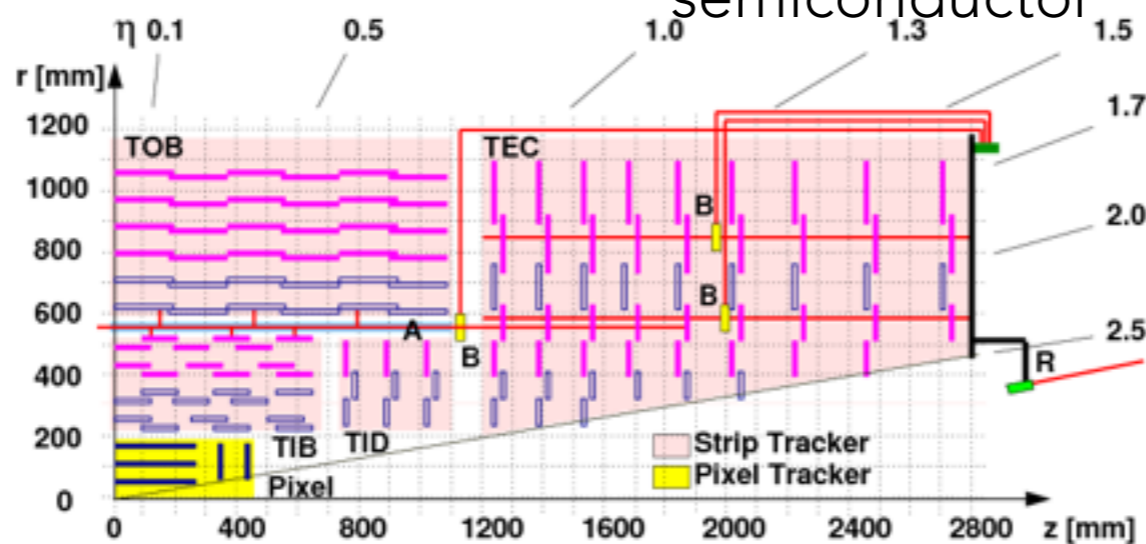


sparking, streaming

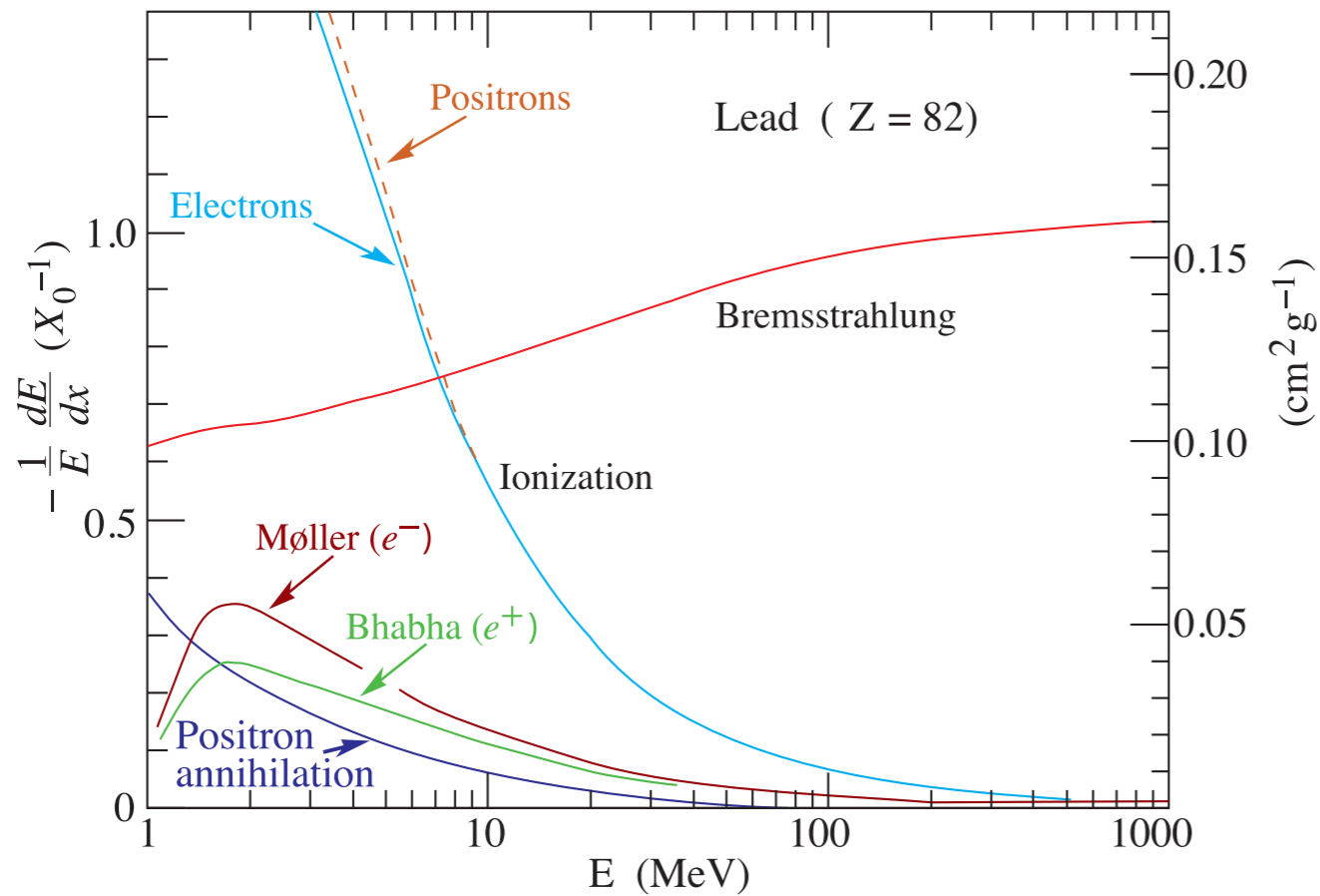


drifting in gas/liquid

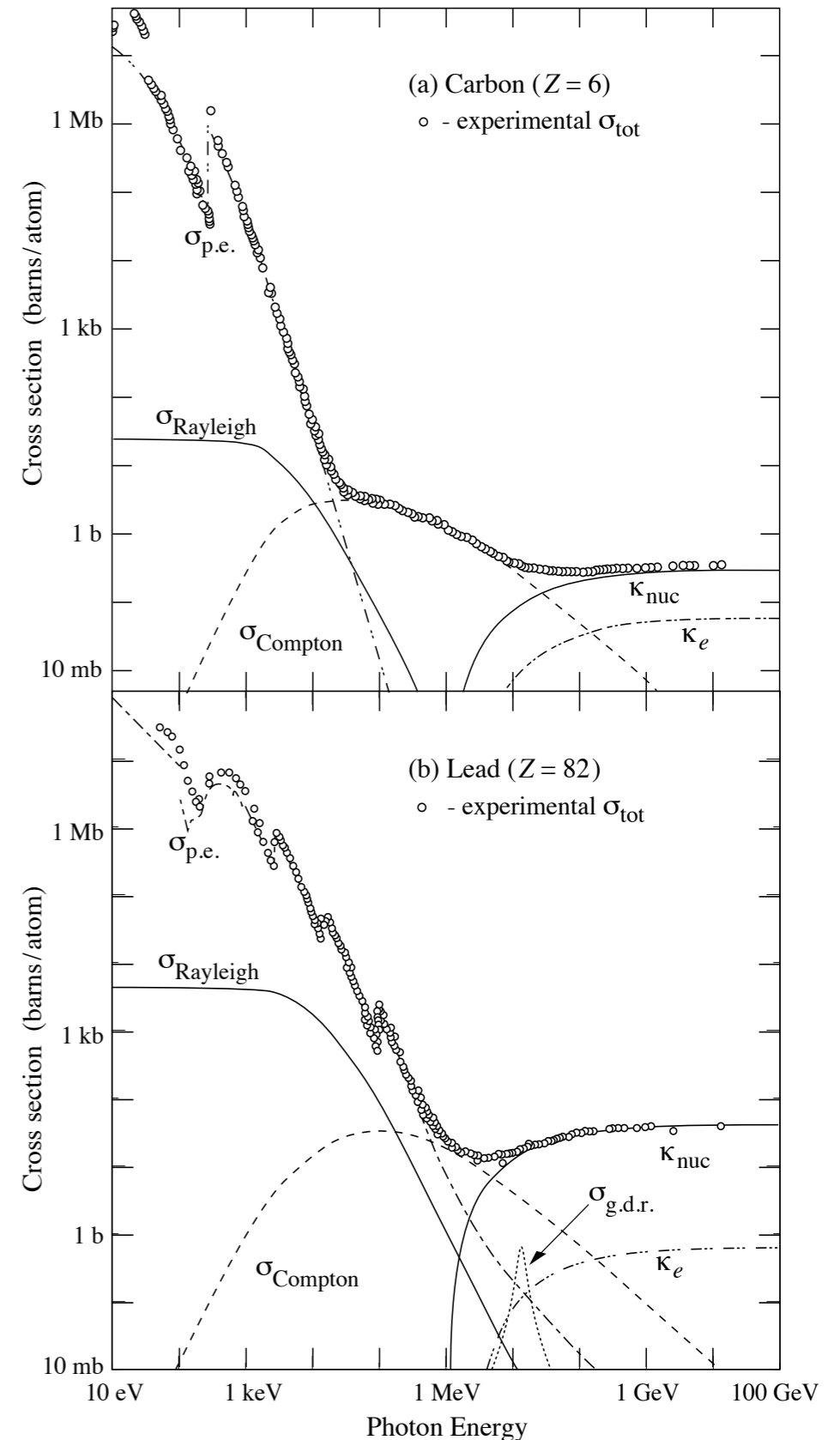
semiconductor



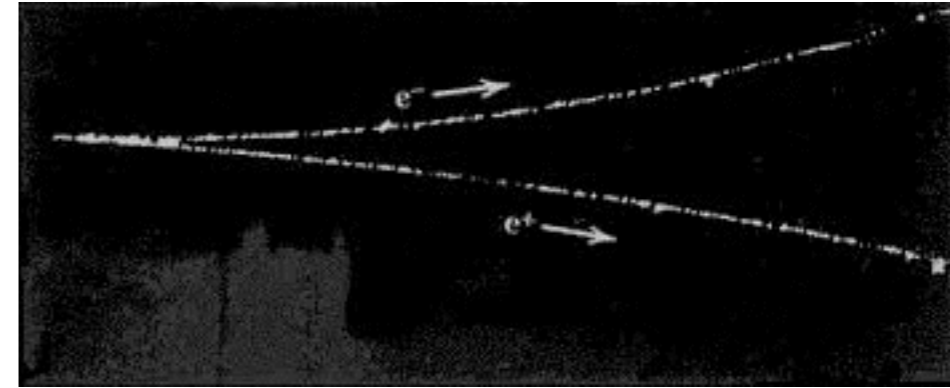
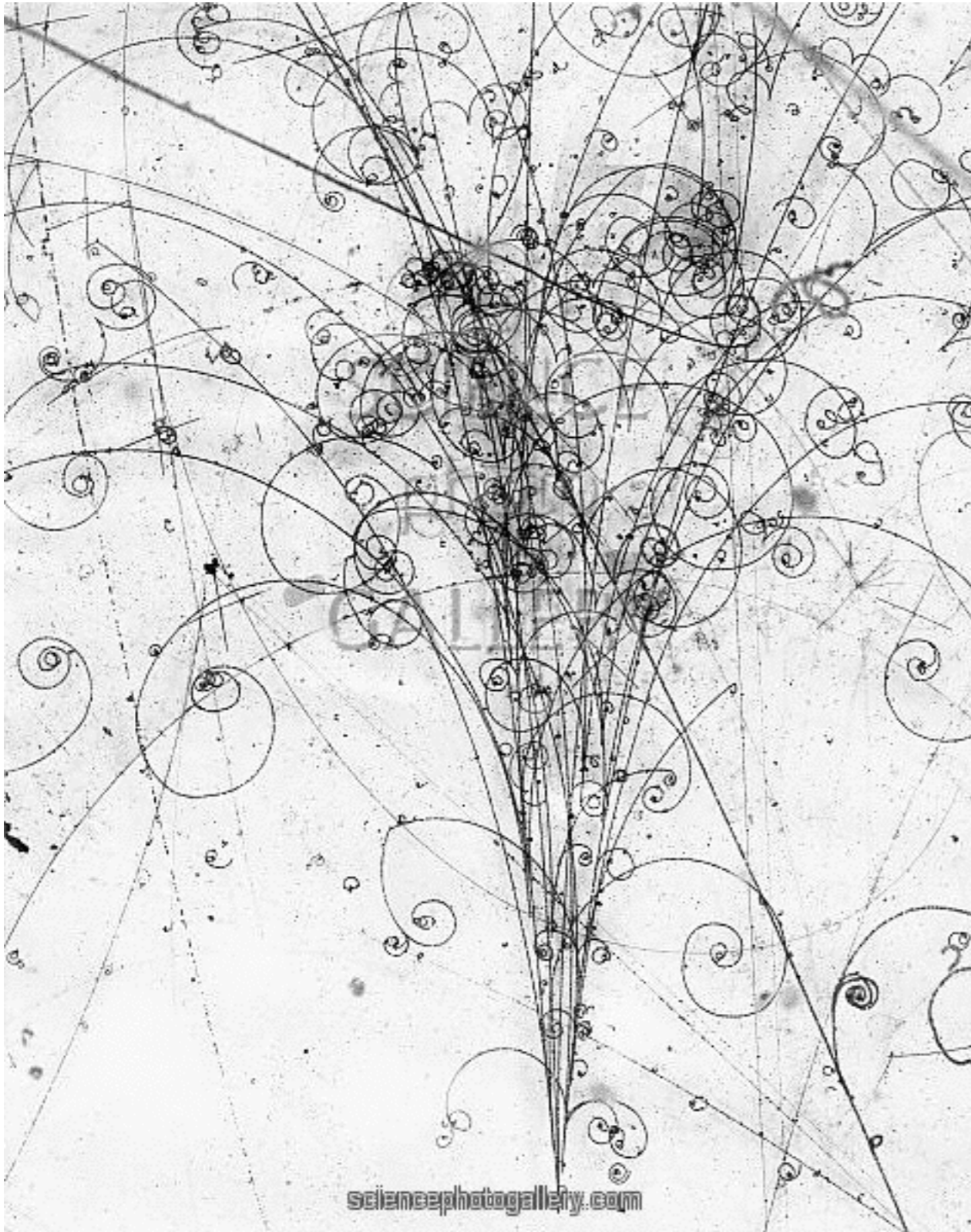
ELECTRONS AND PHOTONS



- electrons differ from other charged particles by their lightness and the presence of electrons in media
 - nuclear field can induce acceleration leading to radiation "bremsstrahlung"
- Photons will interact via Compton scattering or pair production at high energies



ELECTROMAGNETIC SHOWERS



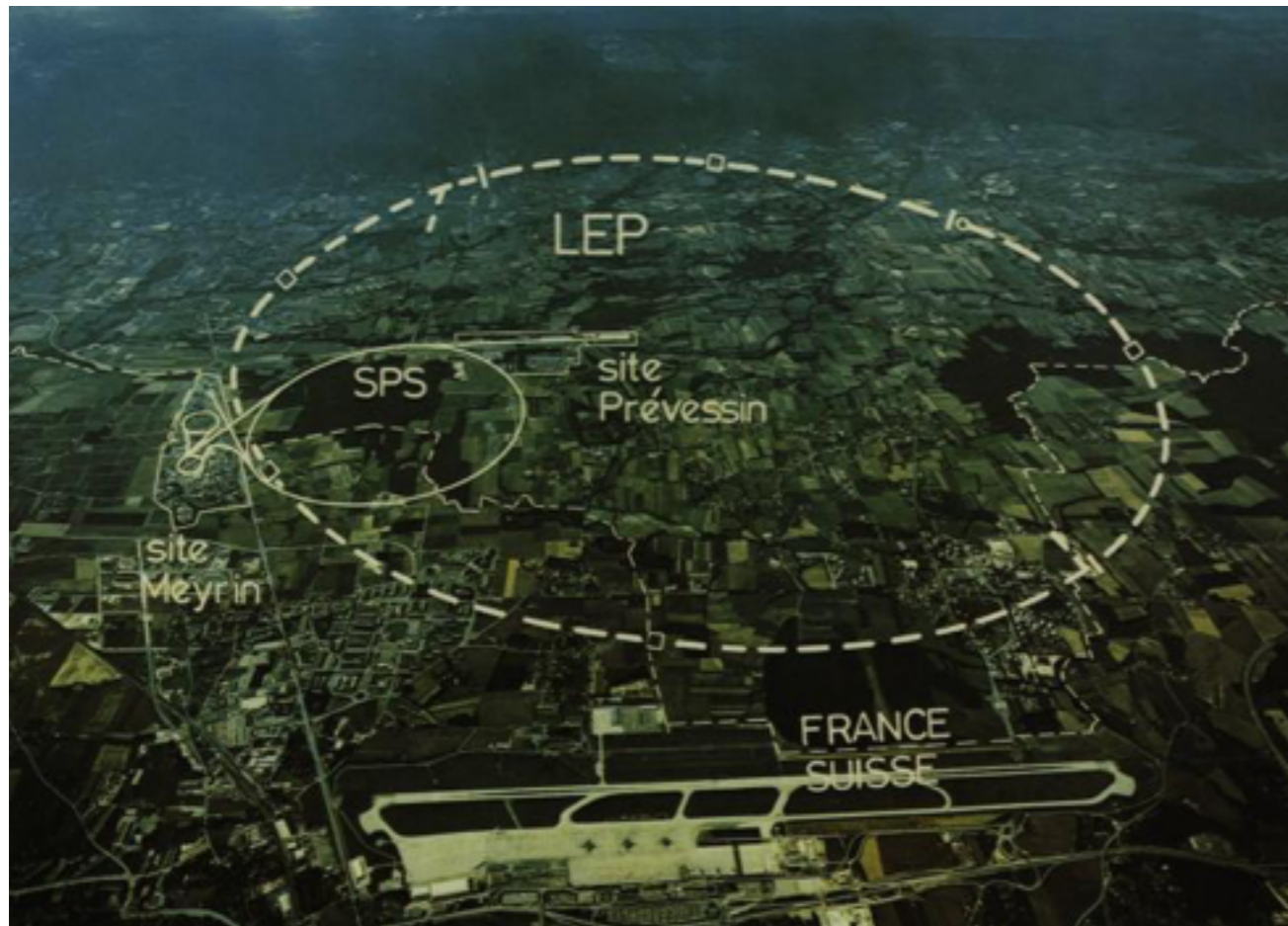
- Cascade of Bremsstrahlung, pair production, Compton scattering, etc.

ACCELERATORS



- Several generations of electron accelerators
 - CESR @ Cornell
 - SLAC linear accelerator
 - SLAC collider
- Also
 - PETRA at DESY (Hamburg, Germany)
 - TRISTAN at KEK (Tsukuba, Japan)
 - VEPP at BINP (Novosibirsk, Russia)
 - BES (Beijing, China)

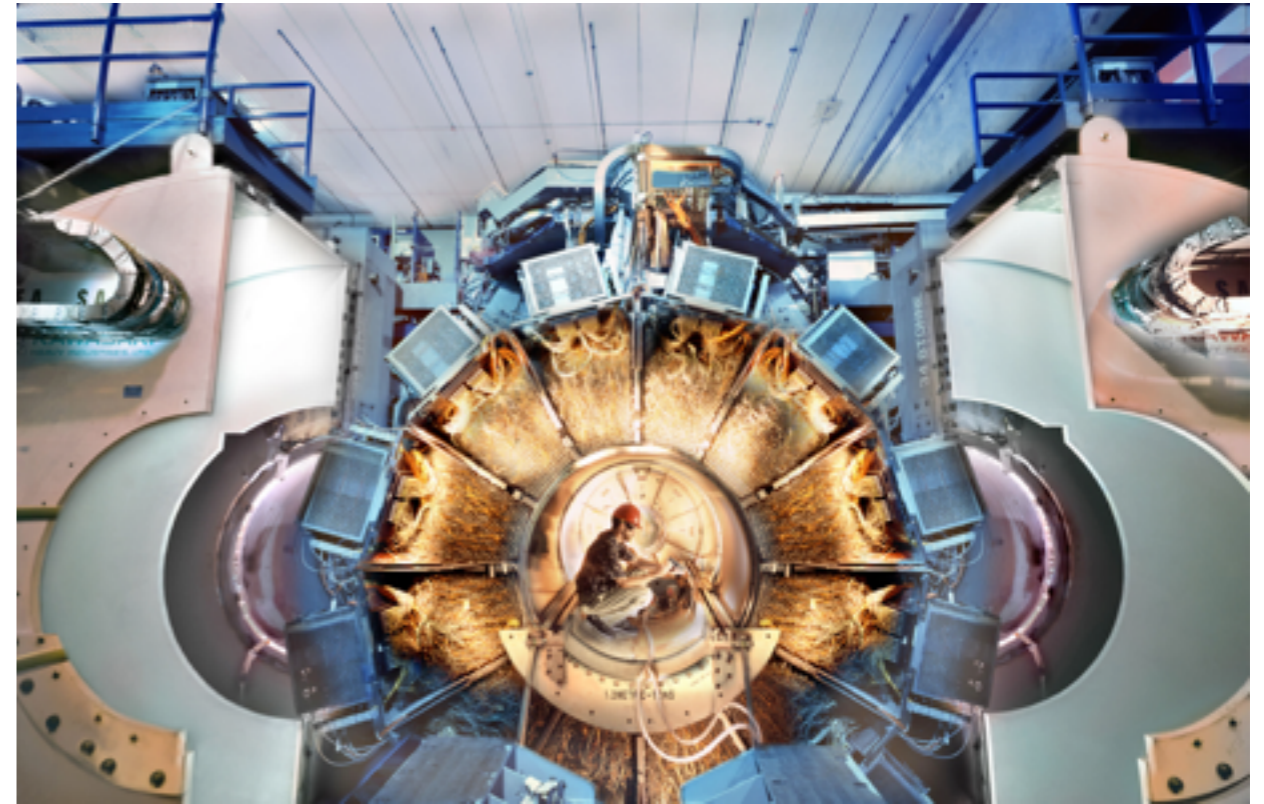
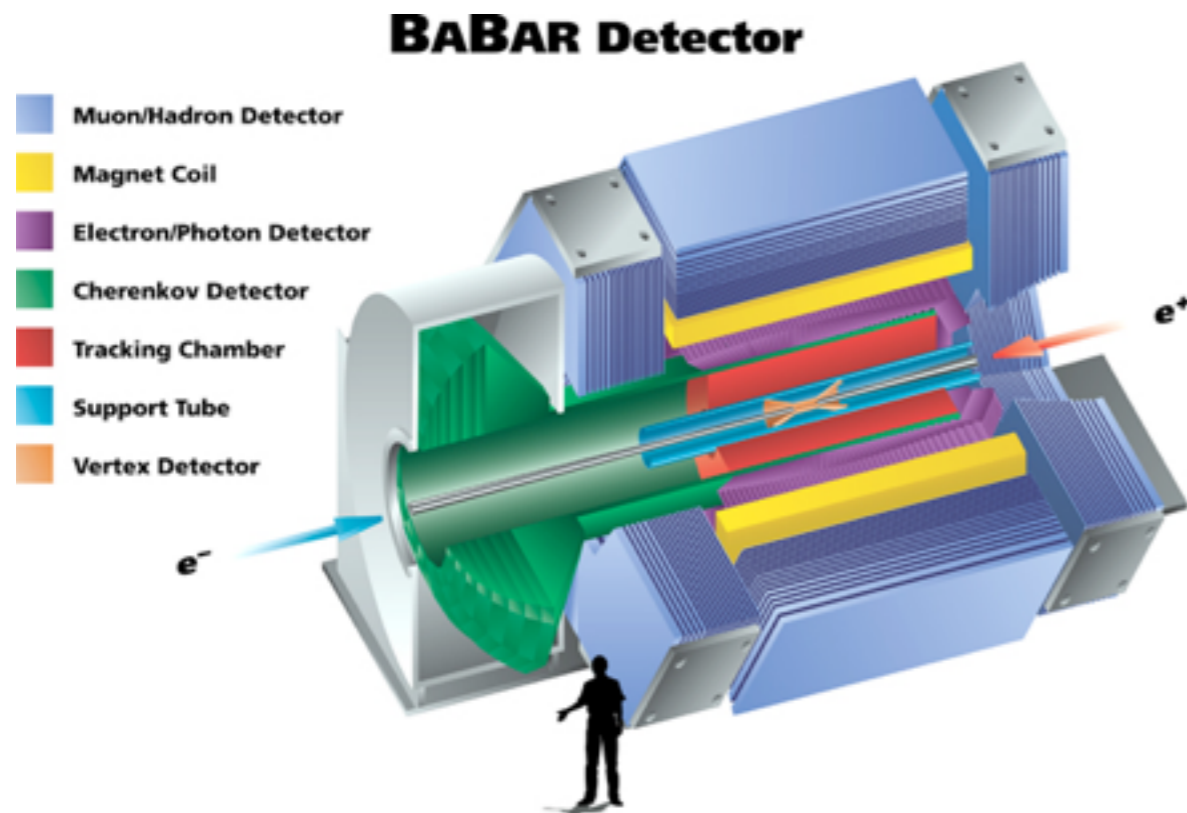
LEP



- Before the LHC there was LEP:
 - “large electron positron collider”
 - operated primarily at 91 GeV to study Z production and decays
- “LEP-II”:
 - increase of energy up to 209 GeV

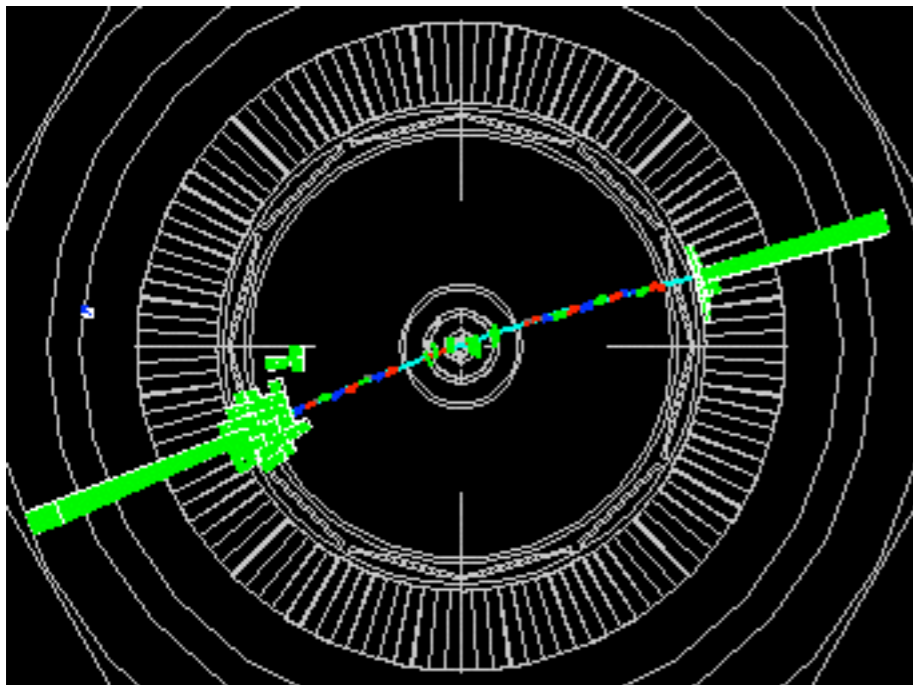


DETECTORS

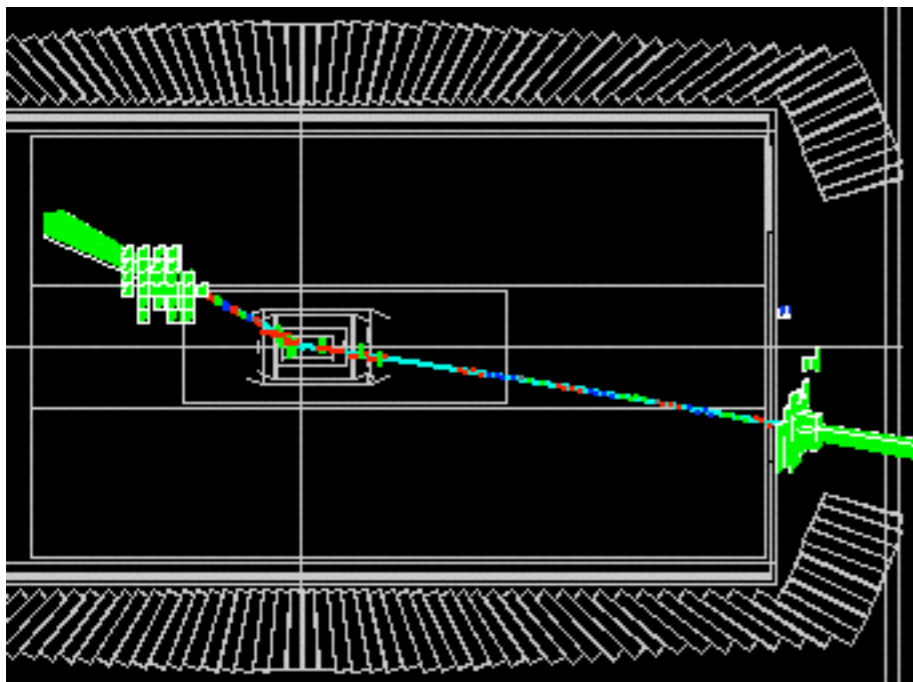


- Most collider detectors share a similar “cylindrical onion” design surrounding the interaction point
 - inner tracking region (silicon, drift chambers, etc.)
 - particle identification (Cherenkov counter, time-of-flight, etc.)
 - electromagnetic calorimeter (measure/identify electron/photon energy)
 - muon detector: identify muons by their penetration through lots of material
 - magnetic field throughout to bend particles and measure sign/momentum

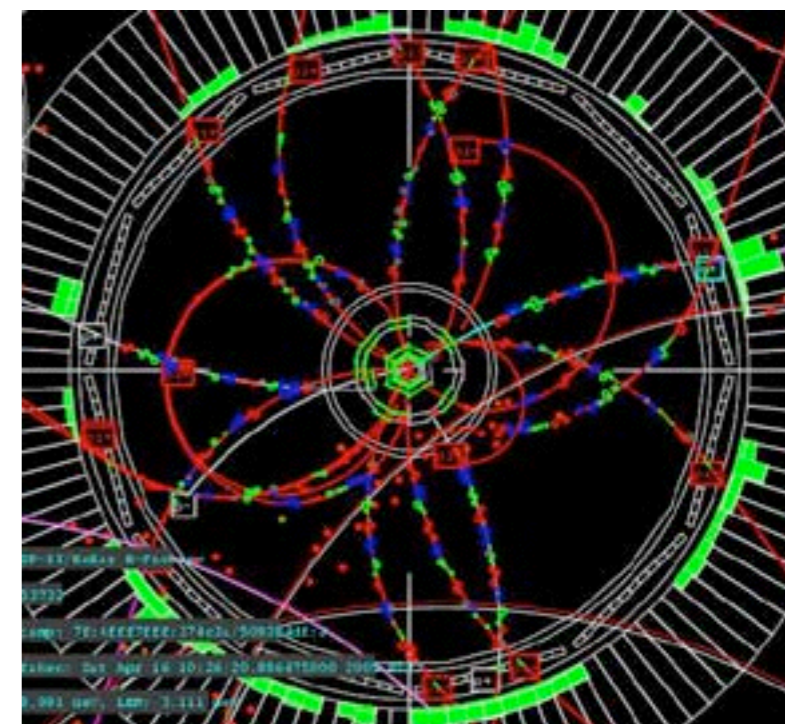
EVENTS AT BABAR



- $e^+ + e^- \rightarrow e^+ + e^-$ event ("Bhabha scattering")
 - "straight" track: high momentum
 - large deposition in electromagnetic calorimeter (green)
- $e^+ + e^- \rightarrow \mu^+ + \mu^-$ would look similar but with little calorimeter deposition



- "Hadronic" event at BaBar
 - $e^+ + e^- \rightarrow qq$
 - b and c quarks produced



τ PRODUCTION

- General expression without massless assumption:

$$\langle |\mathcal{M}|^2 \rangle = g_e^4 \left[1 + \left(\frac{mc^2}{E} \right)^2 + \left(\frac{Mc^2}{E} \right)^2 + \left[1 - \left(\frac{mc^2}{E} \right)^2 \right] \left[1 - \left(\frac{Mc^2}{E} \right)^2 \right] \cos^2 \theta \right]$$

- if we consider $e^+e^- \rightarrow t^+t^-$, we can still assume electron mass is ~ 0 , but keep the mass of the t .

$$\langle |\mathcal{M}|^2 \rangle = g_e^4 \left[1 + \left(\frac{Mc^2}{E} \right)^2 + \left[1 - \left(\frac{Mc^2}{E} \right)^2 \right] \cos^2 \theta \right]$$

- Now putting into our cross section formulas

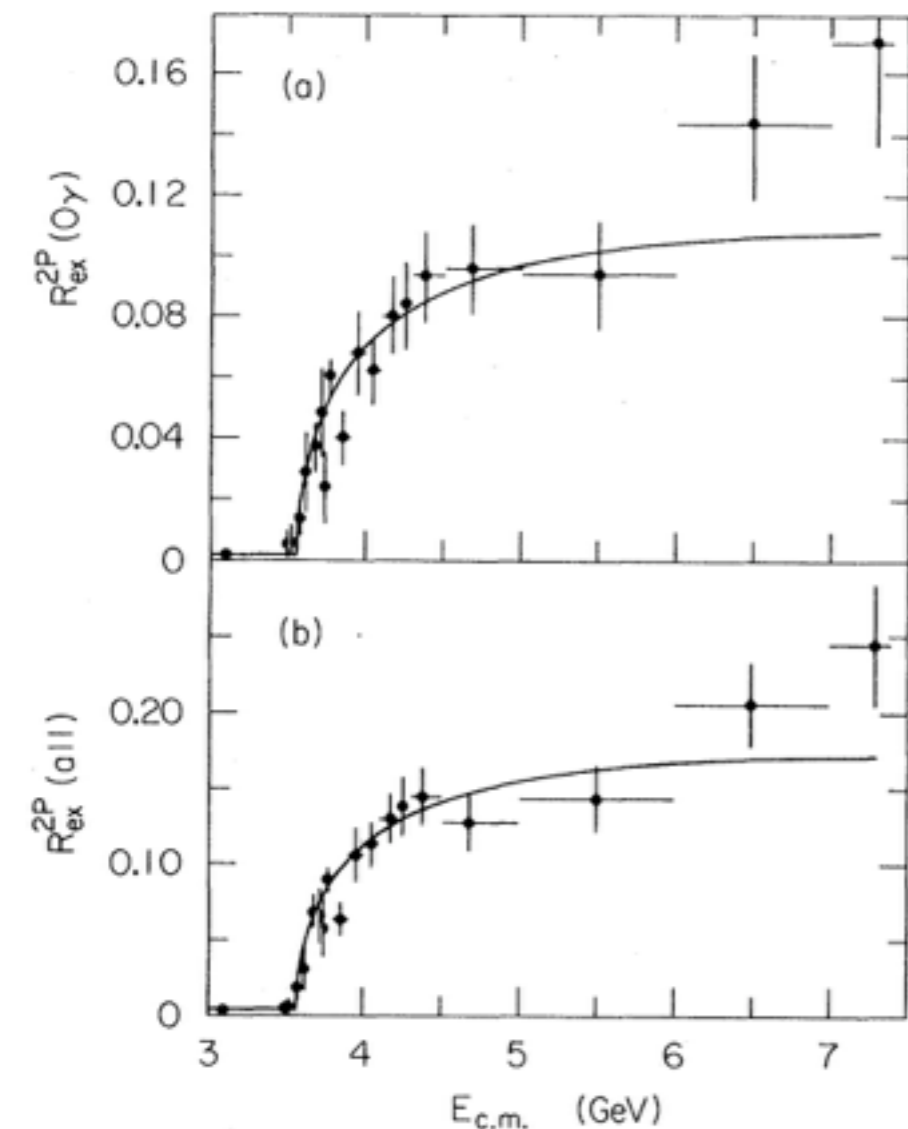
$$\frac{d\sigma}{d\cos\theta d\phi} = \left(\frac{\hbar c}{8\pi} \right)^2 \frac{\langle |\mathcal{M}|^2 \rangle}{4E^2} \frac{|p_f|}{|p_i|}$$

- Integrate to obtain total cross section

$$\sigma = \frac{\pi}{3} \left(\frac{\hbar c\alpha}{E} \right)^2 \sqrt{1 - (Mc^2/E)^2} \left[1 + \frac{1}{2} \left(\frac{Mc^2}{E} \right)^2 \right]$$

RATIO OF CROSS SECTIONS

- $e^+ + e^- \rightarrow \mu^+ + \mu^-$ has a very distinct signature in the detector.
- predict the ratio of τ production to μ production:

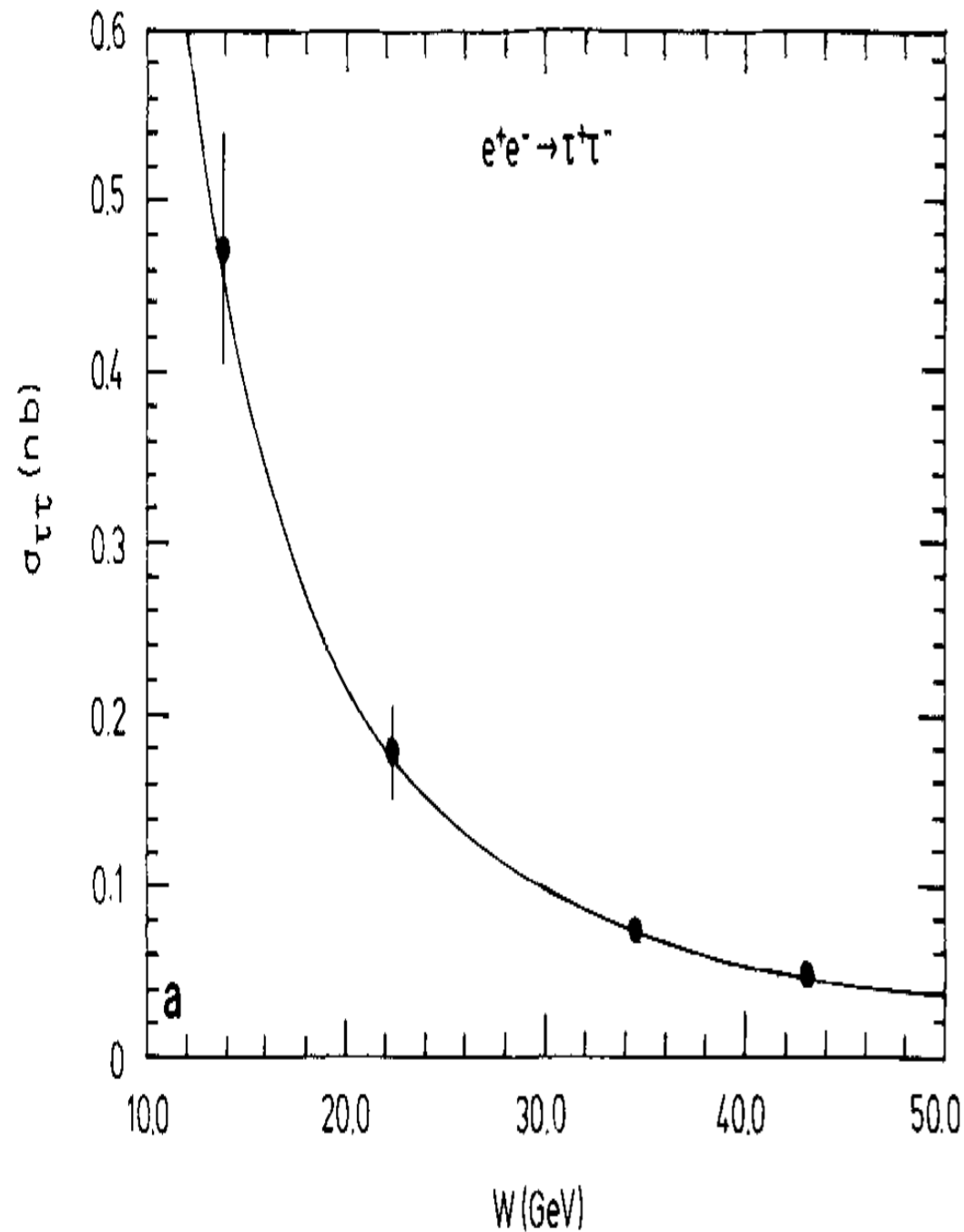


$$R_{\tau\mu} = \frac{\sigma_{\tau^+\tau^-}}{\sigma_{\mu^+\mu^-}} = \frac{\sqrt{1 - (M_\tau c^2/E)^2}}{\sqrt{1 - (M_\mu c^2/E)^2}} \times \frac{1 + \frac{1}{2}(M_\tau c^2/E)^2}{1 + \frac{1}{2}(M_\mu c^2/E)^2}$$

- Step the accelerator in energy
 - count the number of τ and μ produced at each energy
- Plot the ratio vs. beam energy
- Ratio depends on:
 - Dirac nature of τ
 - τ mass

TOTAL CROSS SECTION

- If we go to high energy ($E \gg m_\tau \sim 1.777 \text{ GeV}$)



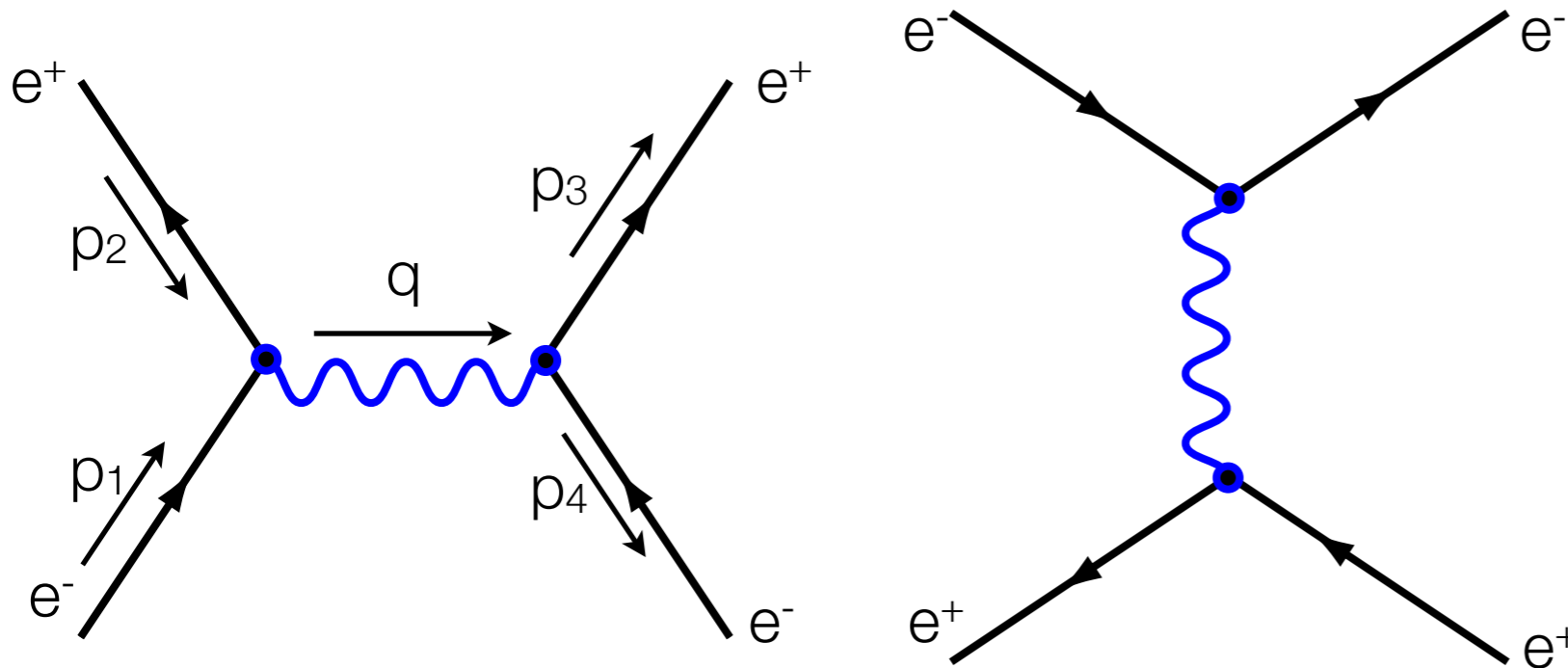
$$\sigma = \frac{\pi}{3} \left(\frac{\hbar c \alpha}{E} \right)^2 \sqrt{1 - (Mc^2/E)^2} \left[1 + \frac{1}{2} \left(\frac{Mc^2}{E} \right)^2 \right]$$

$$\sigma = \frac{\pi}{3} \left(\frac{\hbar c \alpha}{E} \right)^2 = 2.2 \times 10^{-5} \text{ mb}/E^2(\text{GeV}^2) = 22 \text{ nb}/E^2(\text{GeV}^2)$$

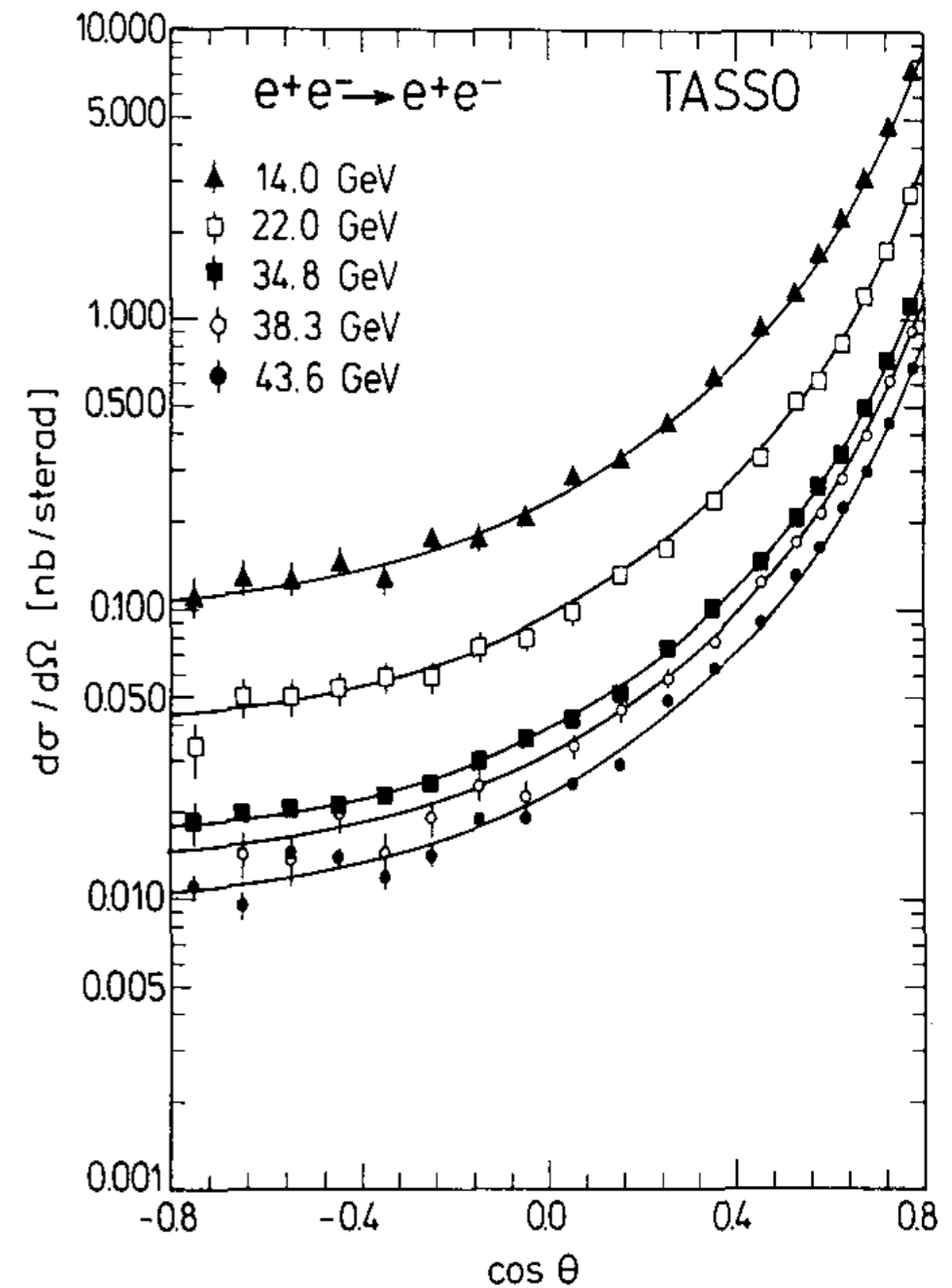
E (GeV)	Cross section (nb)
14	0.44
22	0.18
34	0.075
43	0.047

BHABHA SCATTERING

- $e^+ + e^- \rightarrow e^+ + e^-$
- additional diagram contributes



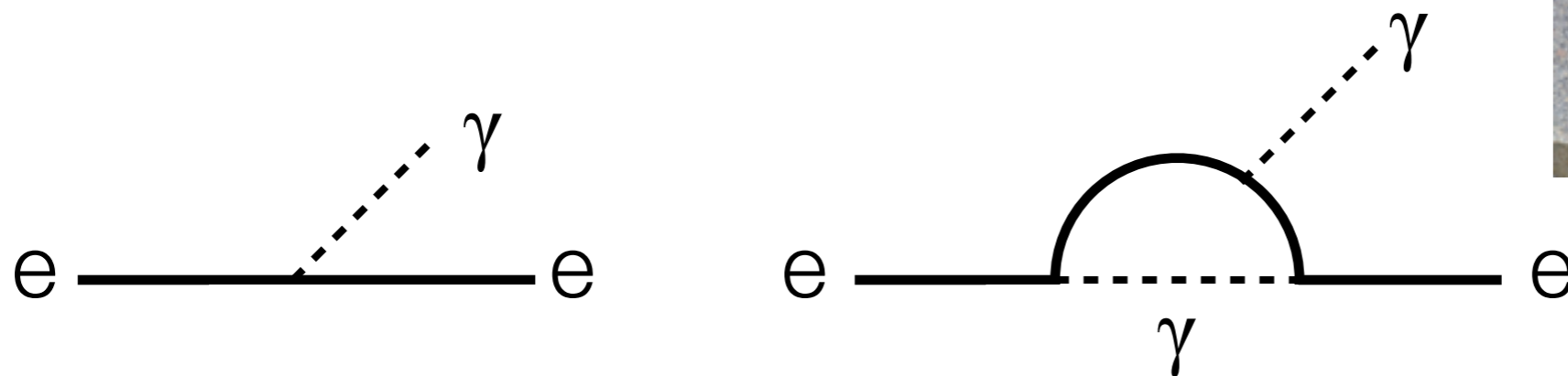
$$\frac{d\sigma}{d\cos\theta d\phi} = \left(\frac{\hbar c}{8\pi}\right)^2 \frac{g_e^4}{4E^2} \left(\frac{3 + \cos^2\theta}{1 - \cos\theta}\right)^2$$



THE "GYROMAGNETIC RATIO"

$$\mu = g\mu_B s/\hbar \quad \mu_B = \frac{e\hbar}{2m}$$

- Ratio of magnetic moment to the spin x Bohr magneton
- This is not exactly 2 for an electron
 - higher order electromagnetic corrections
 - $a = (g-2)/2 = \sim 0.0011596521807328$
 - "anomalous" moment
 - first calculated by Julian Schwinger in 1948
 - $a \sim \alpha/2\pi = 0.0011614$



THE MUON $g-2$ EXPERIMENT

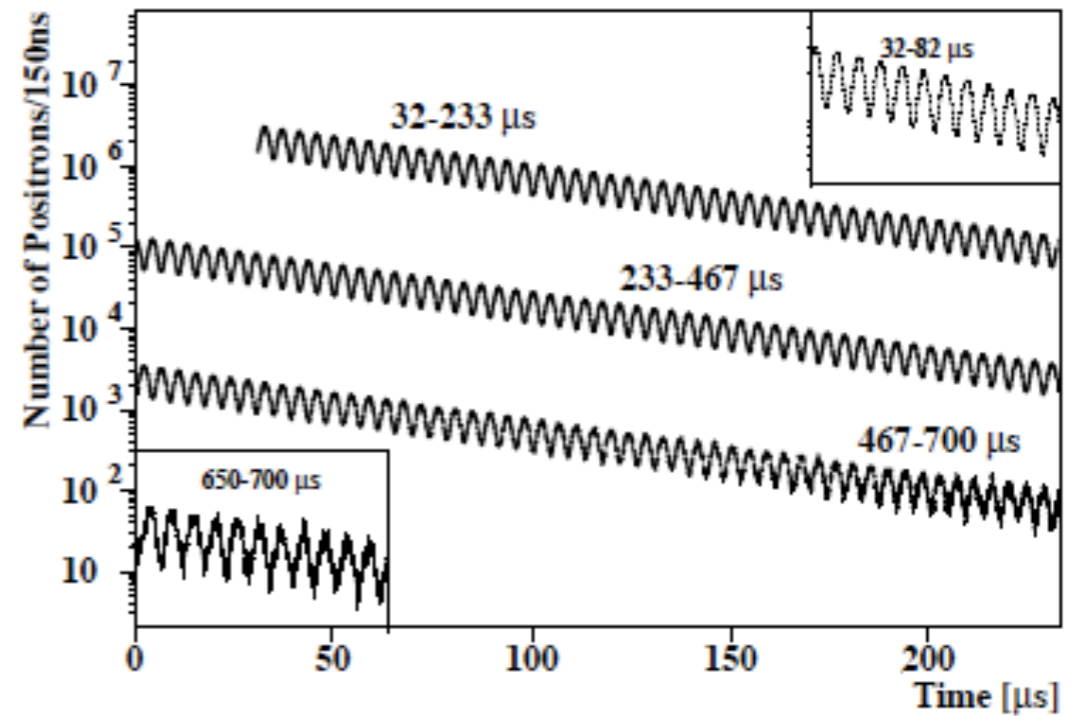
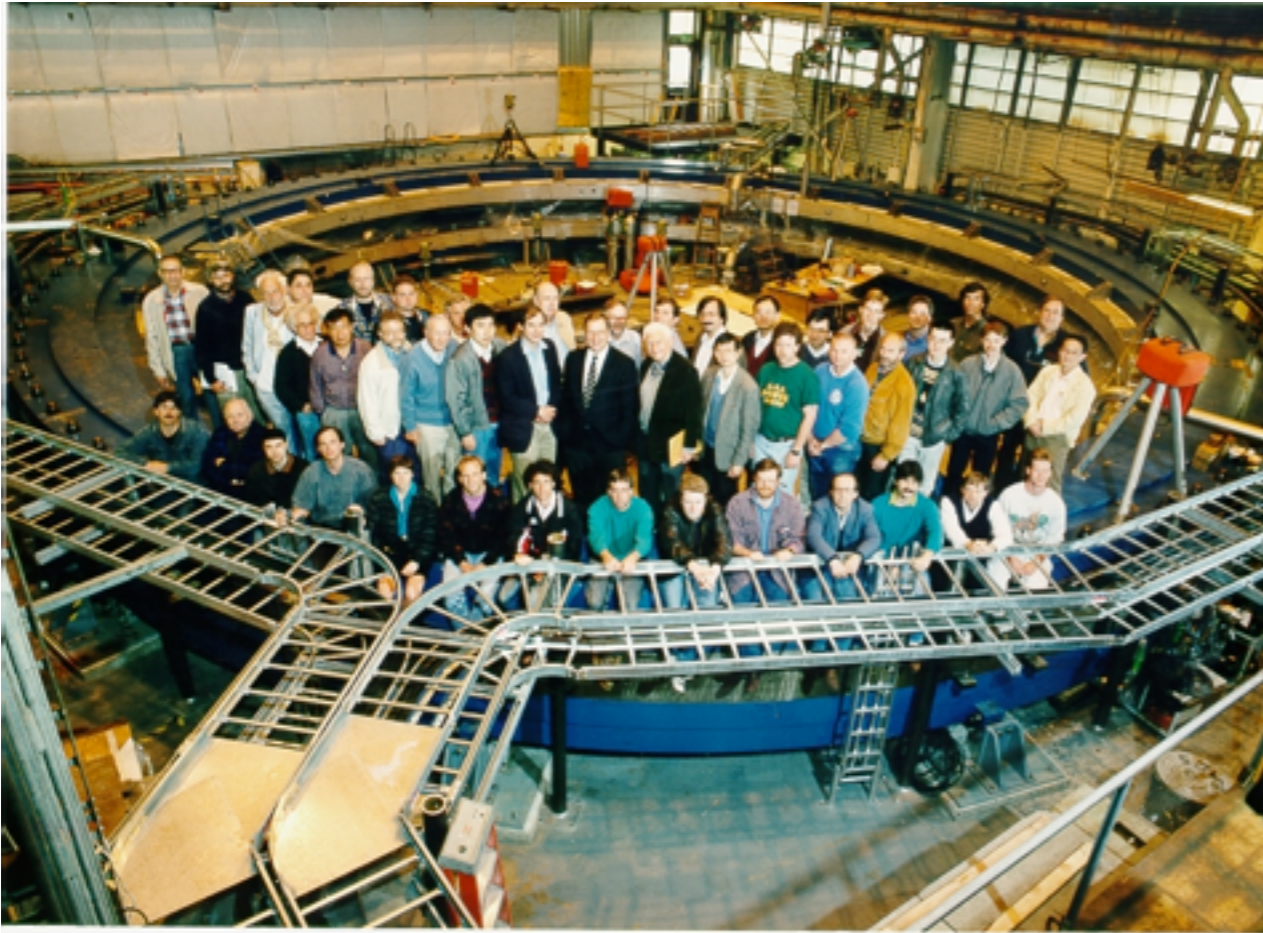
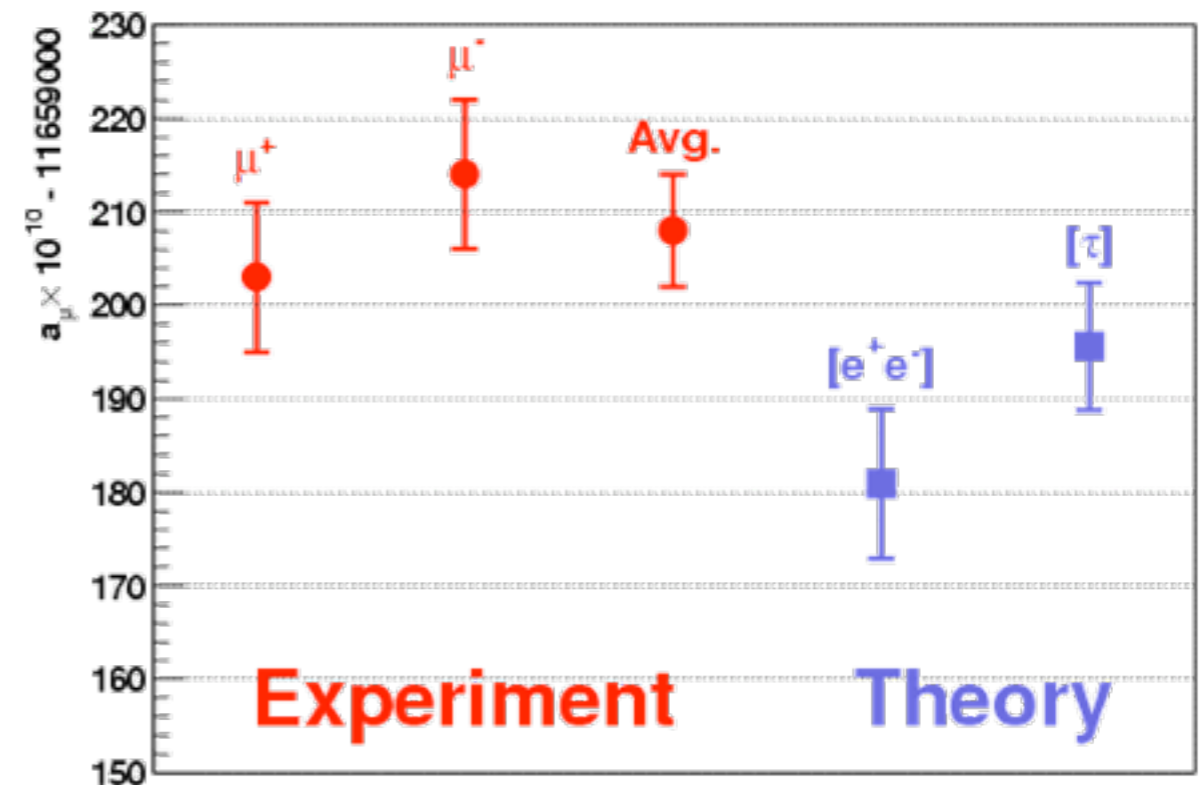


FIG. 3. Positron time spectrum overlaid with the fitted 10 parameter function ($\chi^2/\text{dof} = 3818/3799$). The total event sample of $0.95 \times 10^9 e^+$ with $E \geq 2.0$ GeV is shown.

- Precess muon spin in a magnetic field as it circulates around a ring
 - direction of electron emerging from muon decay is correlated with its polarization
 - measure the precession of the spin to extract magnetic moment
- Predicted $(g-2)/2 = (1165918.81 \pm 0.38) \times 10^{-9}$
- Measured $(g-2)/2 = (1165920.80 \pm 0.63) \times 10^{-9}$



SUMMARY

- Please read Chapter 7 for next time